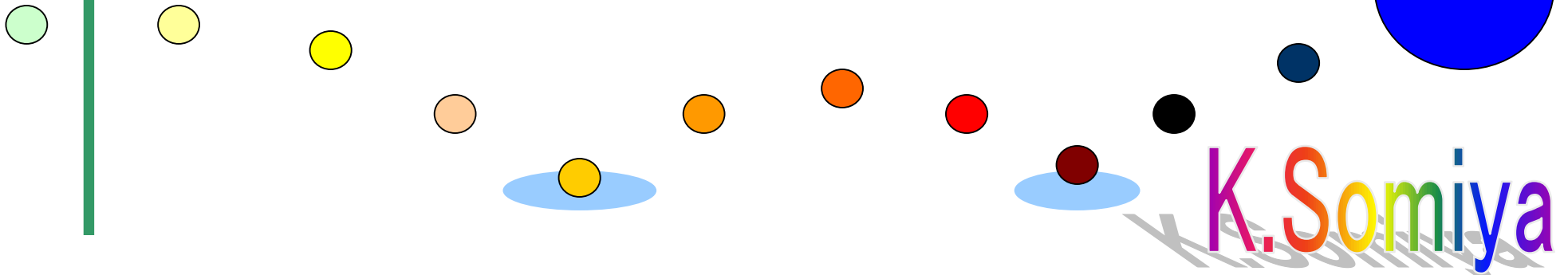


# Reaching the quantum limit with a gravitational wave telescope

Aspects of Quantum Information and Quantum Foundations  
Feb 2023

Tokyo Tech  
Kentaro Somiya



# Gravitational waves

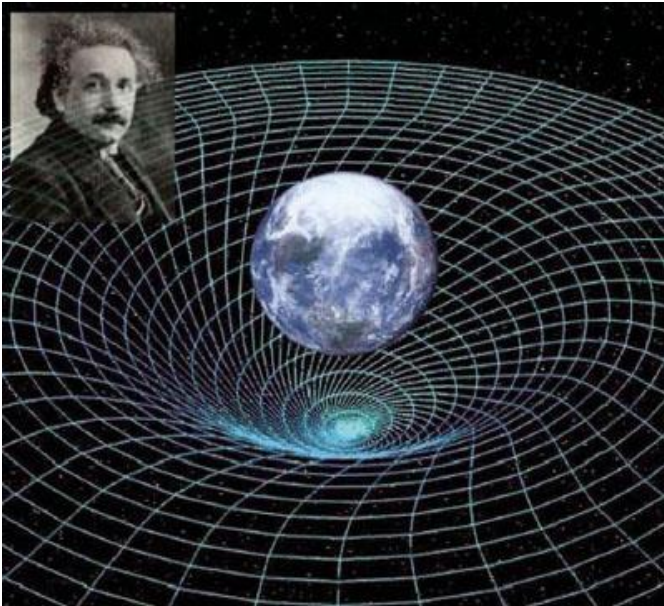


**Newton's gravity  
="distant force between an apple  
and Earth"**

**Einstein's gravity  
="free fall in curved spacetime"**



**"dynamic change of spacetime  
must propagate as a wave"**



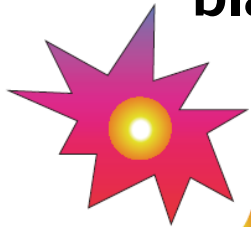
**Einstein's prediction  
of gravitational wave**

**(1916)**

# Laser interferometric GW detector

Far universe

supernovae, neutron star,  
blackhole merger, etc.



Gravitational Waves

Massive astronomical events

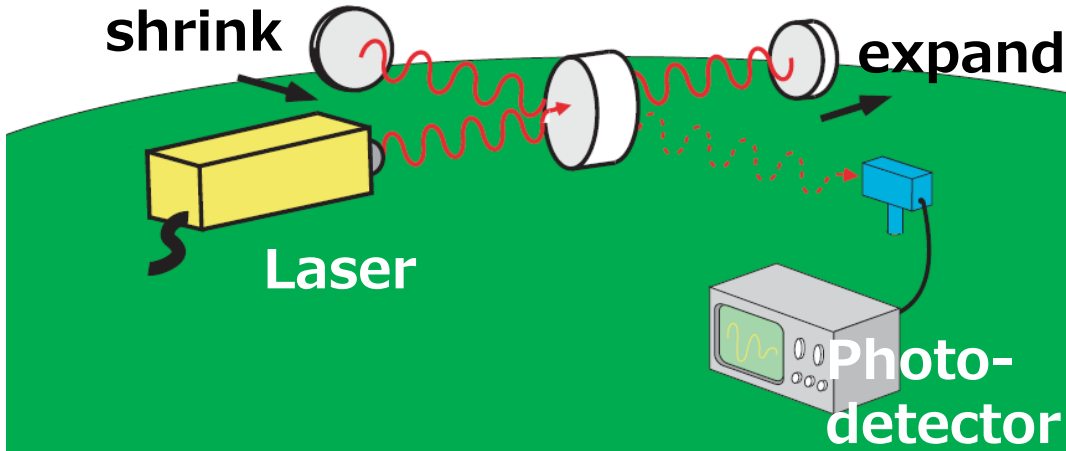


Optical path length changes



Can be observed by  
a large interferometer

shrink expand



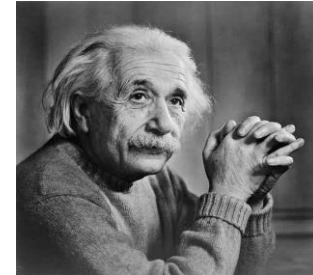
Earth

- LIGO in US [4km]
- Virgo in Italy [3km]
- GEO in Germany [600m]
- KAGRA in Japan [3km]

# GW detector history

1916 Einstein's prediction of GW

1969 Weber's announcement of first detection  
(considered as noise)



1974 Indirect measurement of GW by Hulse&Taylor  
(1993 Nobel Prize)

1999 TAMA (JP) started observation

2002 LIGO (US) started observation

2005 GEO (GE/GB) started observation

2007 Virgo (IT/FR) started observation

2009 LIGO-Virgo joint run for 1 year  
(no GW detected)

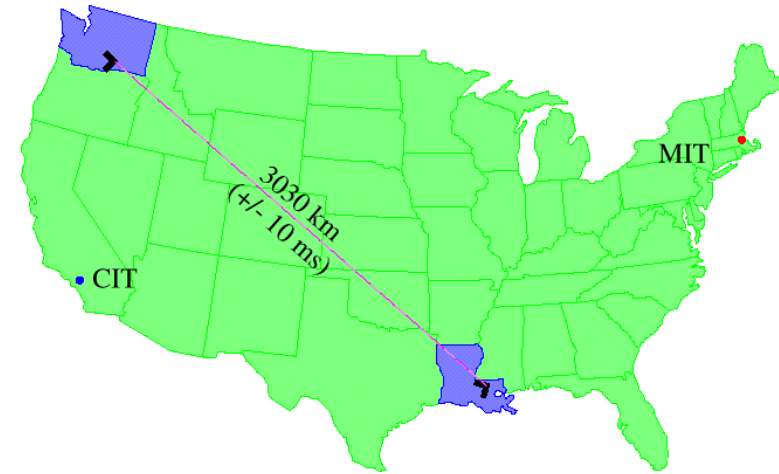
2010 Upgrade to second generation GWs  
KAGRA's construction started in Japan

2015 Advanced LIGO's **first detection**





# Advanced LIGO



- 4km interferometer x2
- 10-times better sensitivity than LIGO
- Started obs. in 2015





# KAGRA

Kamioka, Gifu pref.

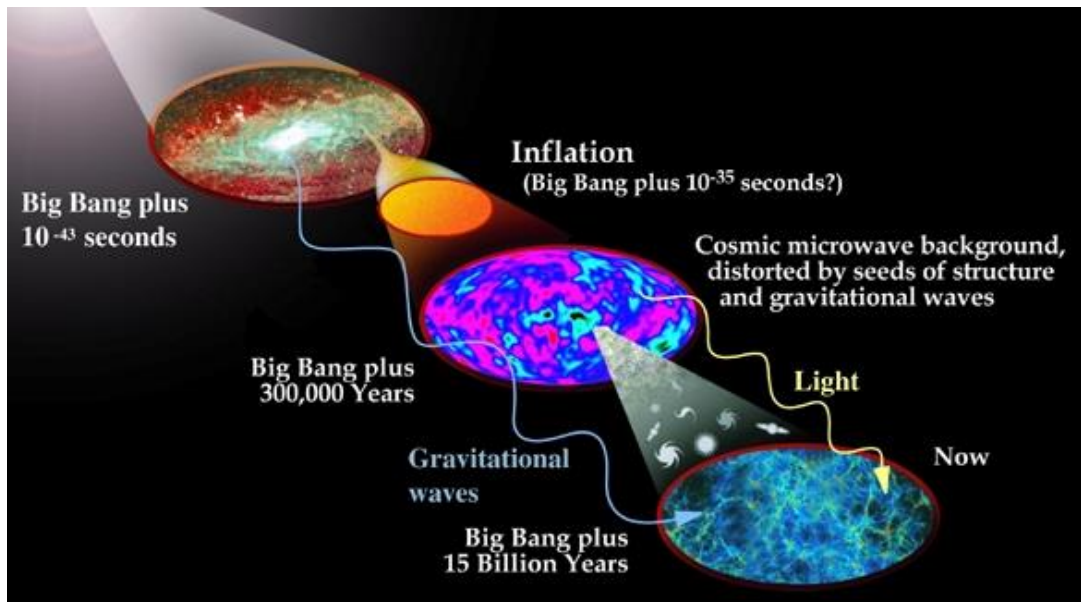


- 3km interferometer
- Underground
- Cryogenic mirrors
- Joined the observation run in 2020



# What can we learn from GW?

[image:NASA]



Interaction with matter is weak



Information is different from EM

- Proof of Einstein's theory
- Early universe
- Blackhole population
- Binary neutron star merger



