



# **Thermal noise in KAGRA**

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@ Hida Hotel Plaza, Takayama, Gifu, Japan**

# *Contribution*

R. Takahashi, H. Tanaka, T. Miyamoto, K. Ono, T. Sekiguchi, Y. Sakakibara, C. Tokoku, M. Kamiizumi, U. Iwasaki, E. Hirose, A. Khalaidovski, R. Kumar, T. Uchiyama, S. Miyoki, M. Ohashi, K. Kuroda, T. Akutsu<sup>A</sup>, H. Ishizaki<sup>A</sup>, F. E. Peña Arellano<sup>A</sup>, T. Suzuki<sup>B</sup>, N. Kimura<sup>B</sup>, T. Tomaru<sup>B</sup>, S. Koike<sup>B</sup>, T. Kume<sup>B</sup>, K. Tsubono<sup>C</sup>, Y. Aso<sup>A</sup>, T. Ushiba<sup>C</sup>, K. Shibata<sup>C</sup>, D. Chen<sup>D</sup>, N. Ohmae<sup>E</sup>, K. Somiya<sup>F</sup>, R. DeSalvo<sup>G</sup>, E. Majorana<sup>H</sup>, L. Naticchioni<sup>H</sup>, W. Johnson<sup>I</sup>, A. Cumming<sup>J</sup>, R. Douglas<sup>J</sup>, K. Haughian<sup>J</sup>, I. Martin<sup>J</sup>, P. Murray<sup>J</sup>, G. Hammond<sup>J</sup>, S. Rowan<sup>J</sup>, G. Hofmann<sup>K</sup>, C. Schwarz<sup>K</sup>, D. Heinert<sup>K</sup>, R. Nawrodt<sup>K</sup>, S. Goto<sup>L</sup>, M. Tanaka<sup>L</sup>, S. Ioka<sup>M</sup>, K. Nakamoto<sup>M</sup>, H. Nezuka<sup>M</sup>, KAGRA collaboration

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# *0. Abstract*

I will explain **outline** of thermal noise of KAGRA  
(some kinds of **lecture or review**).

**Vivid and latest updates** are reported by **younger**  
people **later**.

R. Kumar's talk on Wednesday afternoon

A. Khalaidovski's and D. Chen's talk

on Tuesday morning, D. Chen's poster e-1(Thu)

# *0. Abstract*

I will explain **outline** of thermal noise of KAGRA (some kinds of **lecture or review**).

I will show some values to understand outlines, but it is based on calculation based on **simple assumption**.

If **younger** people shows slightly **different** values, please trust them not me.

# ***Contents***

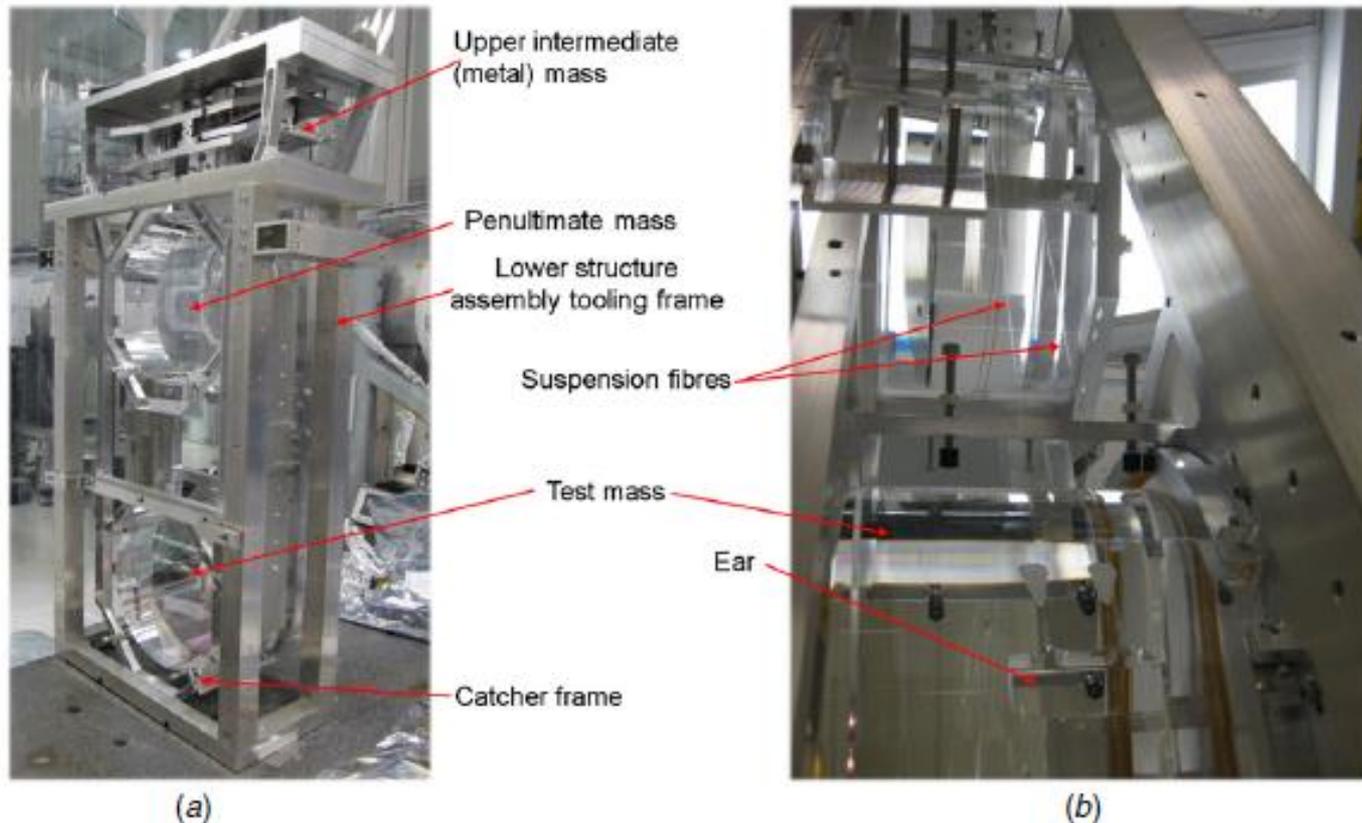
- 1. Introduction***
- 2. Mirror***
- 3. Suspension***
- 4. ELiTES***
- 5. Summary***

# 1. Introduction

Room temperature second generation interferometer  
**Fused silica** mirror suspended by **fused silica** fibers