GR



Cosmology



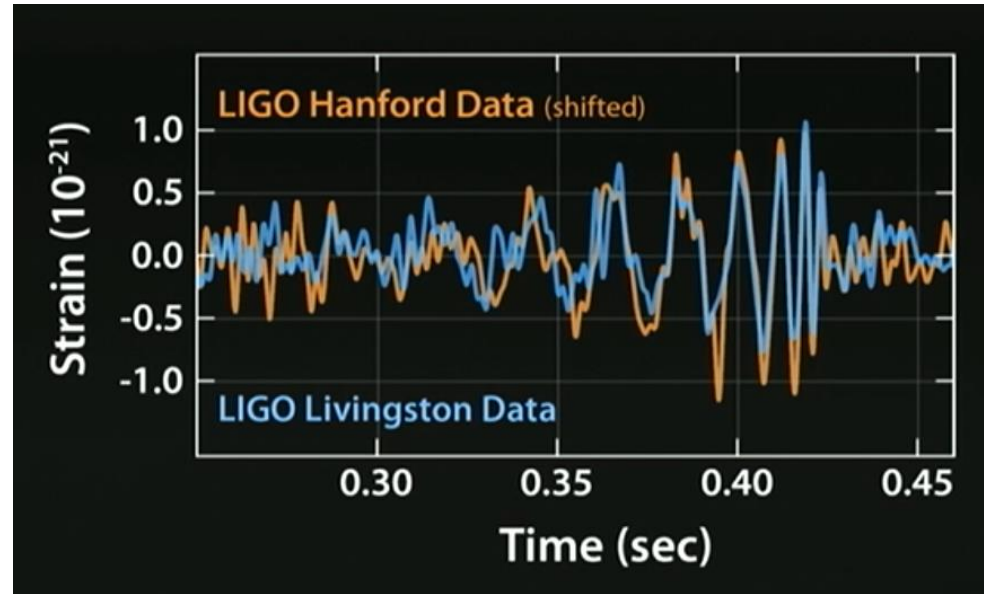
Astronomy



Nuclear Phys



# Advanced LIGO's first detection

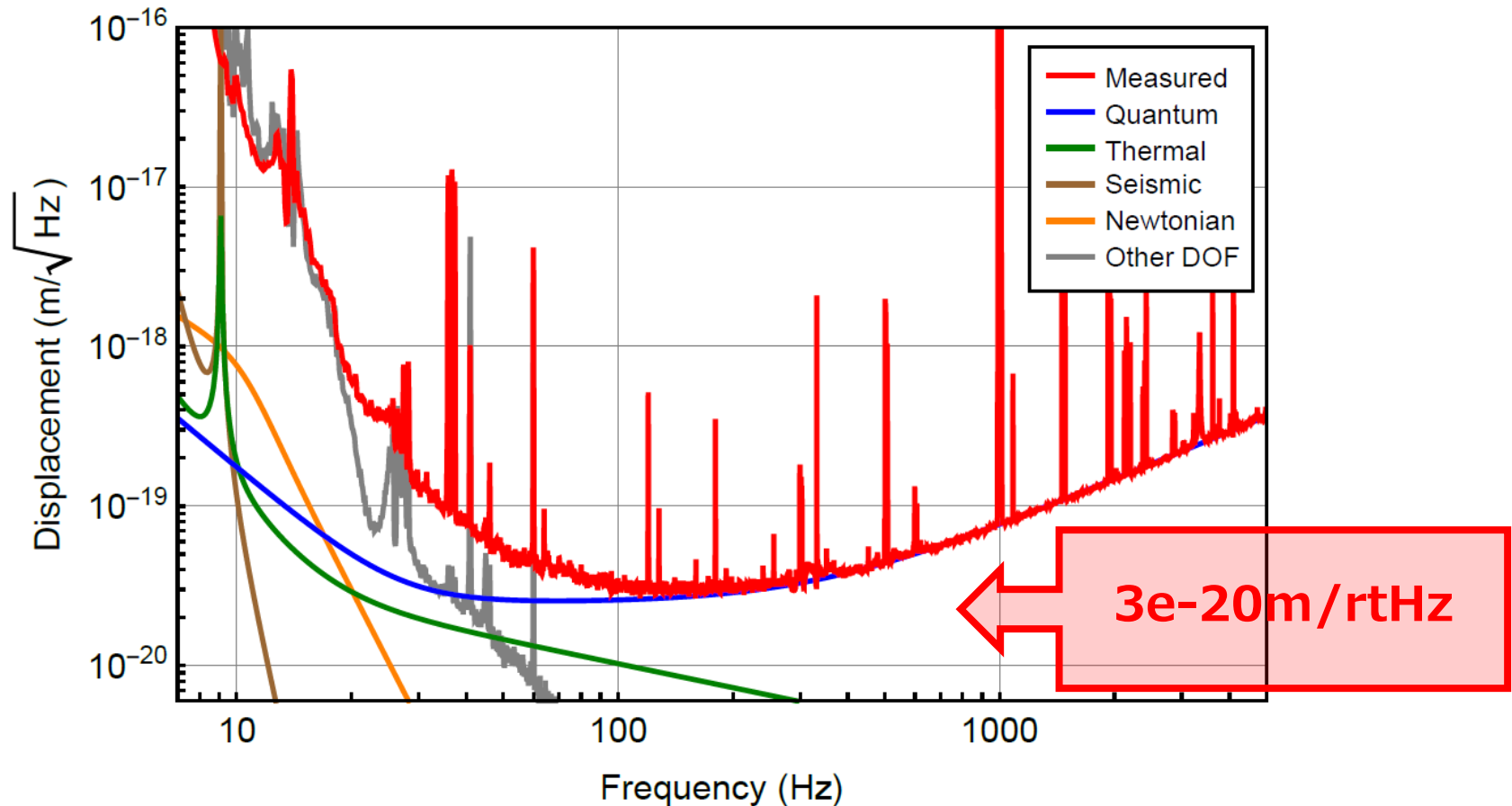


- Binary blackholes with 36 and 29 solar masses
- 62 Ms BH was generated after the merger
- Two detectors observed it with a 10-ms time diff.
- Waveform matched to numerical relativity prediction
- The source is 1.3B light-years from Earth
- SNR was 24 and FAR was 1/200k-yrs or less

(False Alarm Rate)



# Sensitivity of Advanced LIGO in 2015



- Mainly limited by quantum and control noises
- The sensitivity is x2 better in 2022

# Contents of the talk

## **1. Gravitational waves**

## **2. Sensitivity of GW detectors**

**2-1. Quantum noise (of light)**

**2-2. Thermal noise**

**2-3. Seismic+Newtonian noise**

## **3. Toward the standard quantum limit**

## **4. Summary**

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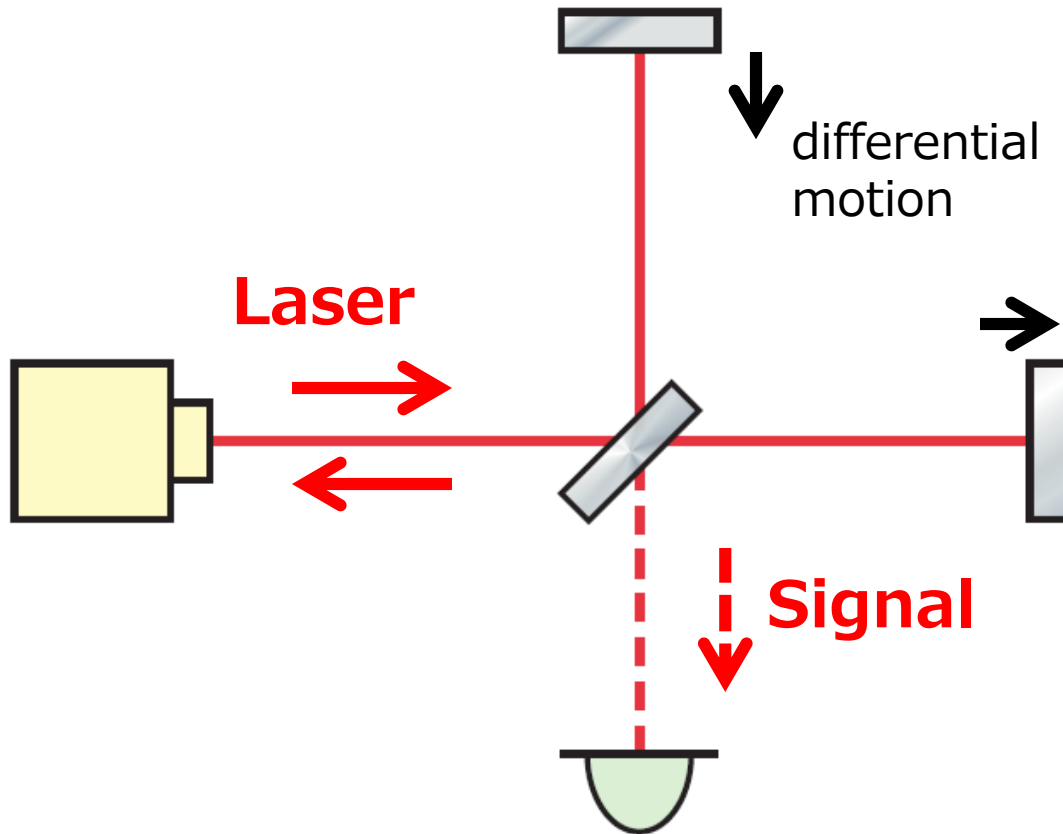
**3. Toward the standard quantum limit**

**4. Summary**

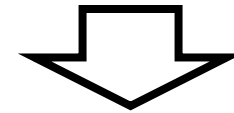


# Quantum noise

(IFO=Interferometer  
GW=Gravitational Waves)



**Operating Michelson IFO at dark fringe**  
(Light goes back to laser)

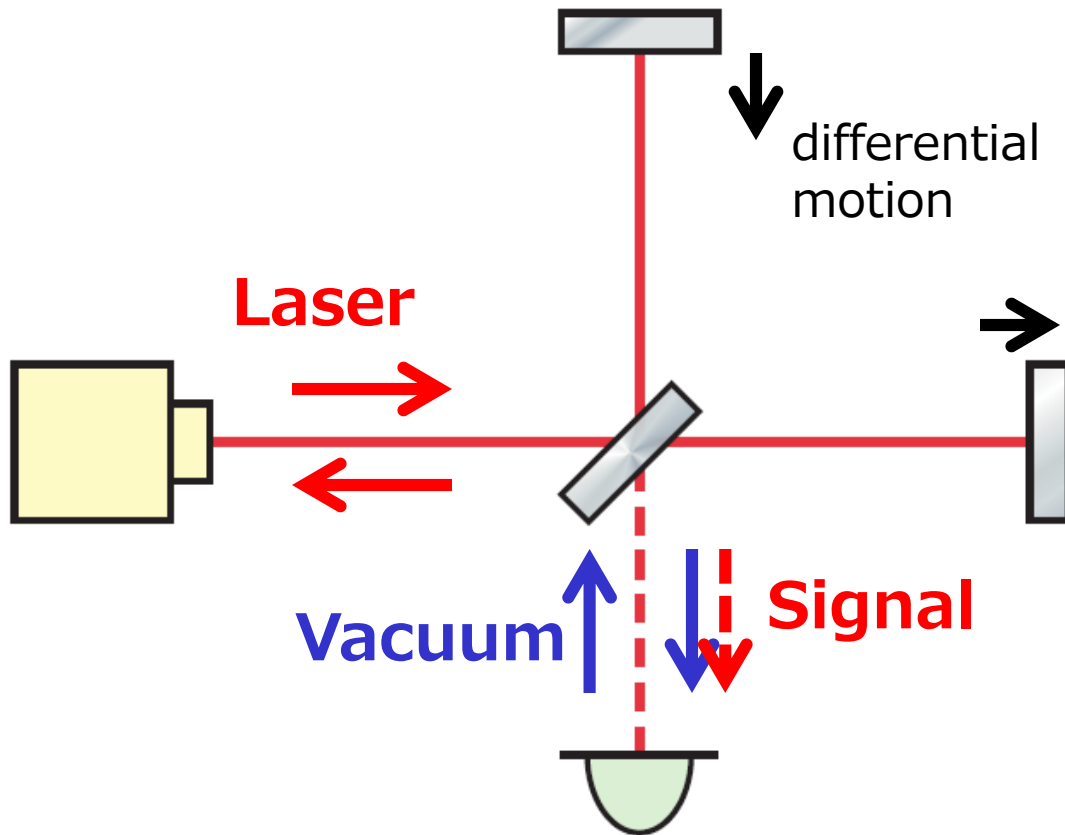


**GW causes differential motion of the mirrors to send signal light to the dark port.**

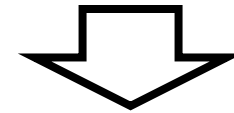
**Laser fluctuation goes back to the laser.  
⇒ What would be the noise source then?**

# Quantum noise

(QN=Quantum Noise  
SNR=Signal-to-Noise Ratio)



**Even without light,  
there exists vacuum**  
(zero mean, non-zero variance)

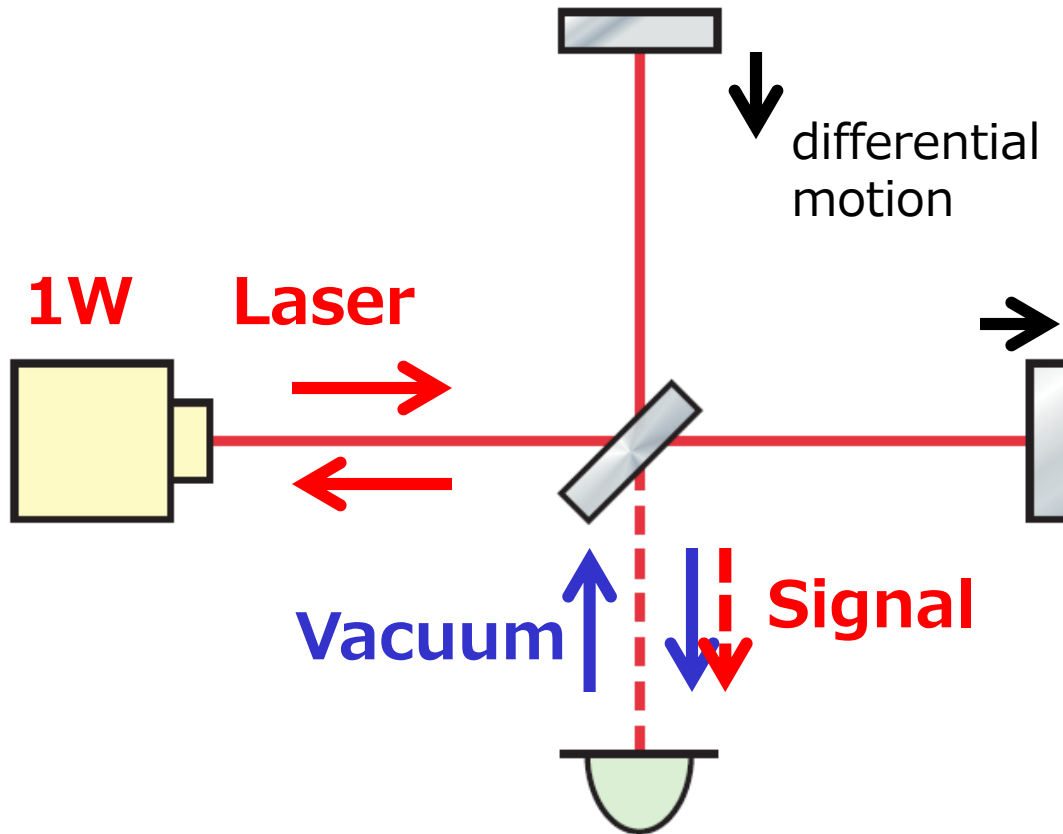


**Vacuum field entering  
from dark port is the  
source of QN.**

**Vacuum fluctuation is equivalent to  $\frac{1}{2}$  photon  
 $\Rightarrow$  SNR is defined by the ratio to signal photons**

# Quantum noise

(IFO=Interferometer  
GW=Gravitational Waves)



**1W laser light contains  
 $N=5e18$  photons/sec.**  
( $\lambda$  is set to 1064nm)

As GW changes the path  
length by  $\Delta L$ ,

$$\Delta N = \left( \sqrt{N} \frac{4\pi\Delta L}{\lambda} \right)^2 \text{ photons}$$

leak to the dark port

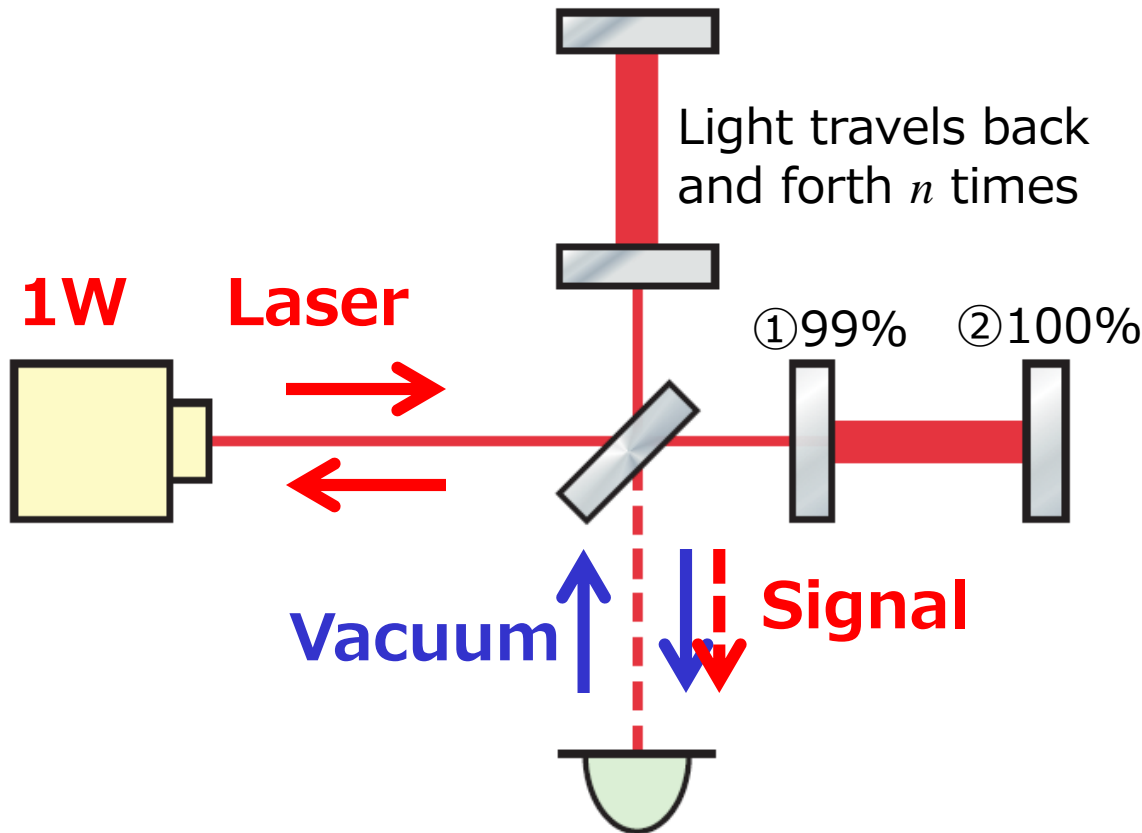
Sensitivity is given by solving  $\Delta N \sim 1/2$

$\Rightarrow$  For 1W IFO, it is  $\Delta L=5e-17(m/\text{rtHz})$



# Optical cavity

(IFO=Interferometer)



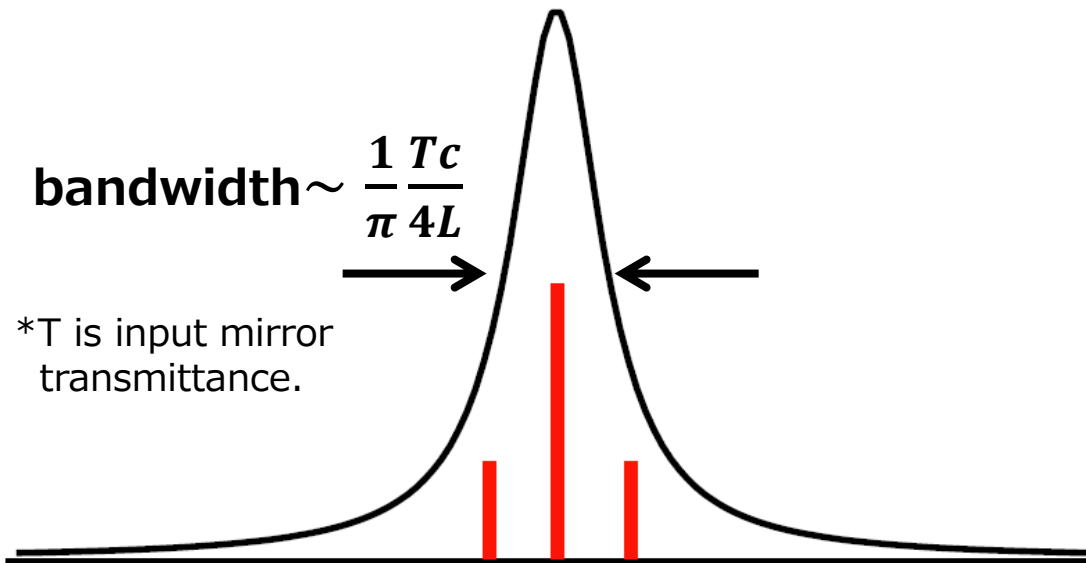
With a cavity to circulate light 400 times, both  $\sqrt{N}$  and  $\Delta L$  increase by 400

$$\Delta N = \left( 400^2 \times \sqrt{N} \frac{4\pi\Delta L}{\lambda} \right)^2$$

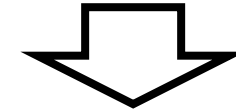
Sensitivity is given by solving  $\Delta N \sim 1/2$   
 $\Rightarrow$  For 1W IFO, it is  $\Delta L=1e-19(m/rtHz)$

# Optical cavity

(BW=Bandwidth)



**Signal outside bandwidth will not increase in cavity.**

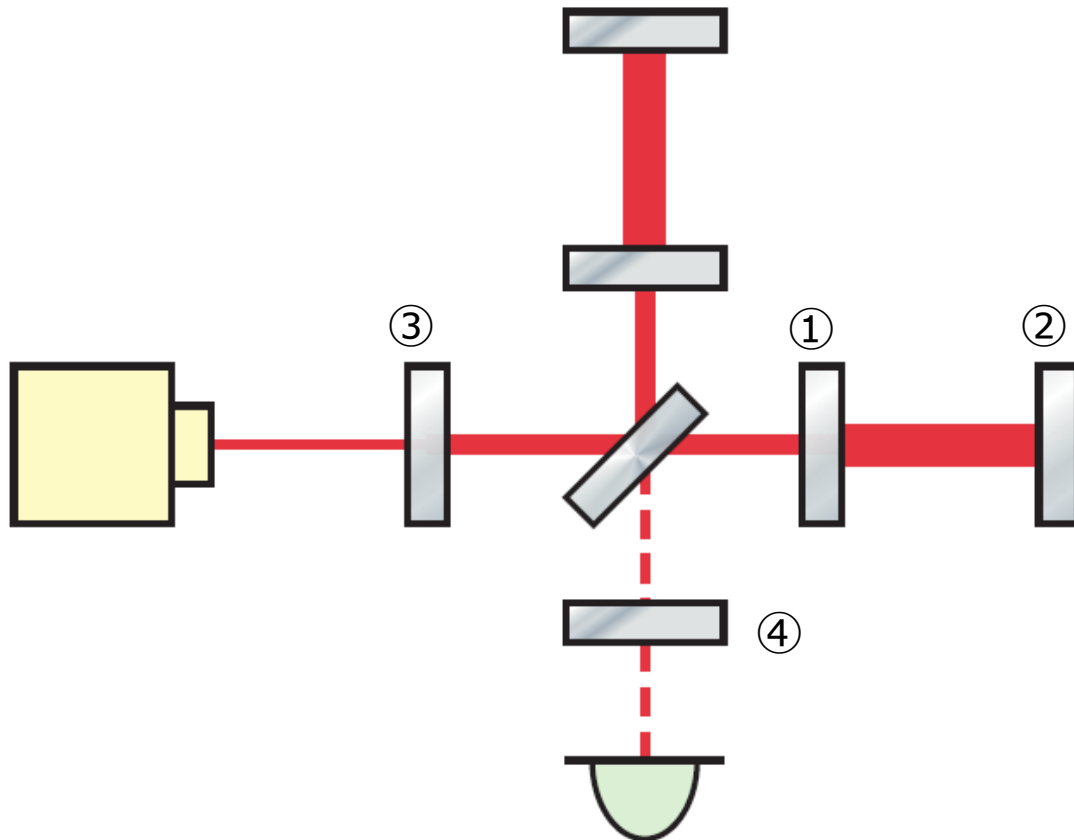


**With 99% input mirror and L=4km, BW is  $\sim 30$ Hz.**

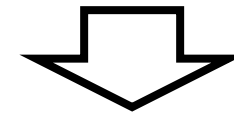
**We like to have more light in the cavity  
but we do not want to decrease the BW  
 $\Rightarrow$  A coupled cavity**

# Coupled cavity

(BW=Bandwidth  
BS=Beam Splitter)



**Coupled cavity w/ ①②③  
determines the power.  
Coupled cavity w/ ①②④  
determines the BW.**



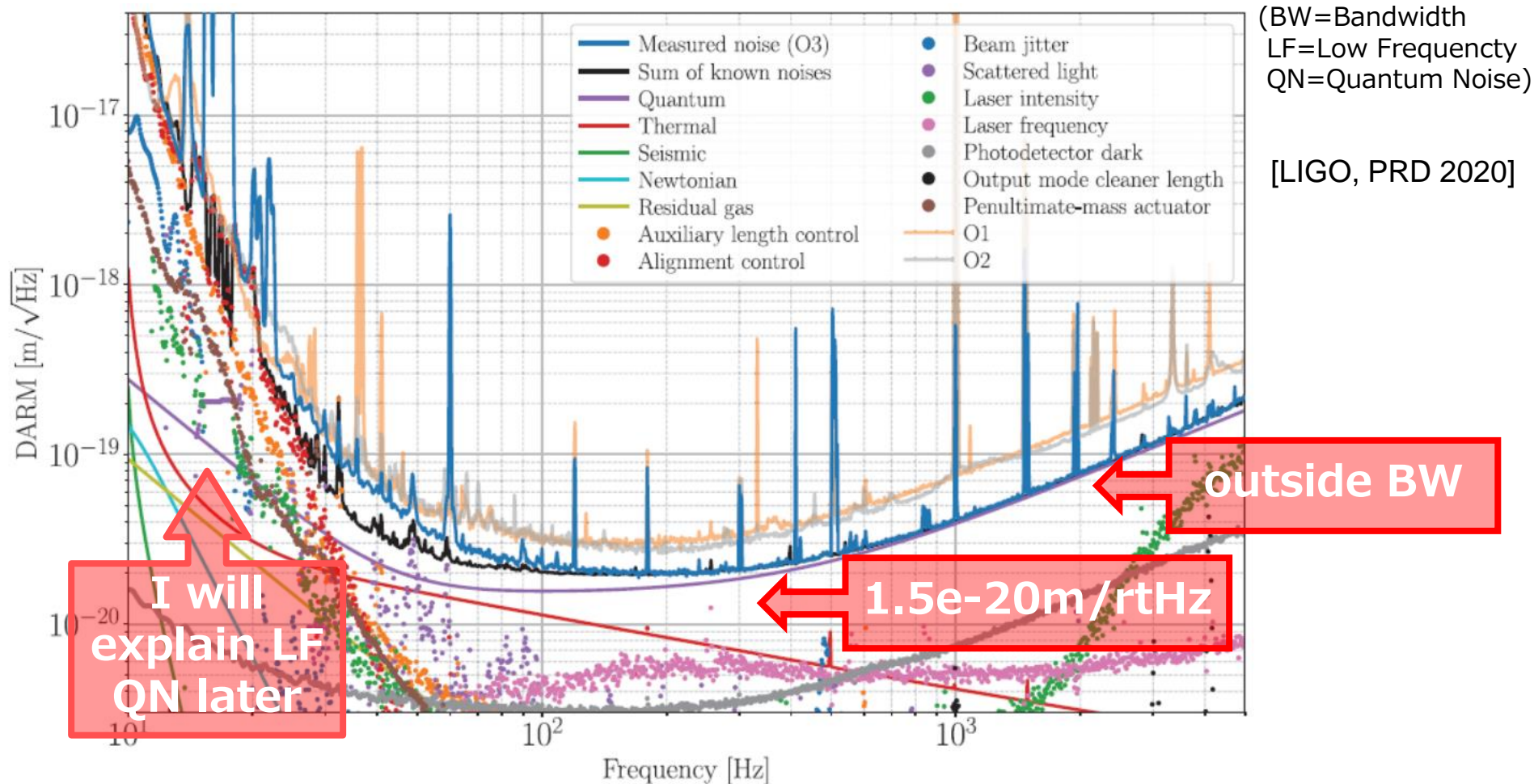
**"Power-recycled  
Resonant-sideband-extraction"**