Class. Quantum Grav. 29 (2012) 035003

A V Cumming *et al*



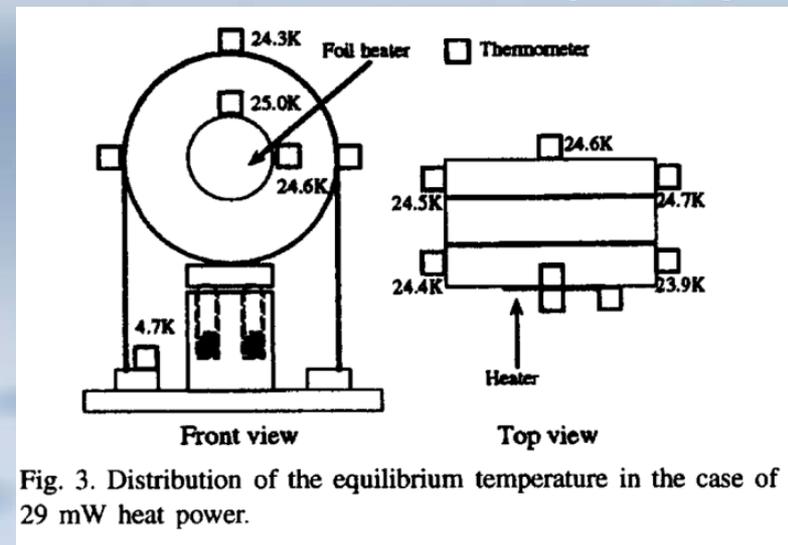
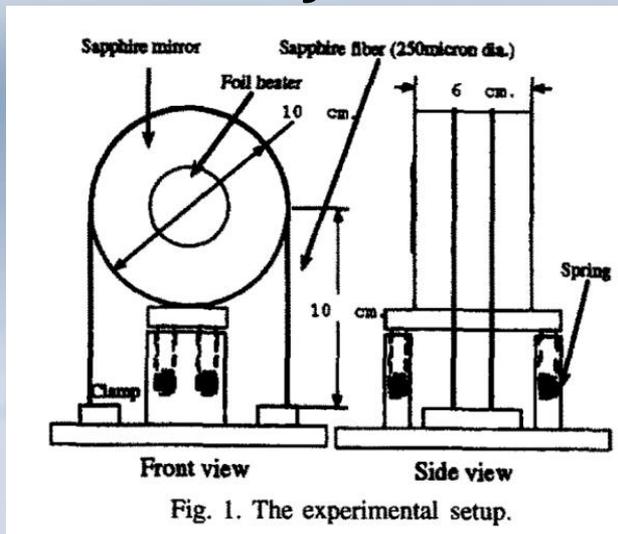
# 1. Introduction

KAGRA (Cryogenic second generation)

Sapphire mirror suspended by sapphire fibers

First feasibility study

T. Uchiyama *et al.*, Physics Letters A 242 (1998) 211.



Sapphire fiber : High Q-values  
and large thermal conductivity

# ***1. Introduction***

**Development of sapphire suspension**

**“Initial phase” (R. Kumar’s talk  
on Wednesday afternoon)**

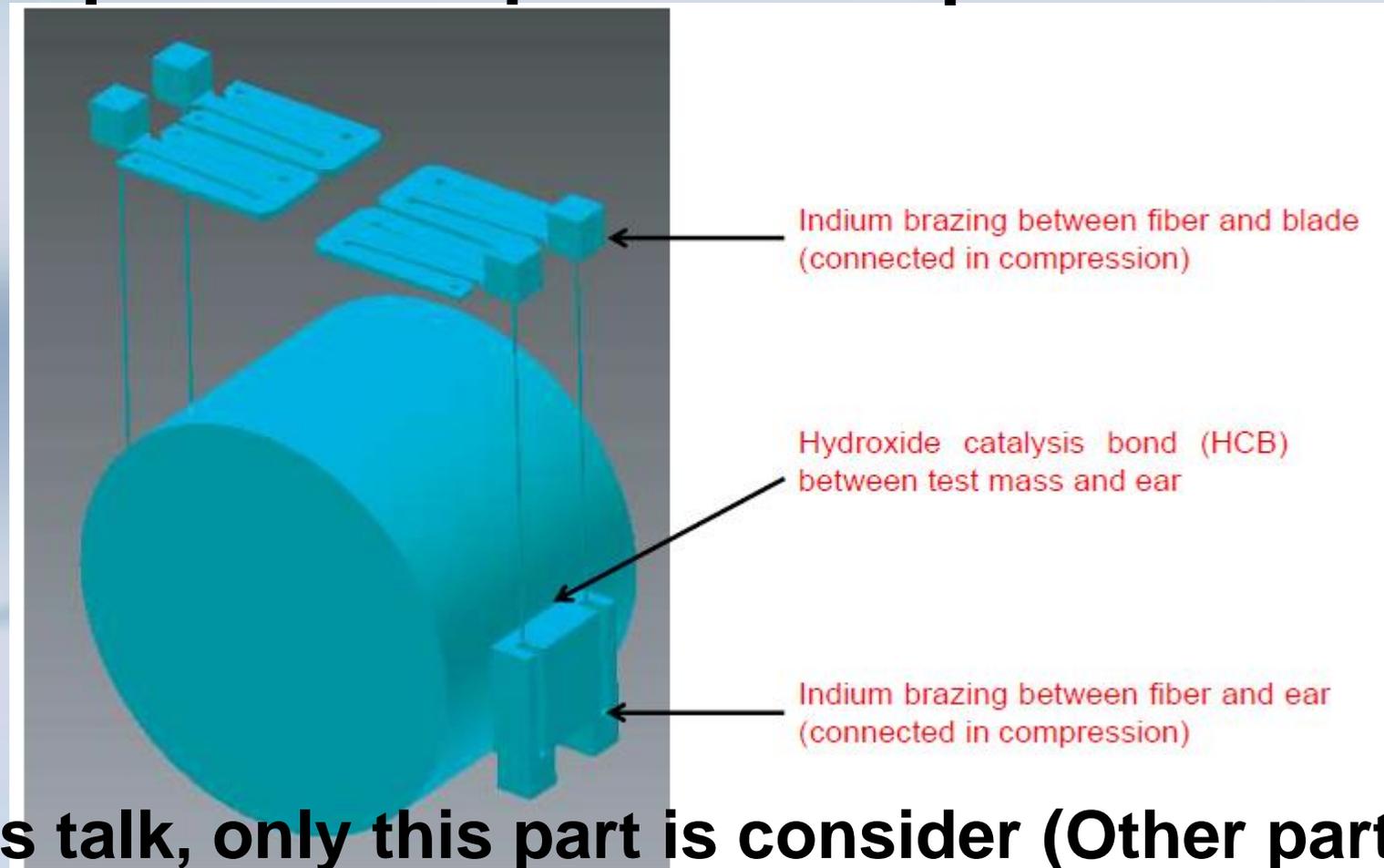
**Feasibility**

**“Final phase” (A. Khalaidovski’s and D. Chen’s talk  
on Tuesday morning,  
D. Chen’s poster e-1(Thu))**

**Small thermal noise**

# 1. Introduction

“Final phase” lop-eared suspension



In this talk, only this part is consider (Other parts of cryo payload are not discussed here).

## 2. Mirror

Mechanical dissipation generates thermal noise.