**Both Advanced LIGO &  
KAGRA use this system.**

**Currently, Advanced LIGO uses  $\sim 1.5\text{kW}$  at BS  
and sensitivity reaches  $\Delta L = 2e-20(\text{m}/\text{rtHz})$ .**



# Quantum noise of LIGO in 2020



**A 3dB squeezing was injected to effectively double the arm power (to be explained later).**

# Contents of the talk

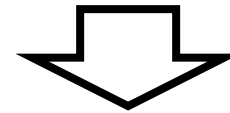
1. Gravitational waves
2. Sensitivity of GW detectors
  - 2-1. Quantum noise (of light)
  - 2-2. Thermal noise
  - 2-3. Seismic+Newtonian noise
3. Toward the standard quantum limit
4. Summary

# Thermal noise

(TN=Thermal Noise,  
1/Q represents dissipation)

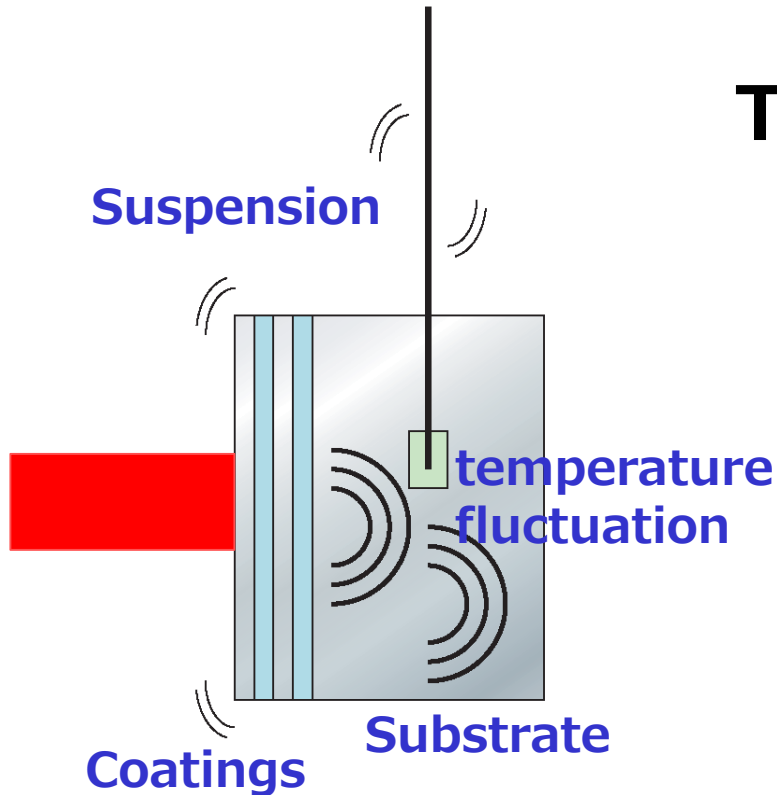
Thermal noise is given by

$$\frac{1}{2}mv^2 = \frac{k_B T}{Q}$$



$$\tilde{x} \sim \sqrt{\frac{2k_B T}{Qm\Omega^3}} \sim 9 \times 10^{-21} \text{ (m/rtHz)}$$

(Suspension TN at 100Hz)



Each thermal noise level is calculated with the fluctuation-dissipation theorem.

# Thermal noise

※expressed with a simple model

- **Coating Brownian TN** [Harry, 2002]

$$S_x = \frac{4k_B T}{\Omega} \frac{(1 + \sigma)(1 - 2\sigma)2d_{coa}}{\pi Y w^2} \phi_c$$

Decreases with a larger beam size ( $w$ )

- **Suspension Brownian TN** [Saulson, 1990]

$$S_x = \frac{4k_B T}{m\Omega^5} \sqrt{\frac{4\pi Y g}{m}} \left( \frac{d_{wire}}{4\ell} \right)^2 \phi_w$$

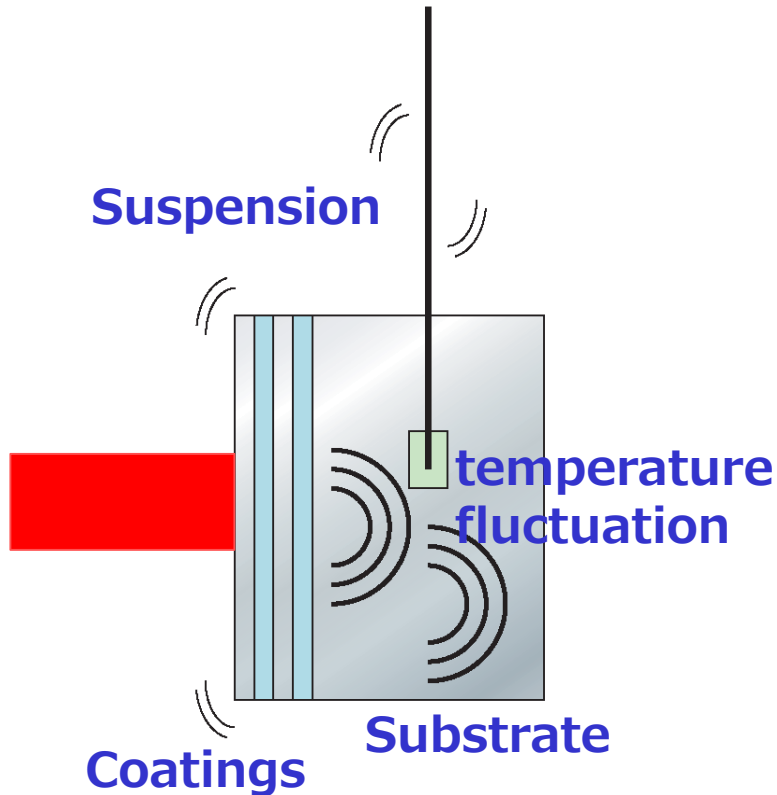
Decreases w/heavy mirror ( $m$ ) and thin wire ( $d$ )

- **Substrate thermoelastic noise**

[Braginsky, 2003]

$$S_x = \frac{16k_B T^2 (1 + \sigma)^2 \alpha_s^2 \kappa_s}{\sqrt{\pi C_s} w^3 \Omega^2}$$

Decreases w/low thermal expansion ( $\alpha$ ) <sup>21</sup>



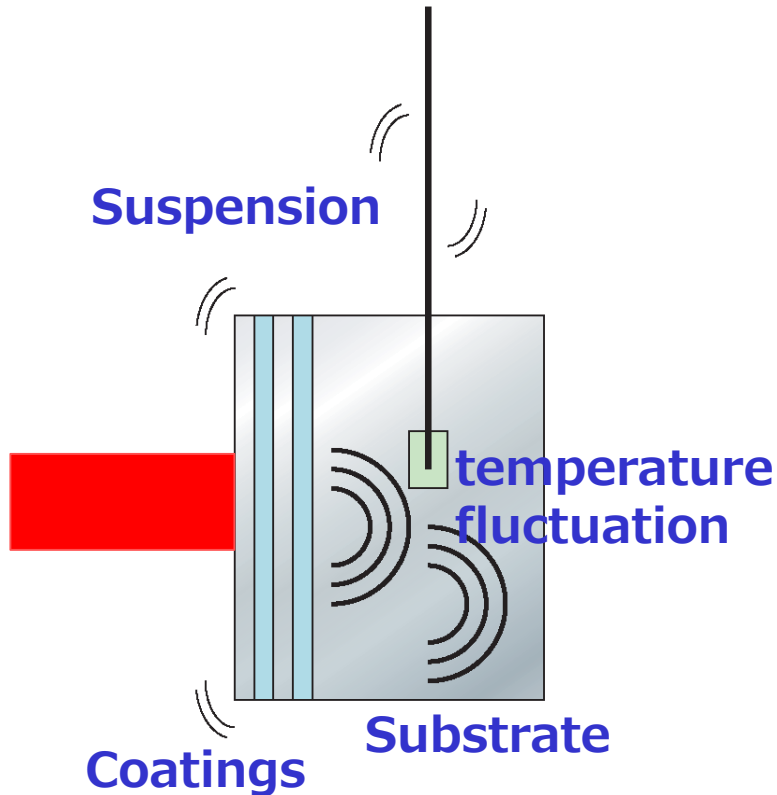
$Y$ : Young's modulus

$\sigma$ : Poisson ratio

$C_s$ : heat capacity

$\phi$ : loss angle

# Thermal noise



## LIGO's strategy

- Find a better coating material
- Increase the beam size
- Use thin monolythic wires
- Optimize the wire thickness

## KAGRA's strategy

- Cool the mirror down to 20K
- Use cryogenic sapphire wires

**Choice of the strategy to reduce TN makes the difference between LIGO and KAGRA.**

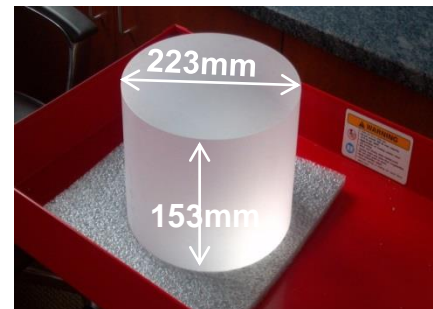
# Cryogenic system

- Radiation shields
- Heat transfer via heat links

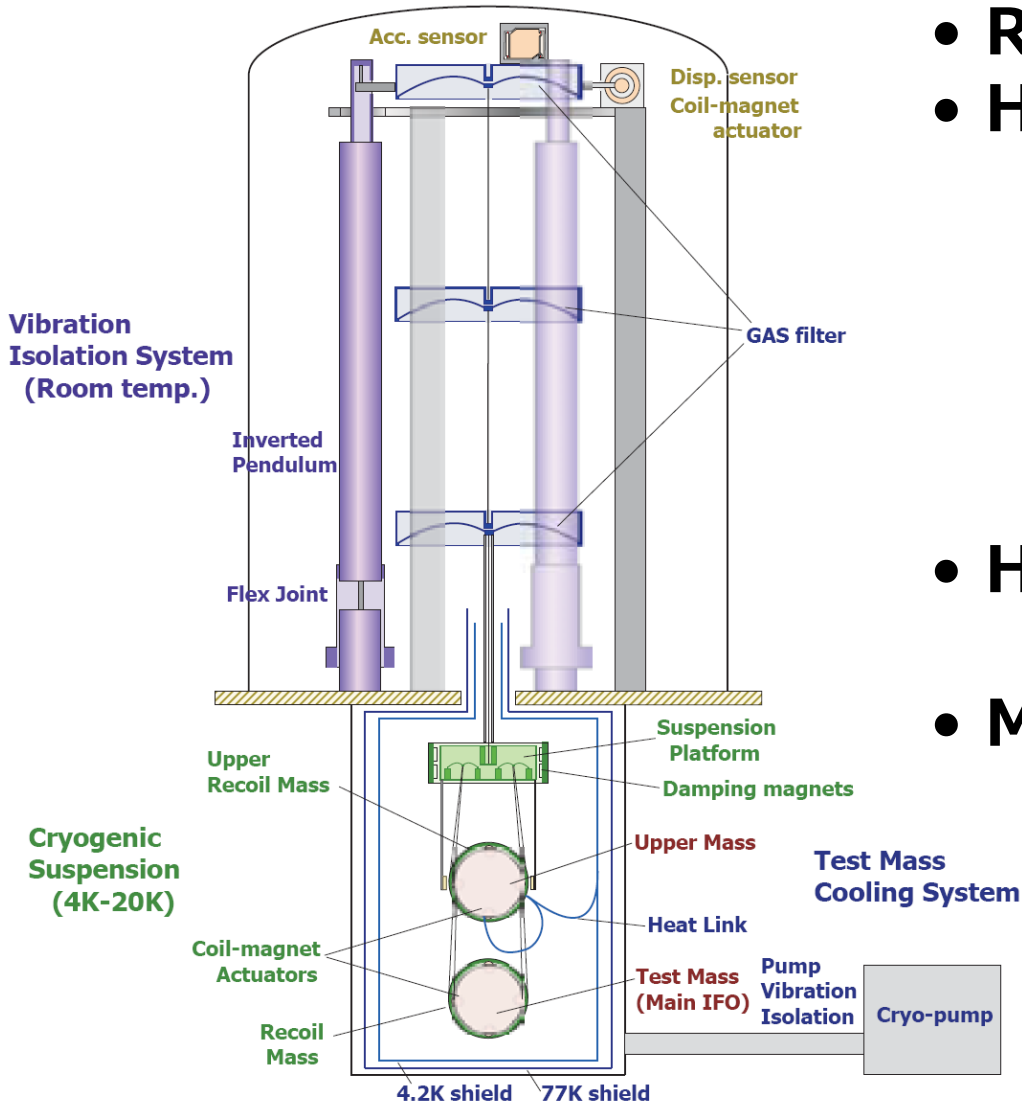


pure Al  
(99.999%)  
 $\phi=0.15\text{mm}$

- Heat transfer via sapphire wire  
 $\phi=1.6\text{mm}$
- Mirror temperature 20~23K