Loss in **substrate** and **coating**

Two kinds of loss : **Brownian**, **Thermoelastic**

**Substrate : Brownian noise**

(Unknown frequency independent)

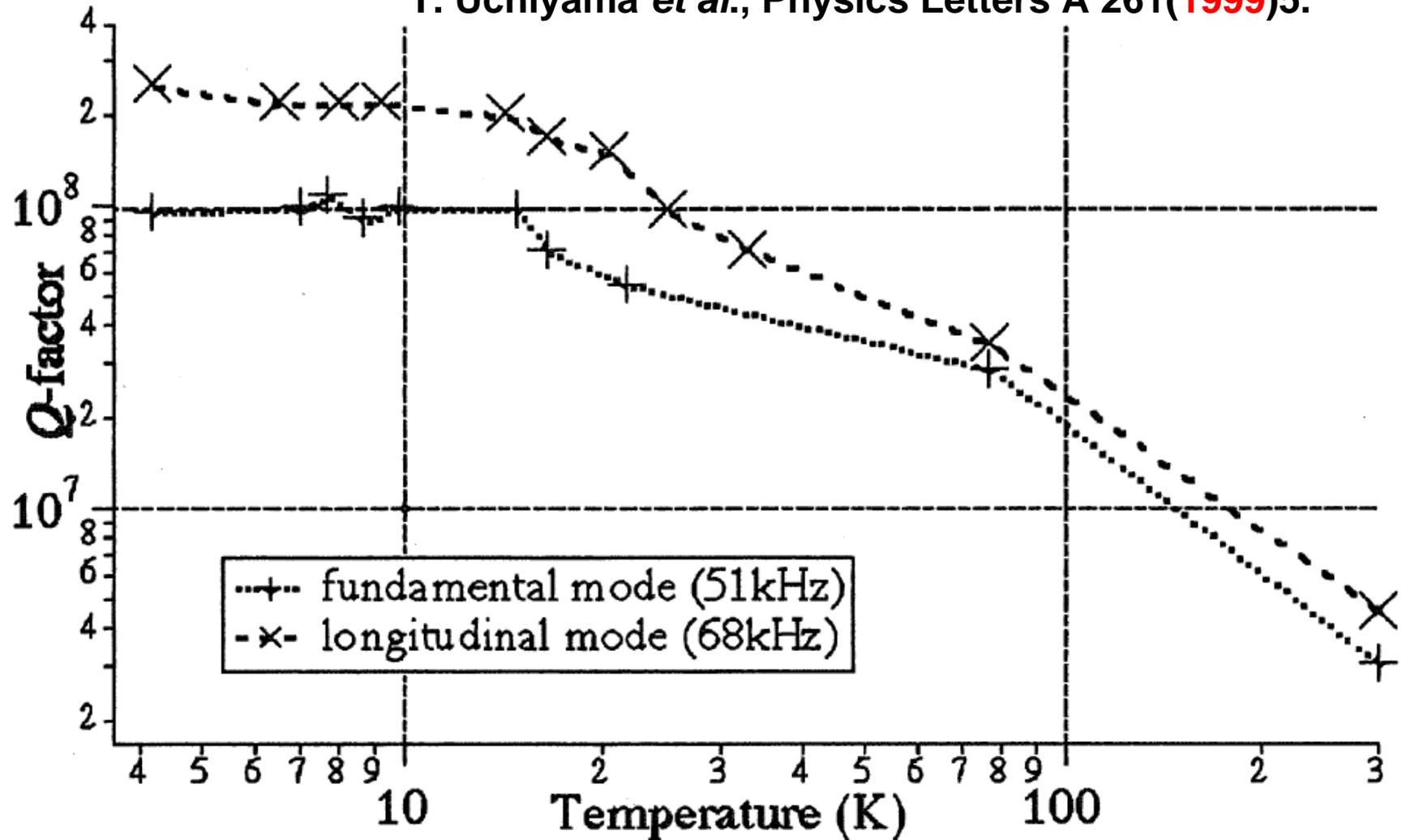
This noise is proportional to  **$1/Q^{1/2}$**  (substrate).

Sapphire **Q** is  **$10^8$**  at low temperature.

T. Uchiyama *et al.*, Physics Letters A 261(**1999**)5.

# 2. Mirror

T. Uchiyama *et al.*, Physics Letters A 261(1999)5.



## 2. Mirror

Mechanical dissipation generates thermal noise.

Loss in **substrate** and **coating**

Two kinds of loss : **Brownian, Thermoelastic**

**Substrate : Thermoelastic noise**

M. Cerdonio *et al.*, Phys. Rev. D 63 (2001) 082003.

**Temperature fluctuation**

and **thermal expansion** of substrate

Below 30 K :  **$T^{5/2}$**

Smaller thermal expansion

Phonon mean free path is

independent of temperature.

## 2. Mirror

Mechanical dissipation generates thermal noise.

Loss in **substrate** and **coating**

Two kinds of loss : **Brownian**, **Thermoelastic**

**Coating : Brownian noise**

Y. Levin, Phys. Rev. D 57 (1998) 659.

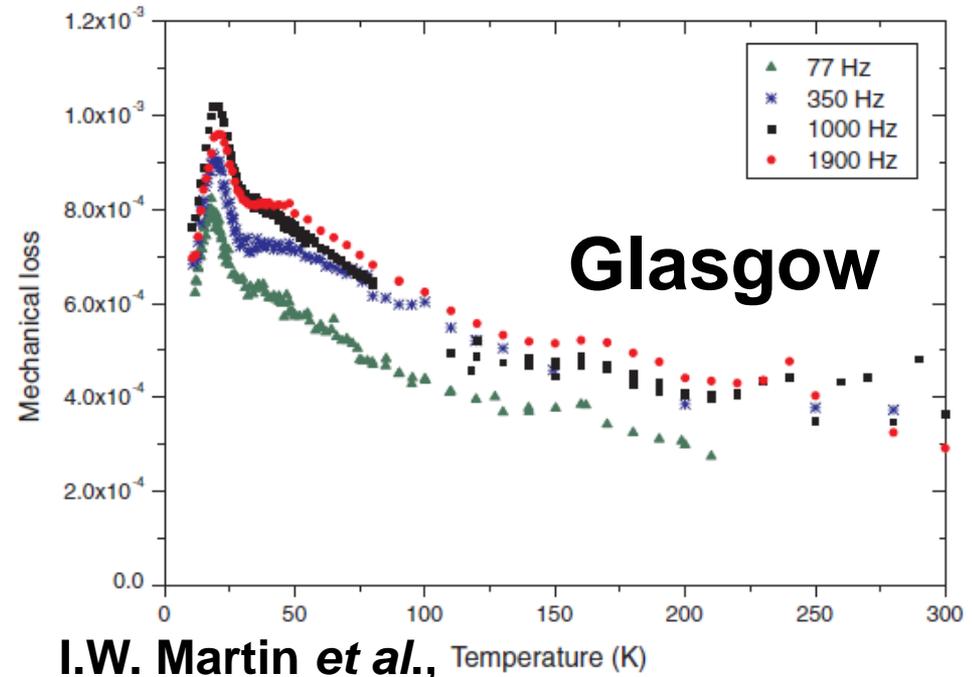
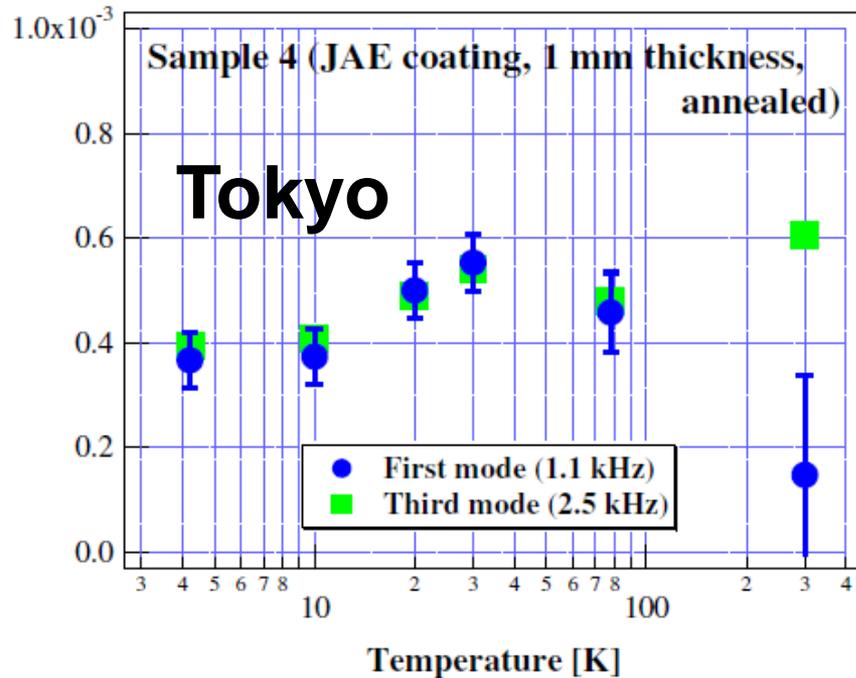
Coating has **large contribution** to thermal noise  
than we expected !

This noise is proportional to  $\phi^{1/2}$ .

# 2. Mirror

Coating : Brownian noise ( $Ta_2O_5/SiO_2$ )

**Discrepancy** between Tokyo and Glasgow



I.W. Martin *et al.*, Temperature (K)

Classical and Quantum Gravity

27 (2010) 225020.

(Annealing could suppress peak)

K. Yamamoto *et al.*,  
Physical Review D 74 (2006) 022002.

Collaboration (Tokyo and Glasgow) for this issue

E. Hirose's talk (Tuesday afternoon)

## 2. Mirror

Mechanical dissipation generates thermal noise.

Loss in **substrate** and **coating**

Two kinds of loss : **Brownian**, **Thermoelastic**

**Coating** : **Thermo-optic noise**

M. Evans *et al.*, Phys. Rev. D 78(2008)102003.

**Temperature fluctuation** and **thermal expansion** and  
**temperature coefficient of refractive index** of  
**coating**

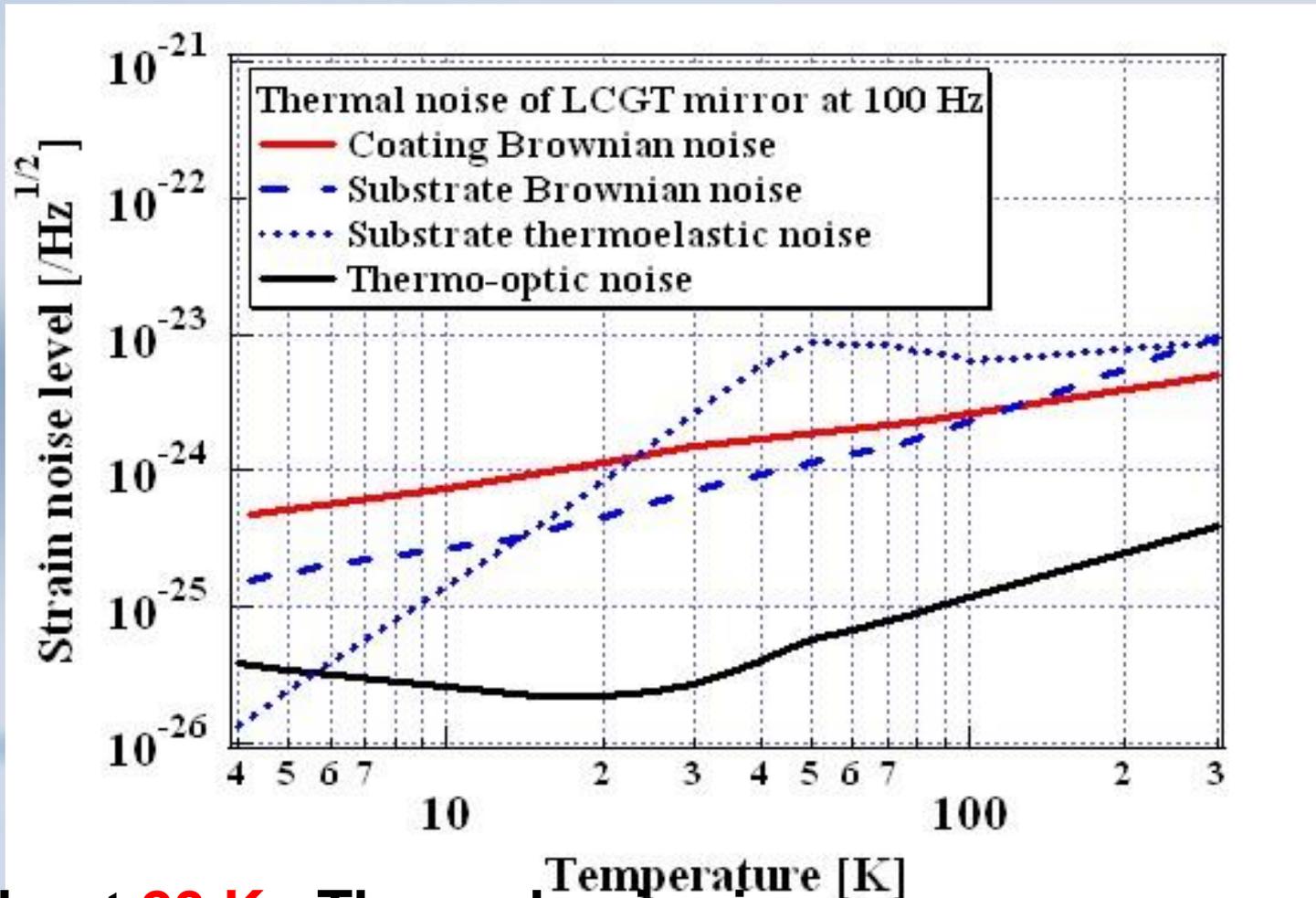
**Small** thermo-optic noise at **cryogenic temperature**