sapphire crystal  
 $m=23\text{kg}$ ,  $Q\sim 1e8$





# Contents of the talk

**1. Gravitational waves**

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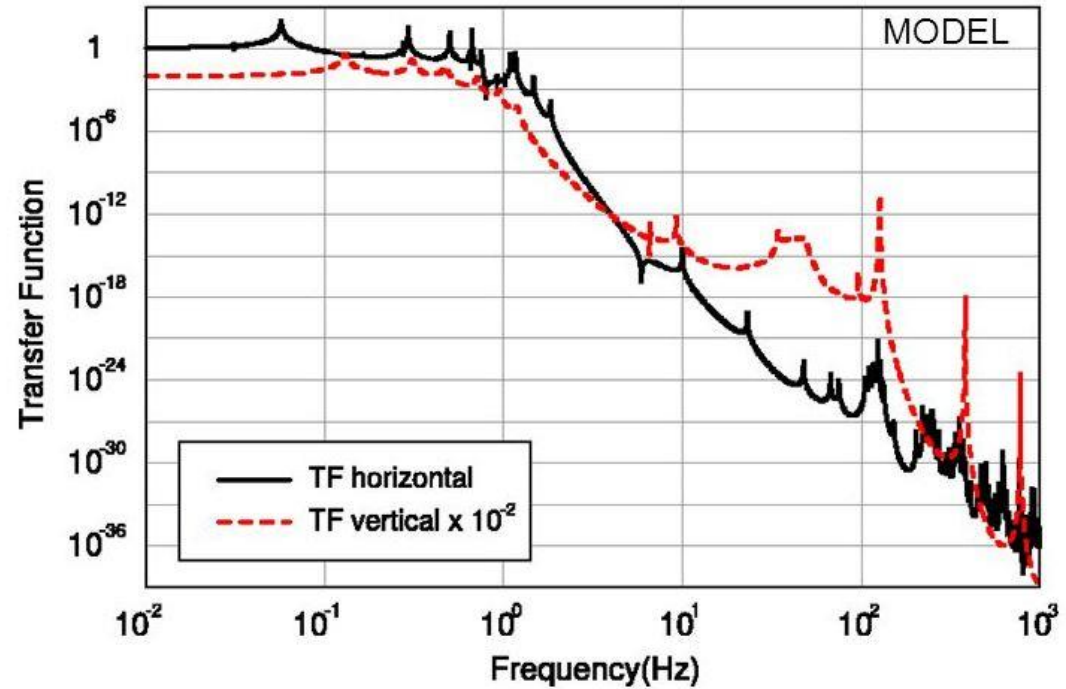
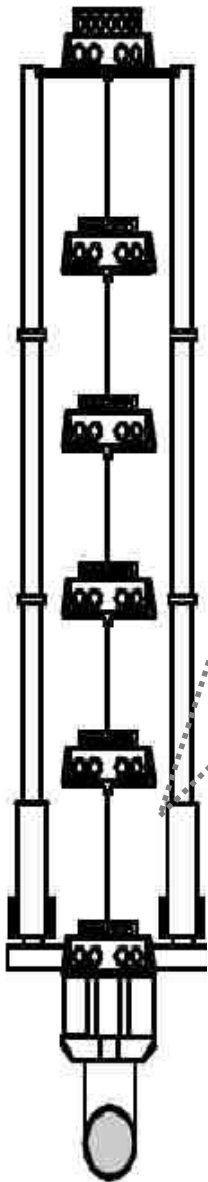
**2-3. Seismic+Newtonian noise**

**3. Toward the standard quantum limit**

**4. Summary**

# Multiple suspension in Virgo

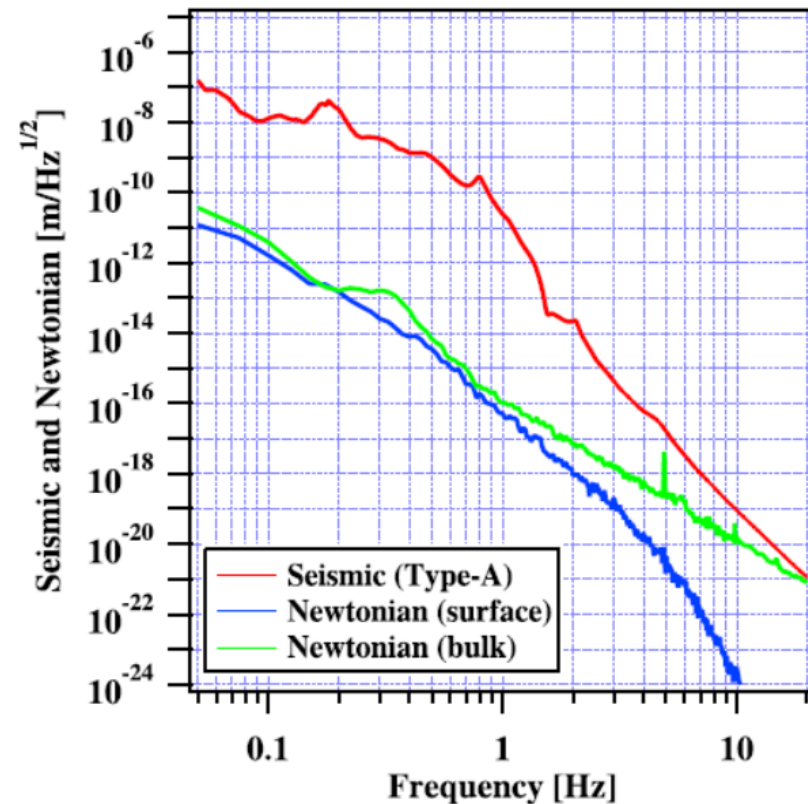
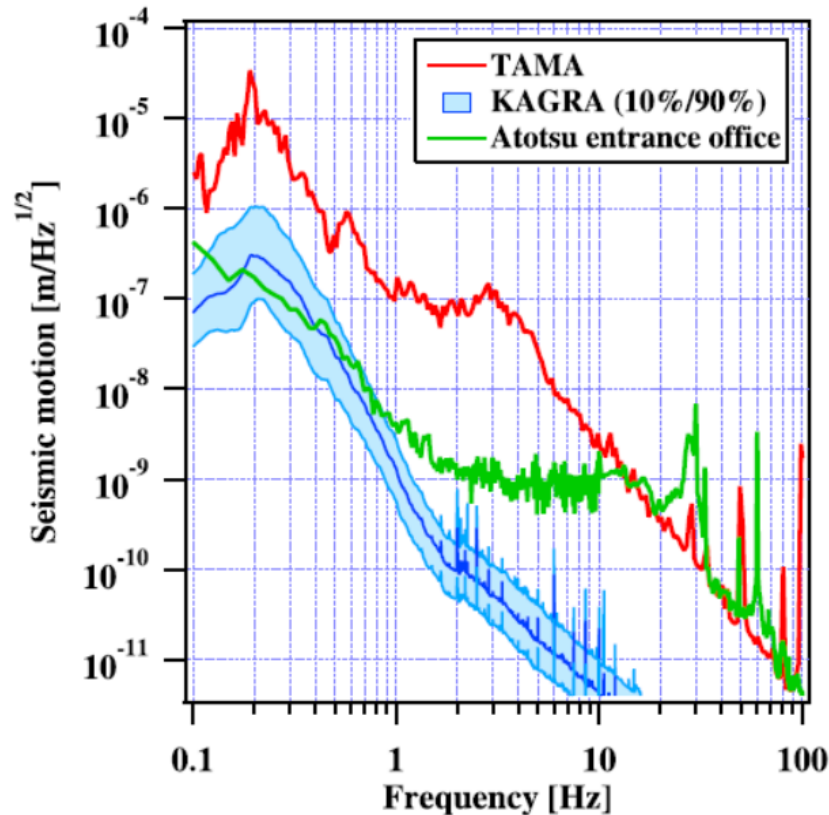
[Frasconi, APPEC Forum 2018]  
[Ballardin, RSI 2001]



**18 order seismic isolation at 100Hz**

# Underground

[KAGRA, PTEP 2020]



- Seismic noise at 1Hz is low at a quiet place.
- Seismic noise above 10Hz is low in the underground.
- Surface Newtonian noise is low in the underground.

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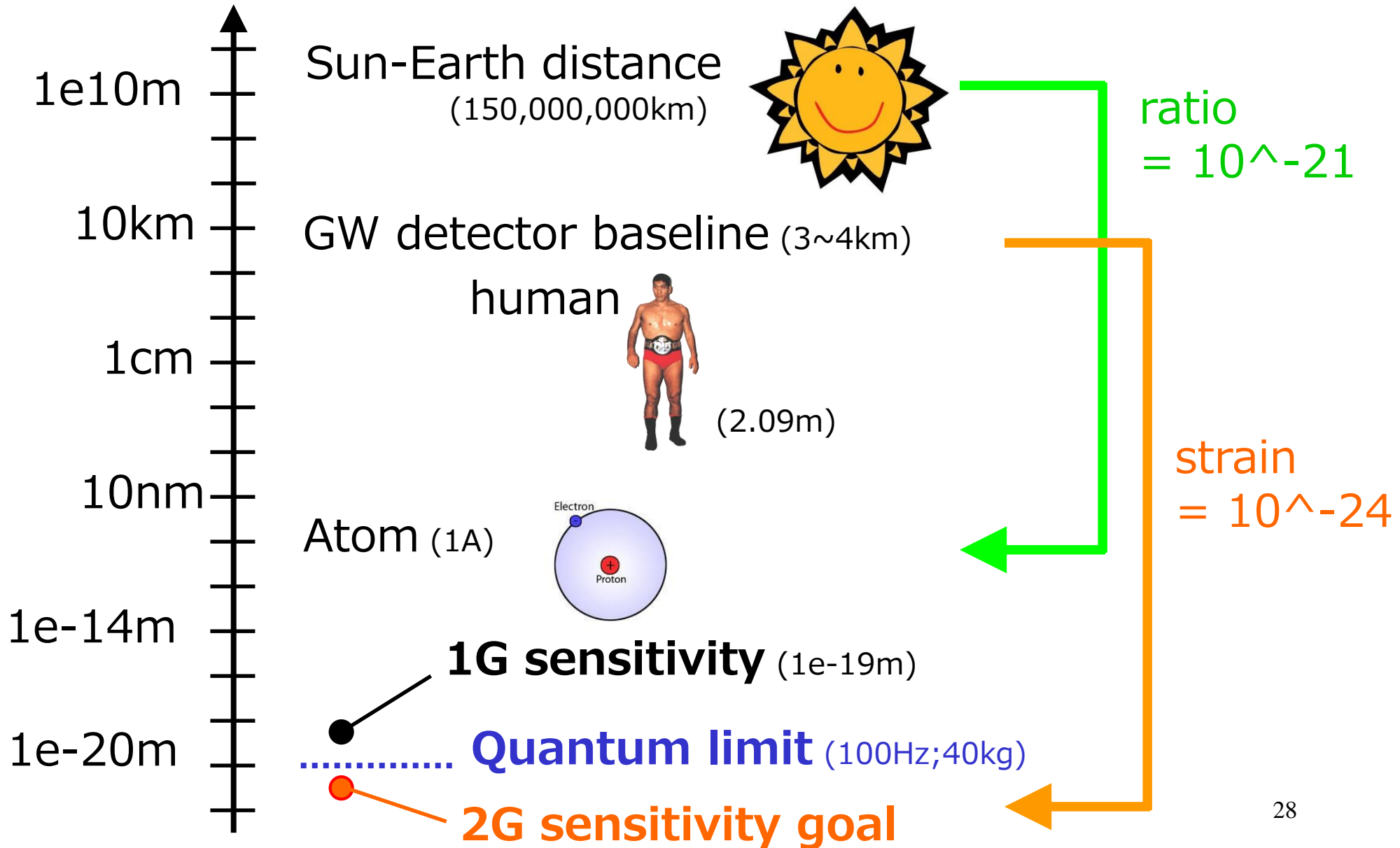
**2-2. Thermal noise**