smaller temperature coefficient

longer phonon mean free path

# 2. Mirror

## Temperature of KAGRA mirror



Below about **20 K** : Thermal noise is

**sufficiently small for KAGRA ( $\sim 3 \times 10^{-24} / \text{rtHz}$ )**<sup>16</sup>

## ***2. Mirror***

**Other mechanical dissipation**

**Bonding (and so on ...)**

**Marielle van Veggel's talk (Monday afternoon)**

**Hydroxide Catalysis Bonding : Mirror and Ears**

**B. Douglas and Marielle van Veggel's poster (d-3, Thu)**

**Indium : Ears and Fibers (disassemble)**

**Dissipation which **far** from **reflective surface** has **small contribution** to thermal noise.**

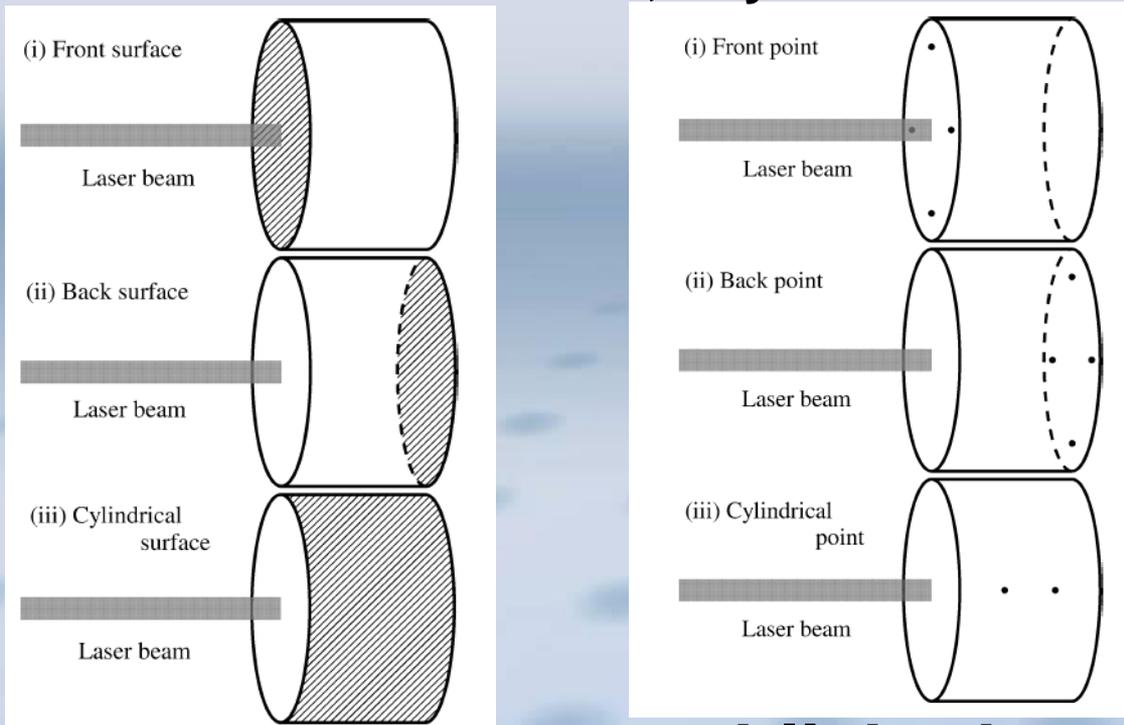
**Y. Levin, Phys. Rev. D 57 (1998) 659.**

# 2. Mirror

Other mechanical dissipation

**Finite element method** is necessary for evaluation.

First paper : K. Yamamoto *et al.*, Physics Letter A 305 (2002) 18.



So far, many papers were published

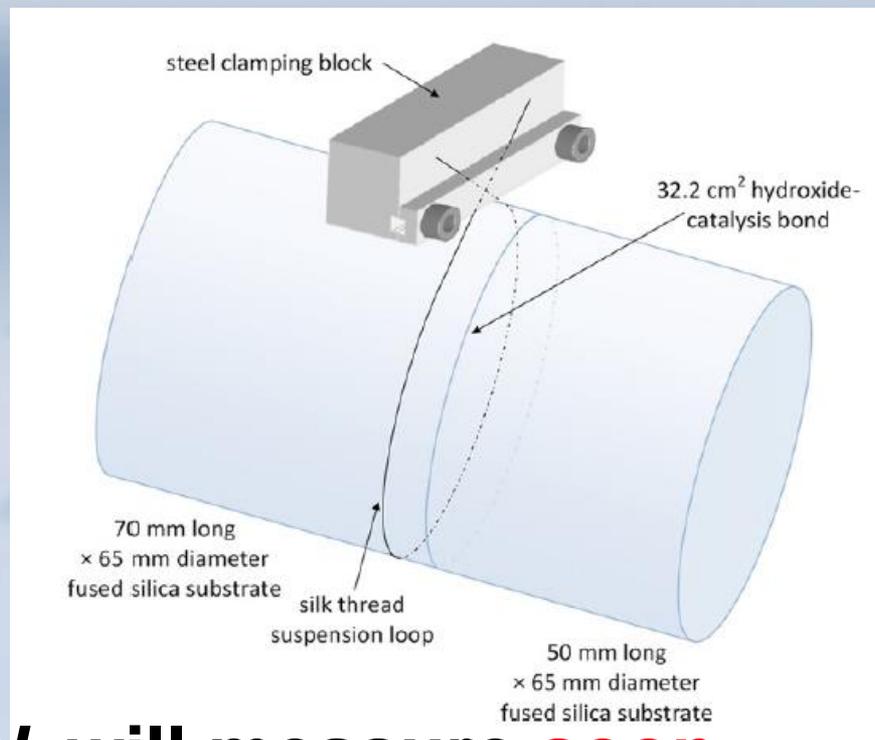
and this is a common method ...

# 2. Mirror

Other mechanical dissipation

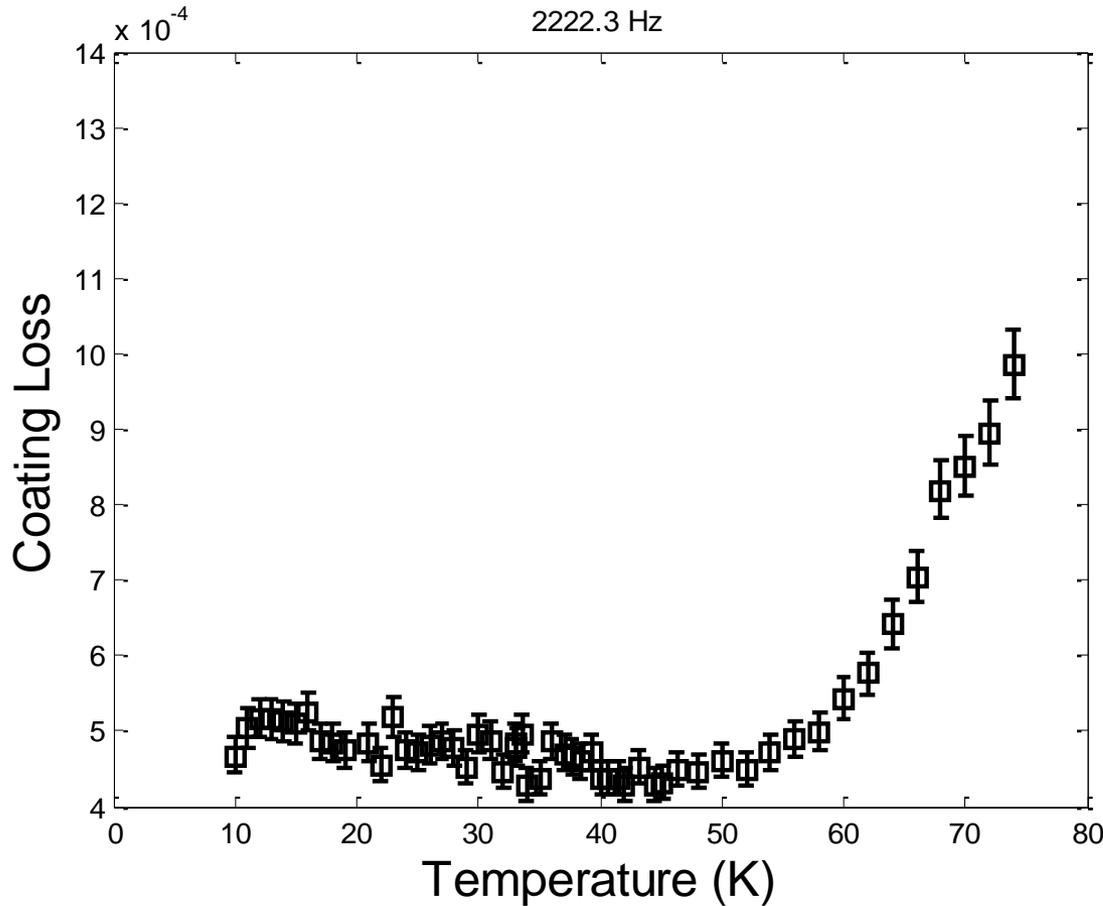
We have **plans** to **measure** mechanical dissipation  
(ELiTES, Jena and Glasgow).

L. Cunningham *et al.*, Physics Letters A 374(2010)3993.



D. Chen *et al.* will measure **soon**.

# Loss of indium film at cryogenic temperature



- Loss of approximately  $5 \times 10^{-4}$  at a few 10's of K
- Broadly consistent with values from Liu et al (1999)
- FEA models of thermal noise from indium bonds used in an Advanced detector-like suspension geometry at 40K suggest noise would be  $\sim 10$  lower than sensitivity of ET.

Mode 4 at  $f = 2222$  Hz

# 3. *Suspension*

## Assumption

**Upper ends** of sapphire fibers are **fixed** rigidly.

(1) In this talk, we discuss only thermal noise from **final stage of payload, sapphire main mirror and its fibers.**

(2) **Resonant frequencies** (except for violin modes) are **different from the actual system.**

They are **not exact** results,  
but **not so different**  
from the actual contribution  
of the final stage.

# 3. *Suspension*

## Strength

Sapphire fibers should **support**  
**the weight** of sapphire mirror.

Mirror : 23 kg

Number of fibers : 4

Tensile strength : 400 MPa

Safety margin : 7

**Fiber diameter** must be larger than **1.1 mm**.

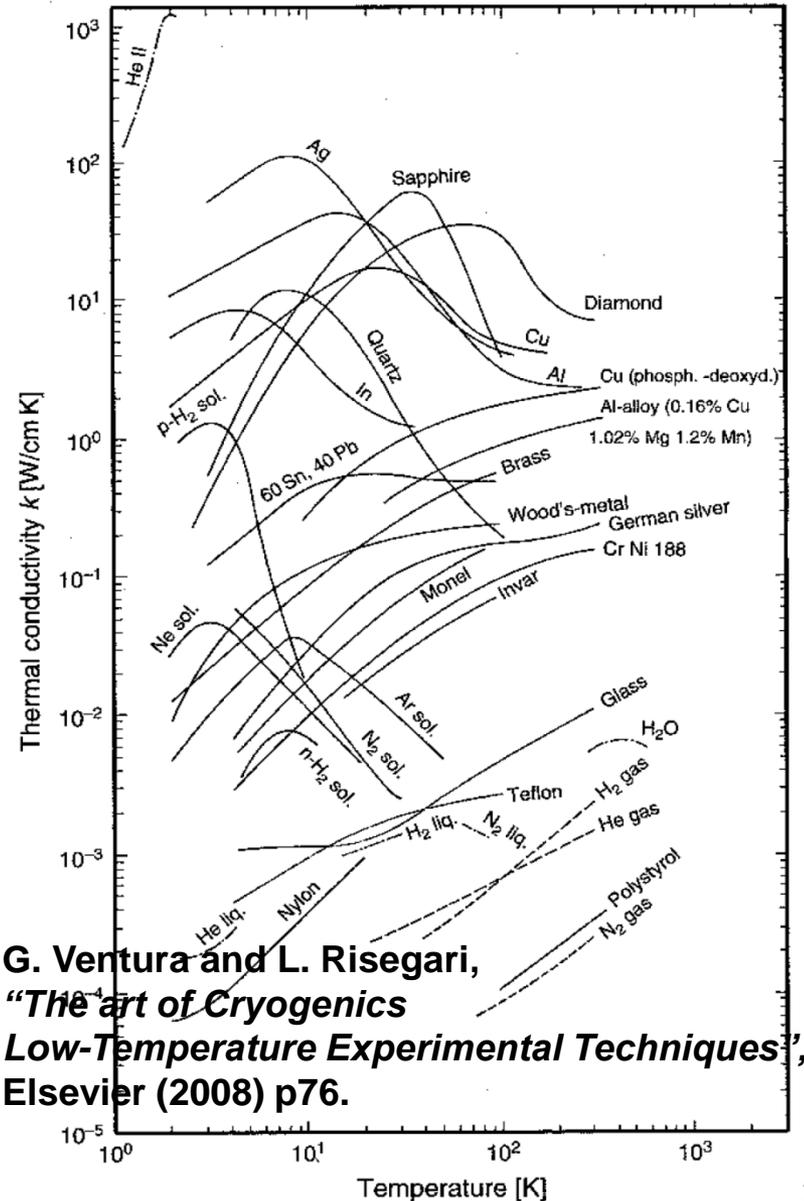
# 3. Suspension

Thermal conductivity

Fibers should **transfer heat**  
(about 1 W).

**Crystal** (for example, sapphire, silicon) and **pure metal** (Al, Cu, Ag) : Thermal conductivity is extremely high (**> 1000 W/m/K**) around 20 K.

Q-values of pure metal is low. **Crystals with high Q-values** are candidates (sapphire, silicon).