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**3. Toward the standard quantum limit**

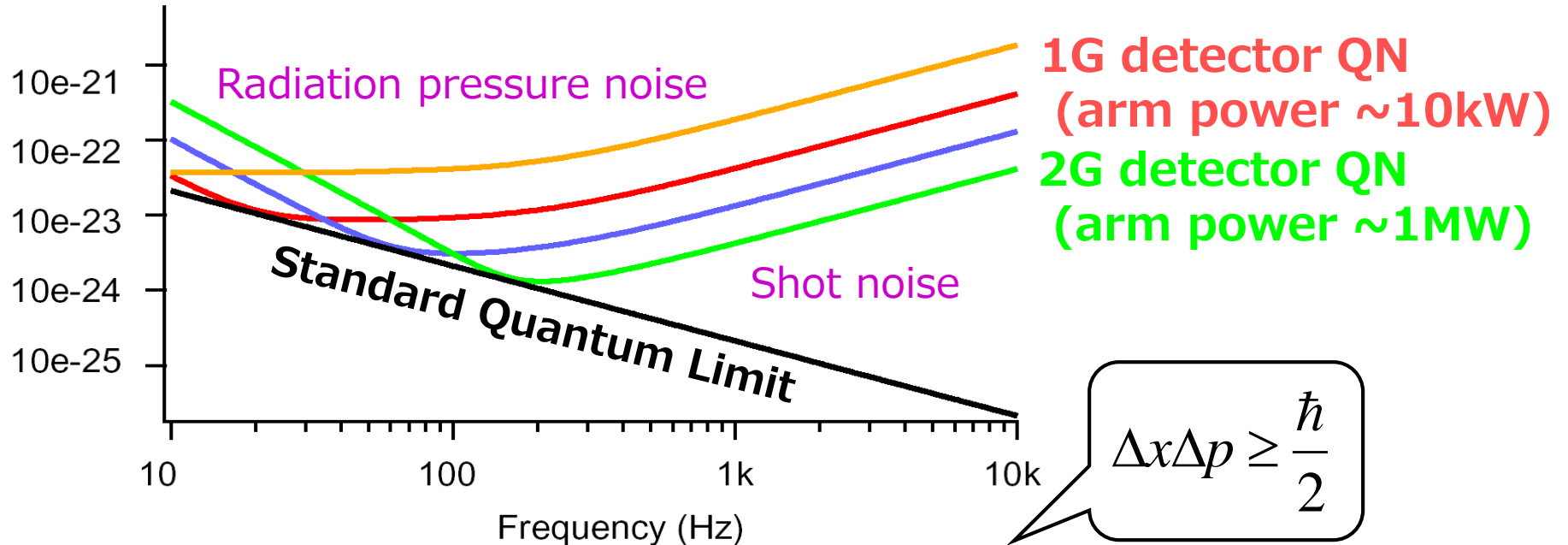
**4. Summary**

# How small are we going to measure?



# Quantum noise in GW detector

Noise Spectrum (1/rtHz)

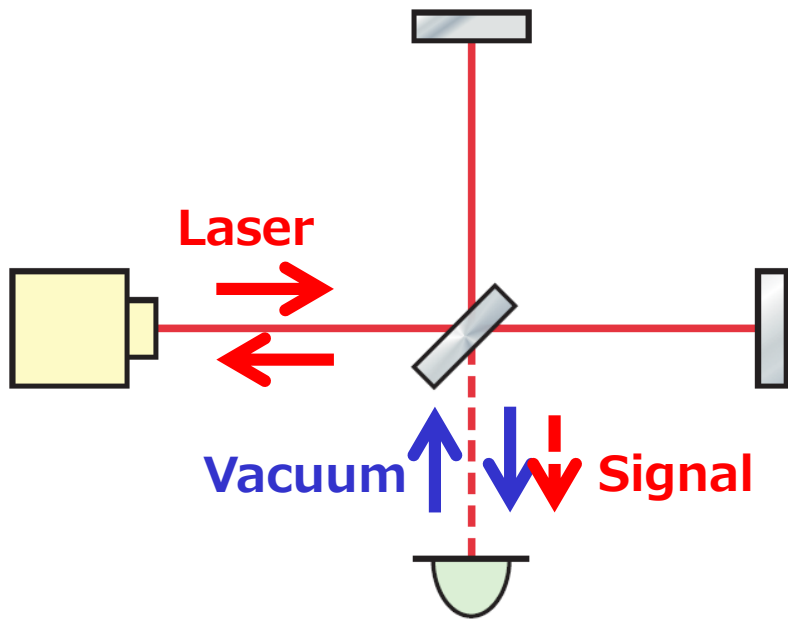


There is a limit that cannot be exceeded by simply increasing laser power.



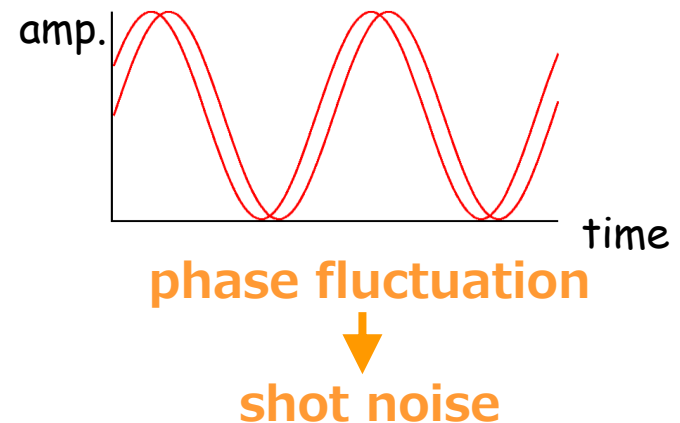
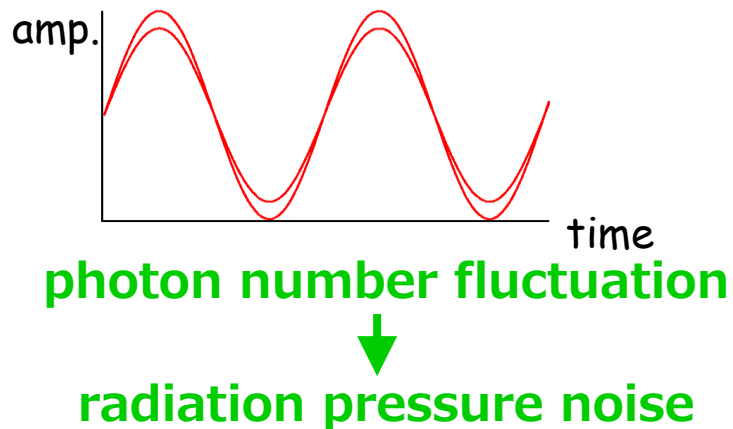
# Source of quantum noise

(SQL=Standard Quantum Limit)



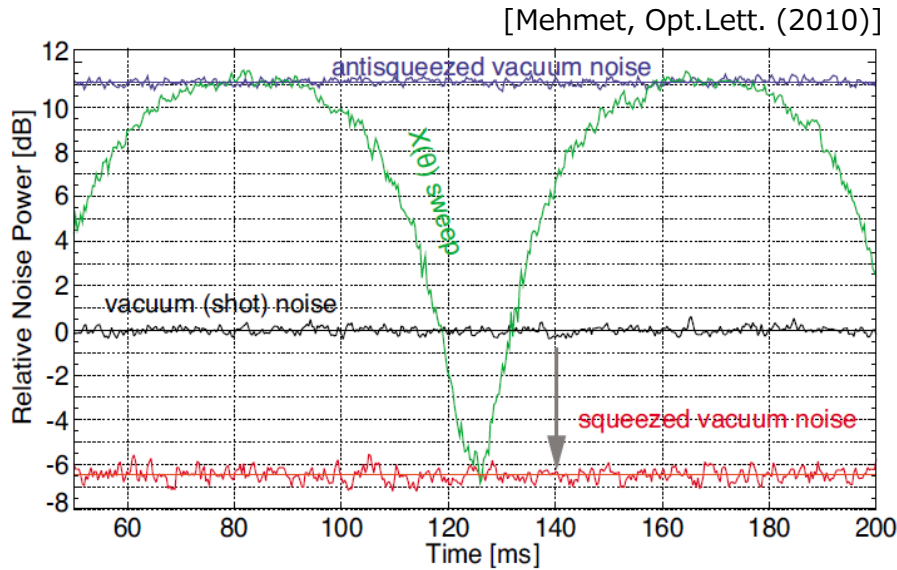
Vacuum field consists of amplitude and phase fluctuations.

SQL derives from a commutator of these two components.



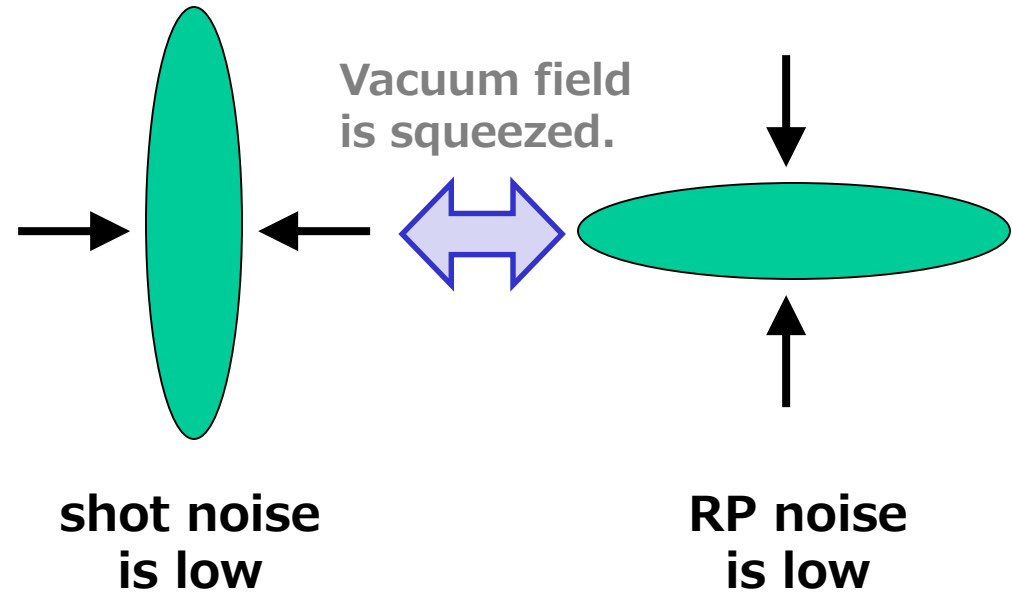
# Optical squeezing

(RP=Radiation Pressure  
LF=Low Frequency  
HF=High Frequency)