# 3. *Suspension*

## Thermal conductivity

Sapphire : Thermal conductivity is **maximum** around **30 K**.  
Temperature of **KAGRA mirror** will be around **20 K**.

## Specification sapphire suspension

Number of fibers : 4

Length of fibers : 0.3 m

Heat generated in a mirror : 1 W

Mirror temperature : 23 K

Temperature at top end of fiber : 16 K

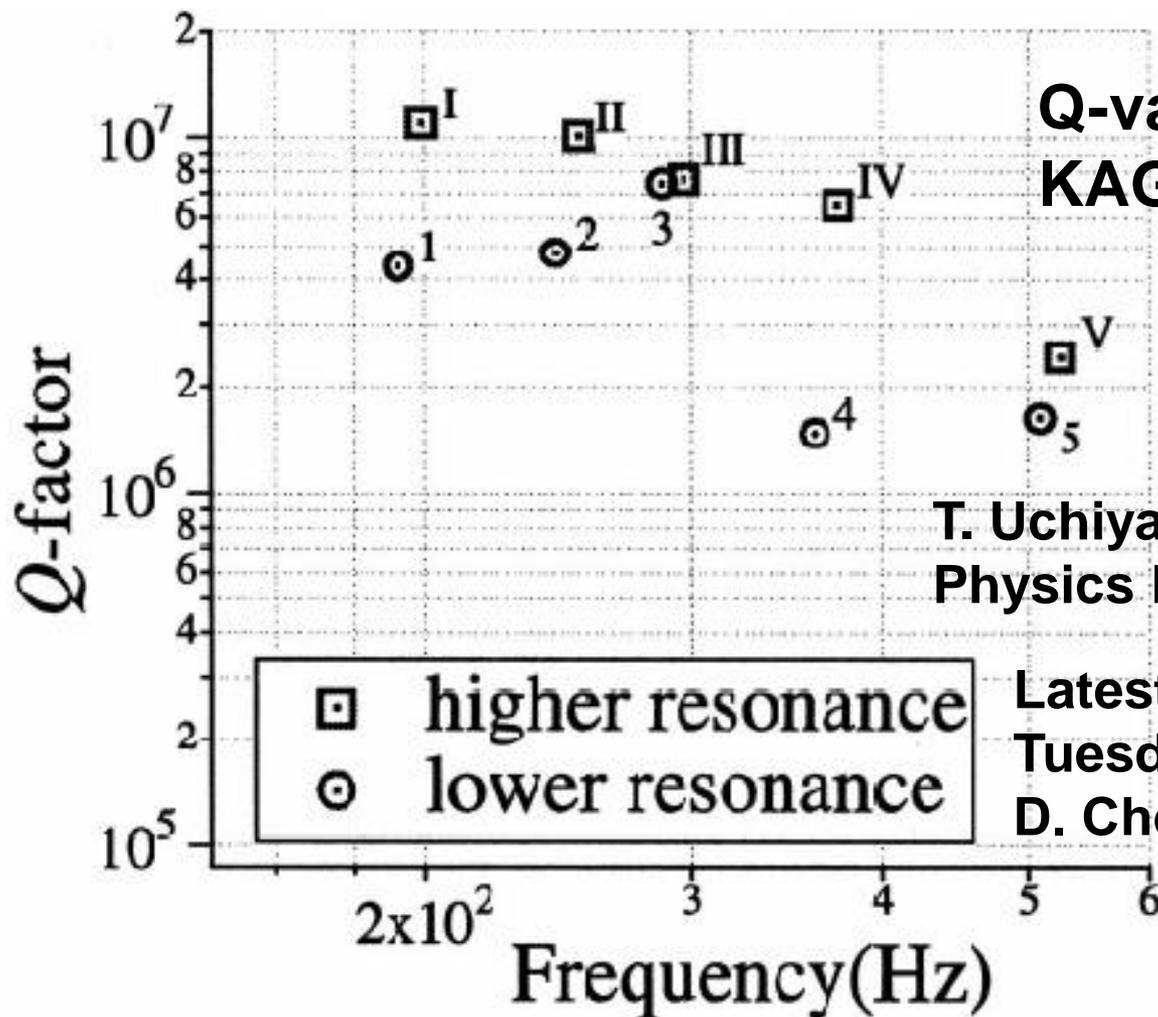
Thermal conductivity :  $5500 (T/20K)^3$  W/m/K

**Fiber diameter** must be larger than **1.6 mm**.

This requirement is severer than that of strength  
(**1.1 mm**).

# 3. Suspension

Q-values of sapphire fibers :  $5 \cdot 10^6$



Q-values are  $5 \cdot 10^6$ .  
KAGRA requirement

T. Uchiyama *et al.*,  
Physics Letters A 273 (2000) 310.

Latest update : D. Chen's talk on  
Tuesday morning,  
D. Chen's poster e-1 (Thu)

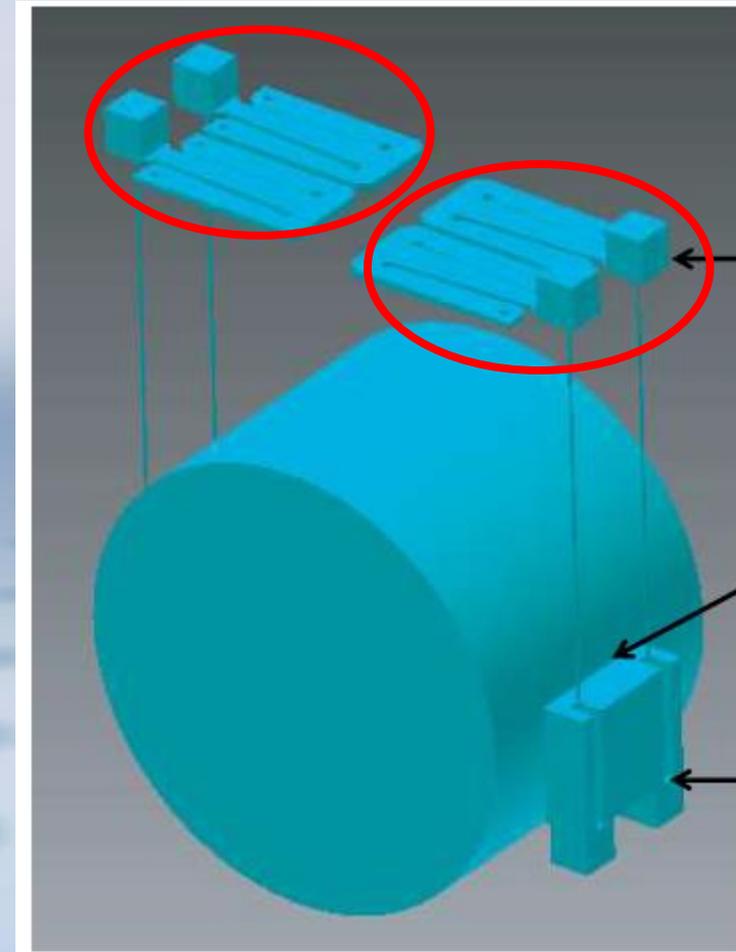
# 3. Suspension

Sapphire **fibers** are **thick**  
(1.6 mm in diameter)  
for heat transfer.