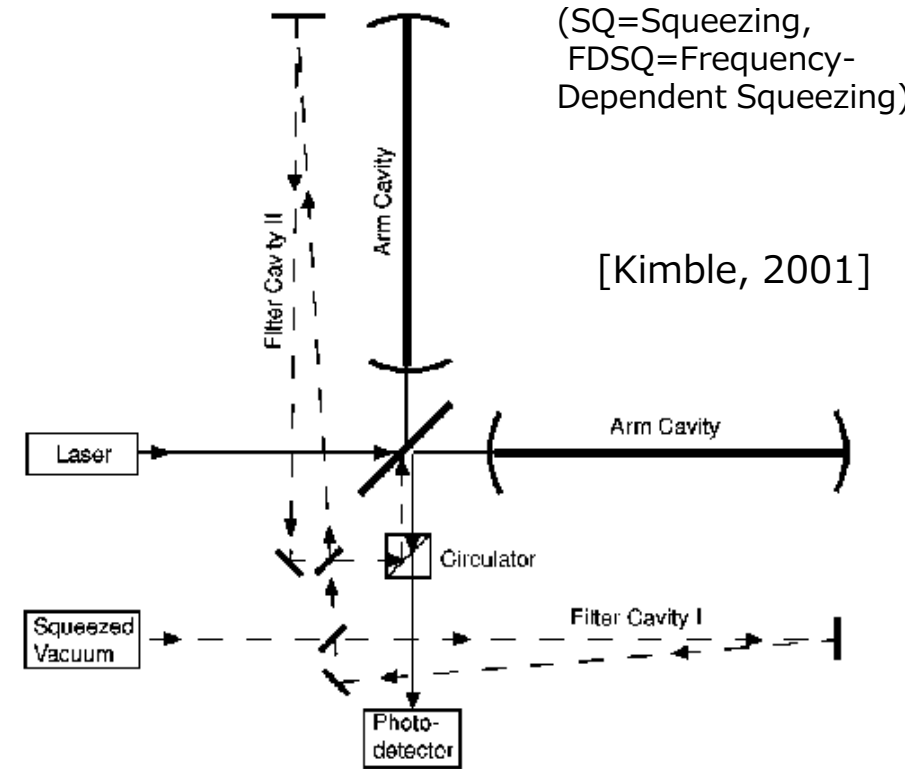
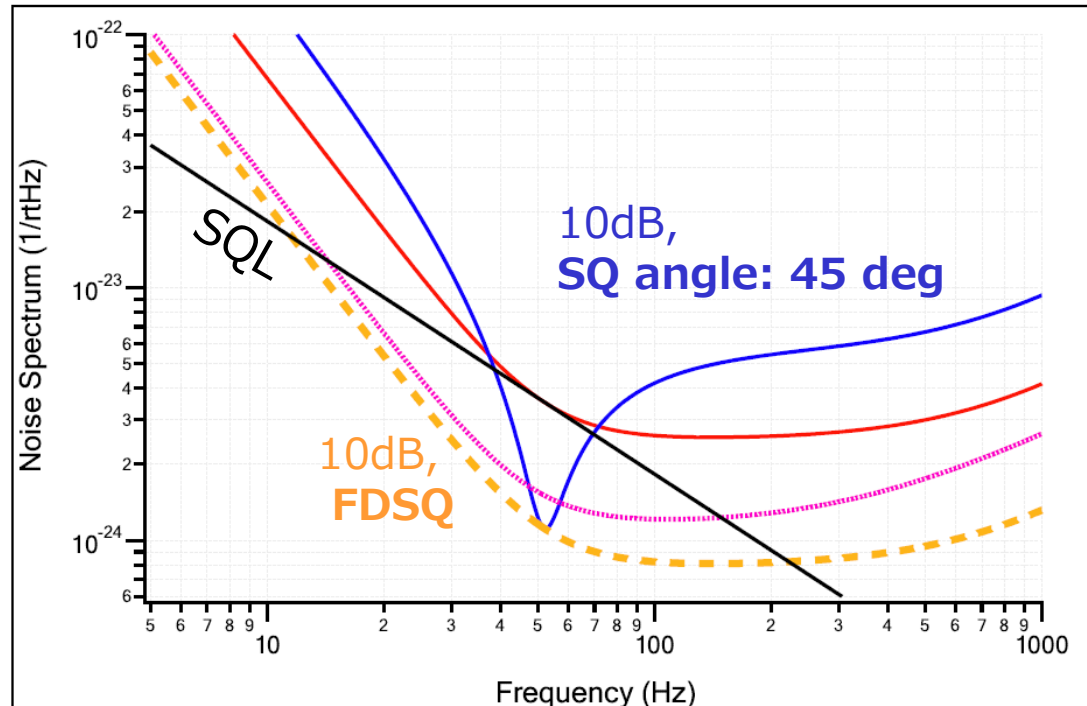
**7dB squeezing**

Optical parametric amplification process creates a correlation in upper and lower sidebands.



# Frequency-dependent squeezing

orange: lossless, pink: with loss

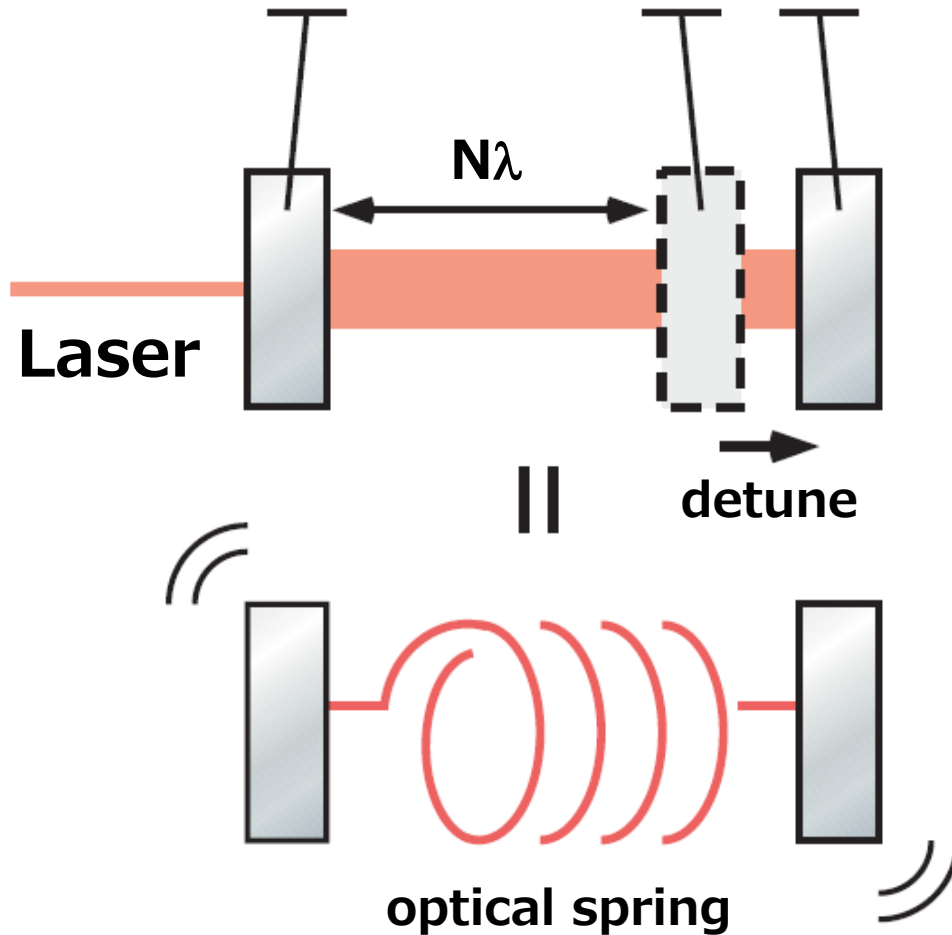


- SQ angle is rotated in filter cavities
- Rotation angle depends on the frequency

**This technique has been installed in LIGO & Virgo.**

# Optical spring

(RP=Radiation Pressure  
GW=Gravitational Wave  
OS=Optical Spring)



Far from reso  $\rightarrow$  less RP

Approach to reso  $\rightarrow$  more RP



Optomechanical restoring force

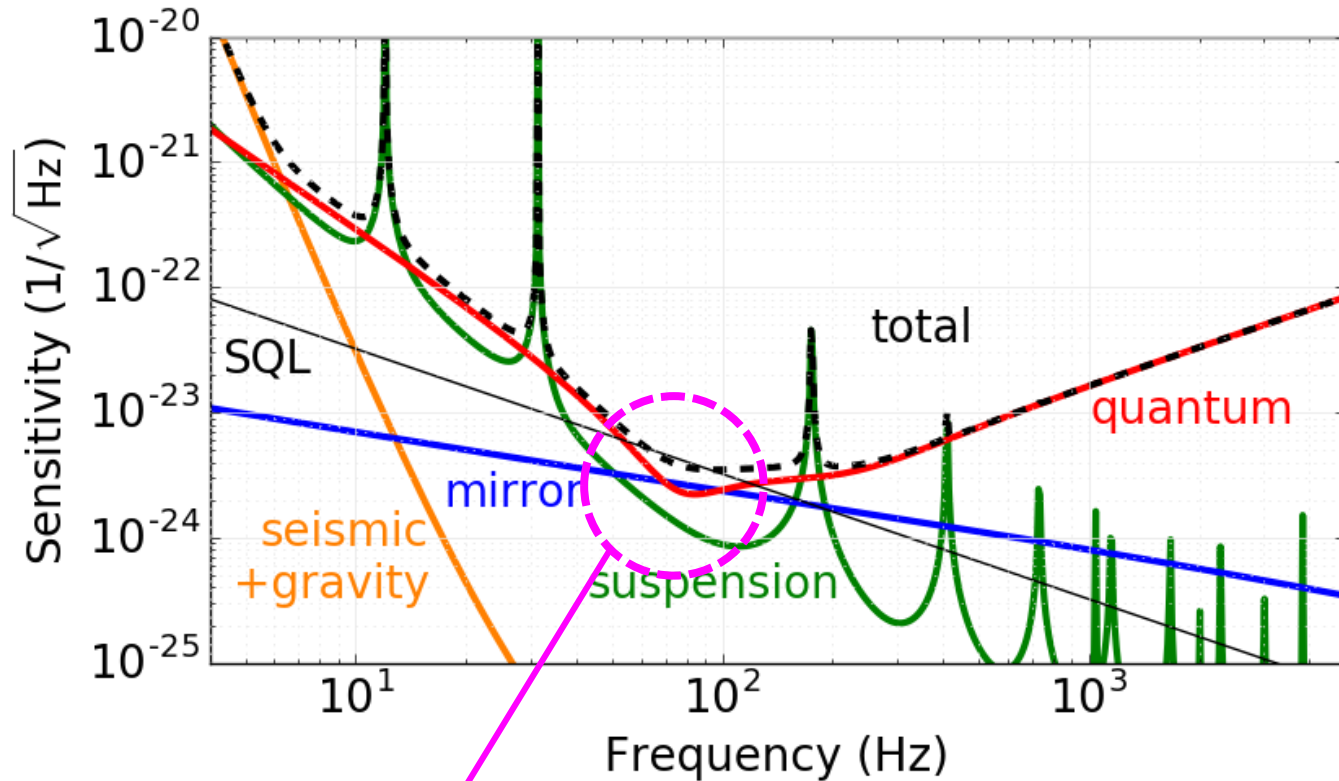
**GW response increases  
at OS resonance.**

**KAGRA plans to implement this technique.**

# Optical spring

(QN=Quantum Noise  
NS=Neutron Star  
SQL=Standard Quantum Limit  
HP=Home Page)

## KAGRA design sensitivity

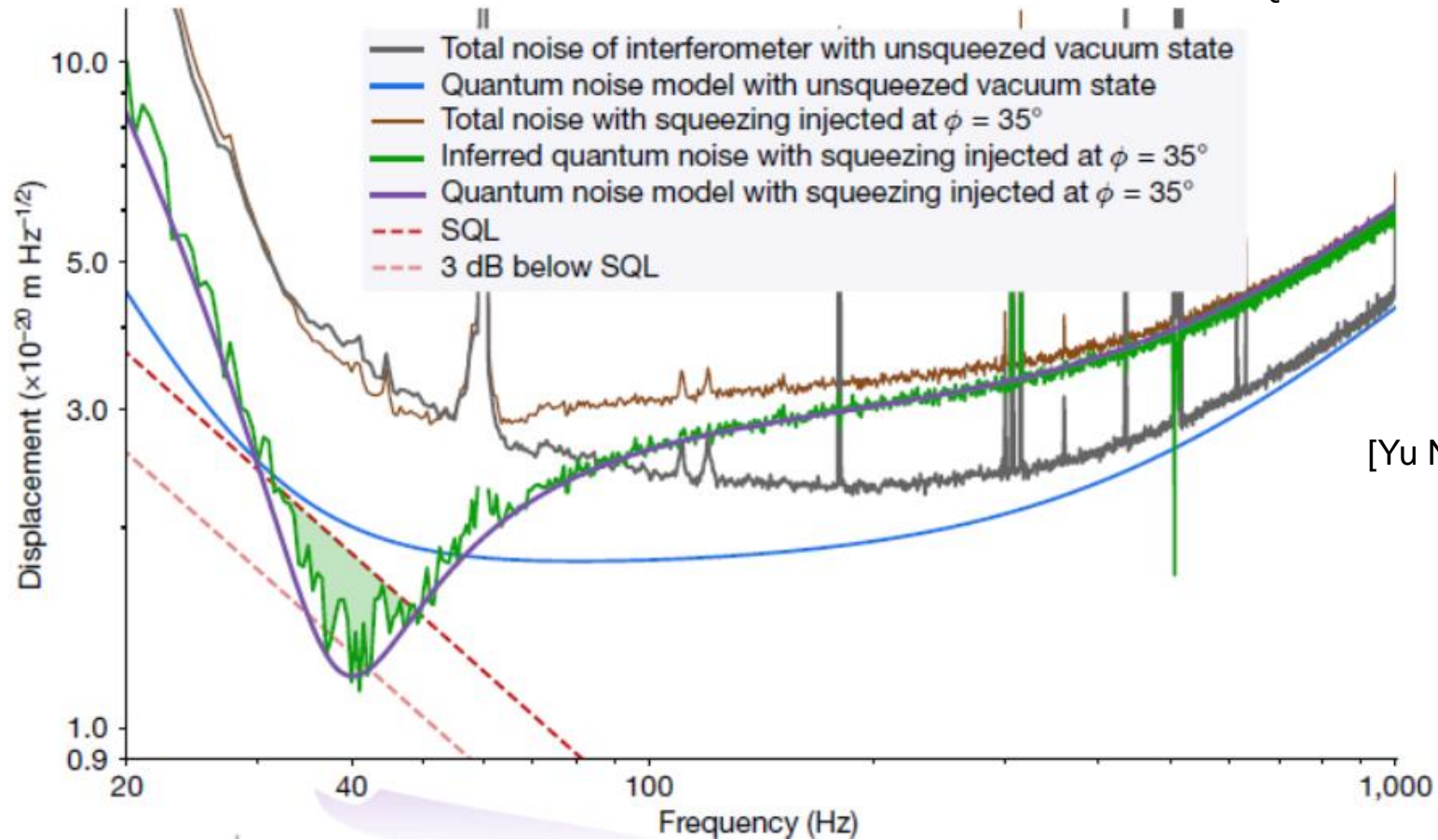


[KAGRA HP]

**QN exceeds the SQL at the optical spring frequency.  
⇒ 20% sensitivity improvement to observe binary NS.**

# Toward the SQL

(QN=Quantum Noise  
SQL=Standard Quantum Limit)

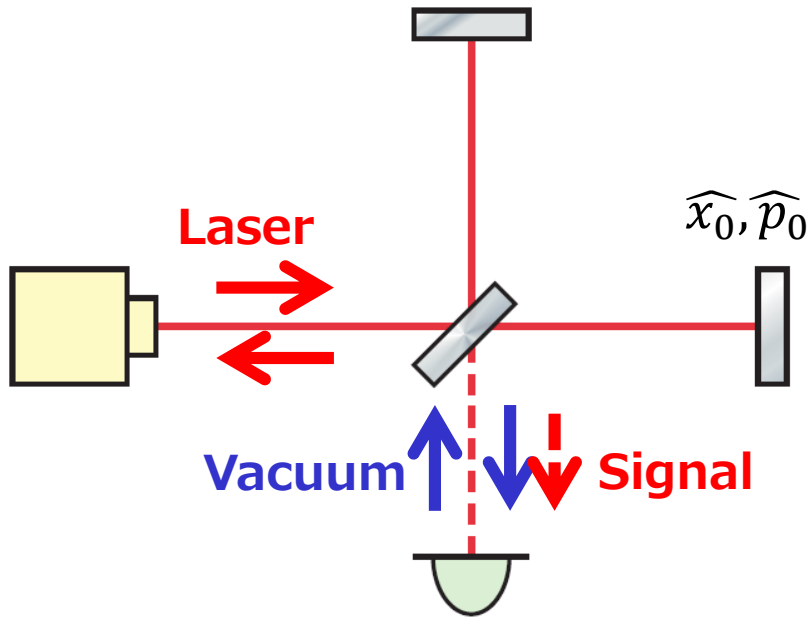


[Yu Nature 2020]

**LIGO demonstrated their QN exceeds the SQL by 3dB with a post-processing removal of classical noise.**



# How come the sensitivity can go beyond the SQL?



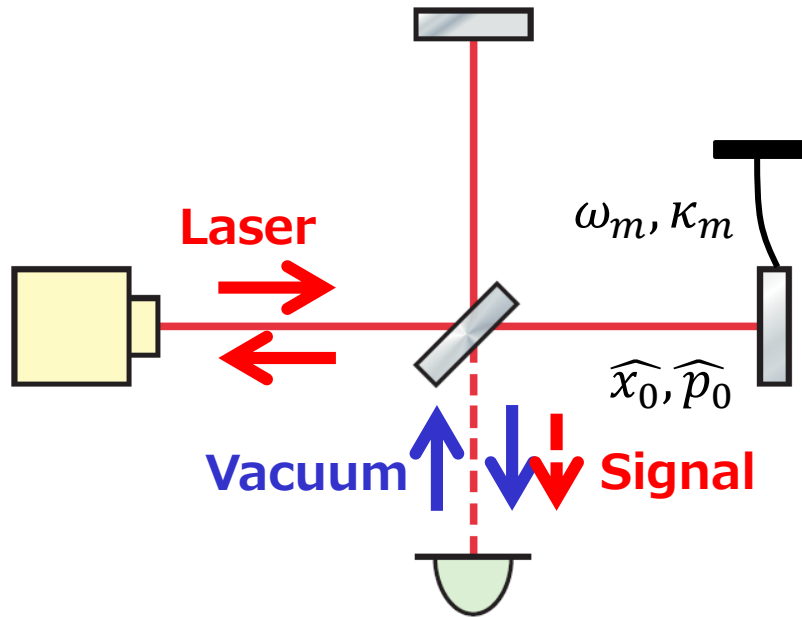
Brangisky's explanation in his paper, [PRD 67, 082001 (2003)] is as follows:

“GWD measures the external force on the mirror. Its initial position  $\hat{x}_0$  is not measured and remains quantum.”

The mirror fluctuates with back action noise but one can measure the external force without seeing the fluctuation of the test mass.

In other words, the output field  $y(t)$  commutes at different times:  $[y(t), y(t')] = 0$ .

# How come the sensitivity can go beyond the SQL?



Khalili's updated theory in his paper, [PRA 86, 033840 (2012)] is as follows:

"Oscillator's initial fluctuation  $\hat{x}_0 \cos \omega_m t$  dissipates in time and a thermal field enters. If T is low, the zero-point fluctuation of the thermal field takes over the initial quantum fluctuation."

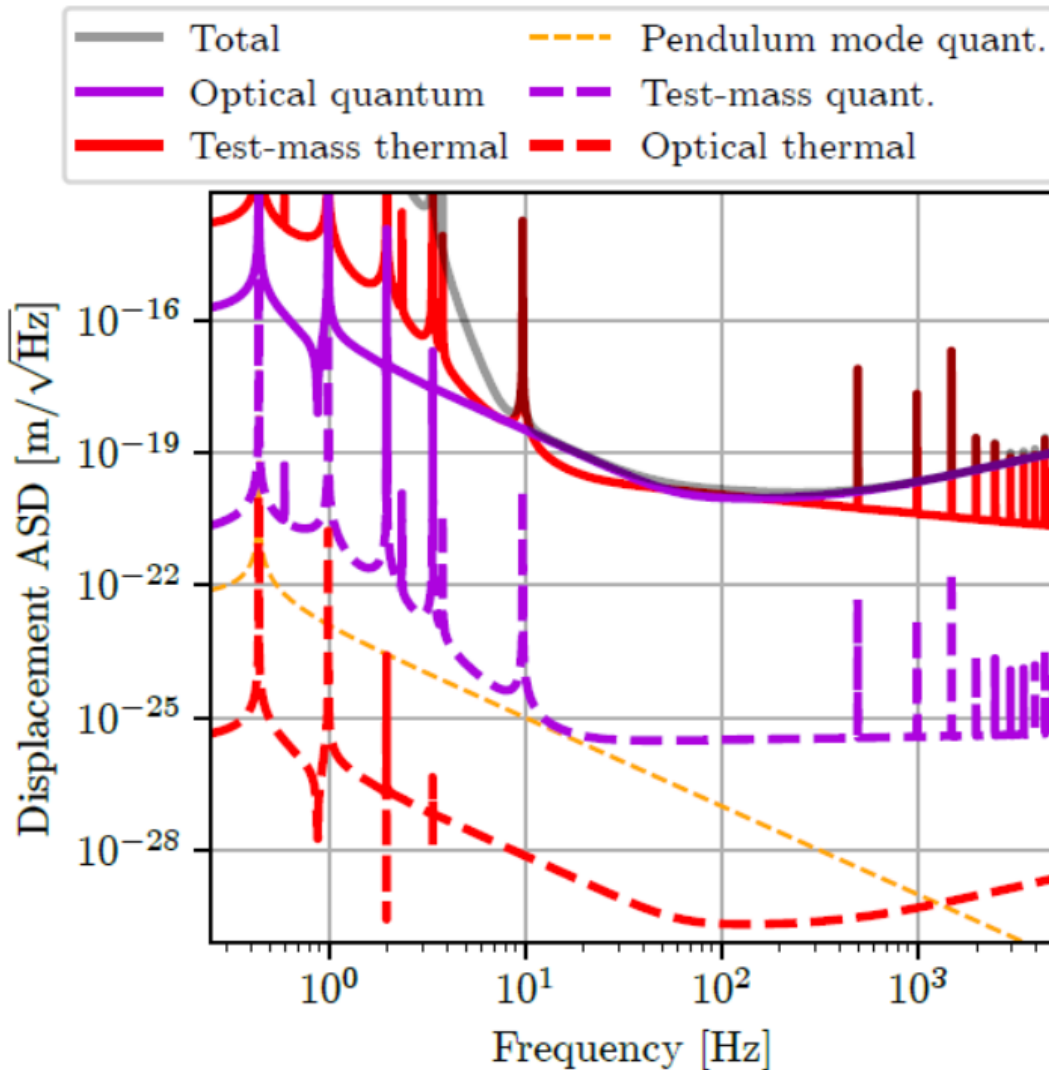
$$\hat{x}_q(t) = e^{-\frac{\kappa_m t}{2}} \left[ \hat{x}_0 \cos \omega_m t + \frac{\hat{p}_0}{m \omega_m} \sin \omega_m t \right] + \int_{-\infty}^t e^{-\frac{\kappa_m(t-t')}{2}} \frac{\sin \omega_m(t-t')}{m \omega_m} F(t') dt'$$

$$\hat{y}(t) = \underbrace{\hat{z}(t)}_{\text{shot noise}} + \underbrace{\hat{x}_{BA}(t)}_{\text{RPN}} + \underbrace{\hat{x}_q(t)}_{\text{initial position}}$$

Either  $z + x_{BA}$  or  $x_q$  does not commute at different times, but commutators cancel and  $y$  does commute at different times.

# Zero-point fluctuation in GWD

[Whittle, arXiv 2023]



**Whittle et al. demonstrated to calculate test mass quantum fluctuation in Advanced LIGO, which is very low compared with quantum noise of light.**

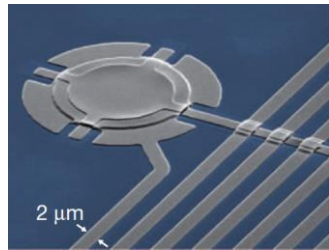
(dashed curves)

orange: pendulum mode only

purple: all mechanical modes

red: thermal fluctuation of photons

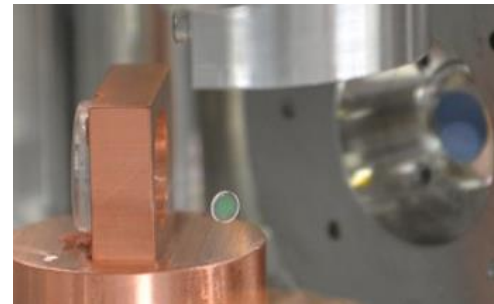
# Macroscopic QM on various mass scales



48pg membrane



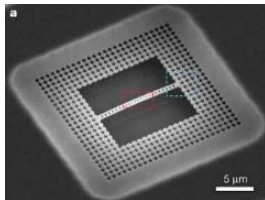
50ng cantilever



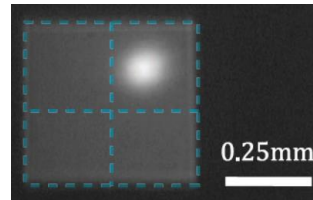
7mg pendulum



LIGO 40kg mass



331fg nanobeam



7ng membrane

Planck mass  
( $\sim 22\mu\text{g}$ )



1g pendulum

fg

pg

ng

$\mu\text{g}$

mg

g

kg

Some microresonators have reached the SQL (not the zero-point fluctuation). None above the Planck mass has reached the SQL.

## Reference

331fg nanobeam [Chan, Nature (2011)], 48pg membrane [Teufel, Nature (2011)], 7ng membrane [Peterson, PRL (2016)], 50ng cantilever [Cripe, Nature (2019)], 7mg pendulum [Matsumoto, PRL (2019)], 1g pendulum [Neben, NJP (2012)]

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# Summary

(SQL=Standard Quantum Limit  
GW=Gravitational Wave  
QM=Quantum Measurement)

- **Quantum noise in GW detector consists of quantum fluctuation of light.**
- **SQL can be surpassed in several ways; (i) squeezing, and (ii) optical spring.**
- **Sensitivity of GW detector is quite close to exceed the SQL.**
- **Test mass quantum noise is a few orders below the quantum noise of light.**
- **Macroscopic QM experiments are going on in various mass scale.**