**Stretch** by sapphire mirror  
weight (23kg) : **21  $\mu\text{m}$**

If difference between length  
of 4 fibers are **larger than 21  $\mu\text{m}$** ,  
there is **no tension in one fiber !**

**Blade spring is necessary.**



# 3. *Suspension*

Requirement

Length difference compensation

**0.5 mm -> 22 Hz**

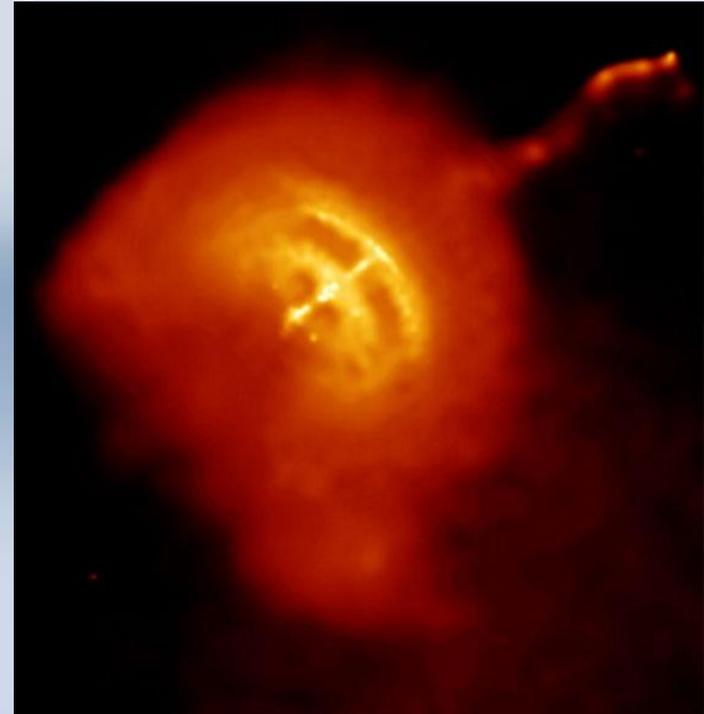
(Resonant frequency  
is inversely proportional  
to square root of length difference)

Pulsar search : Vela (22 Hz)

Current design : 14.5 Hz

R. Kumar's talk

on Wednesday afternoon, S. Barclay and G. Hammond's  
poster (d-4, Thu)



Vela pulsar (Wikipedia: English)

# 3. *Suspension*

Degrees of freedom

**Horizontal** motion along optical axis

**Pendulum** and **violin modes**

**Vertical** motion

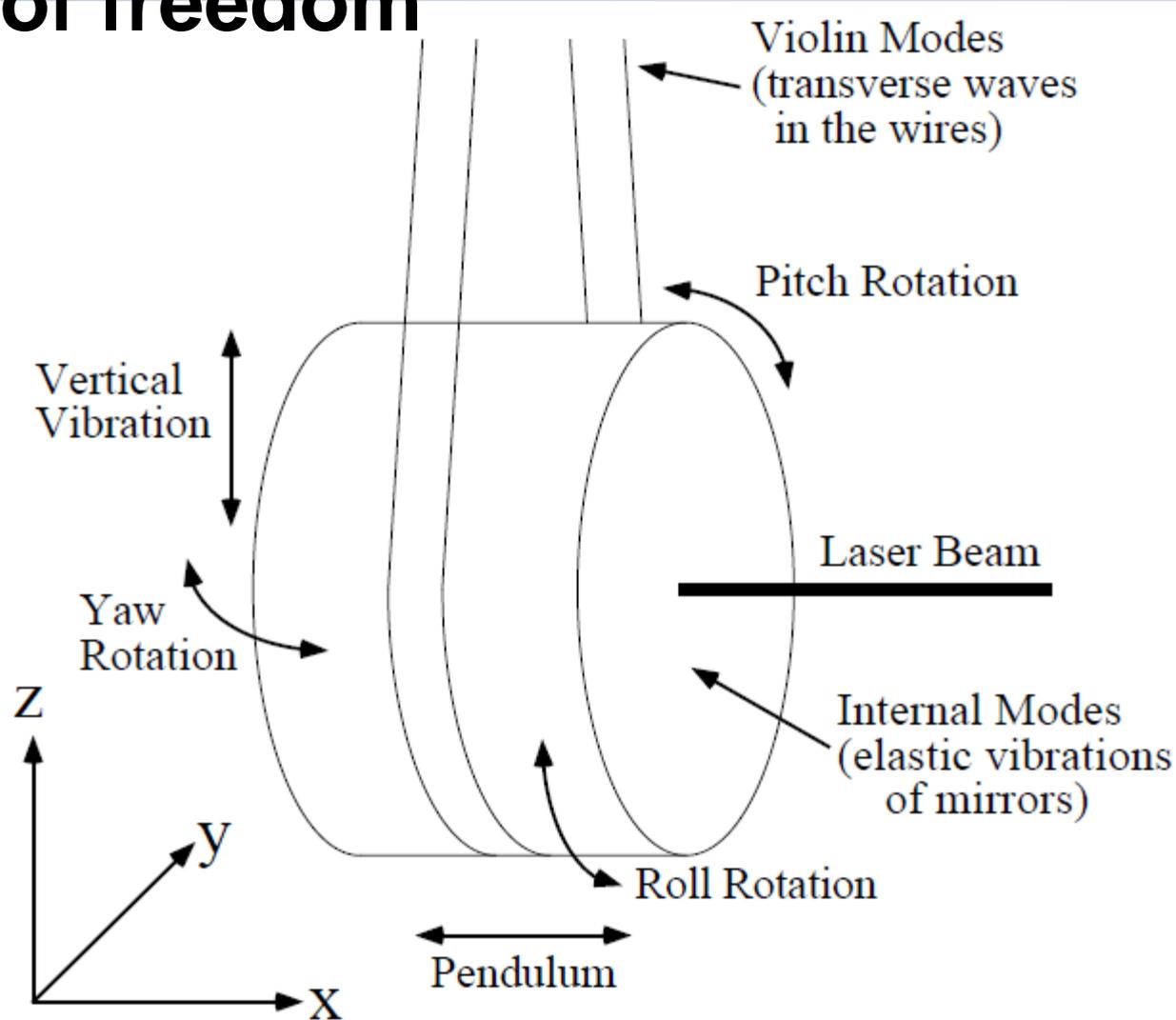
**Gradient of interferometer baseline** is  $1/300$   
for discharge of water in the mine.

**Rotation** (Pitch and Yaw)

**Distance** between **optical axis**  
and **center of gravity of mirror** is 1 mm.

# 3. Suspension

## Degrees of freedom



# 3. Suspension

## Resonant frequencies and Q-values

T. Sekiguchi, K. Somiya, K. Yamamoto

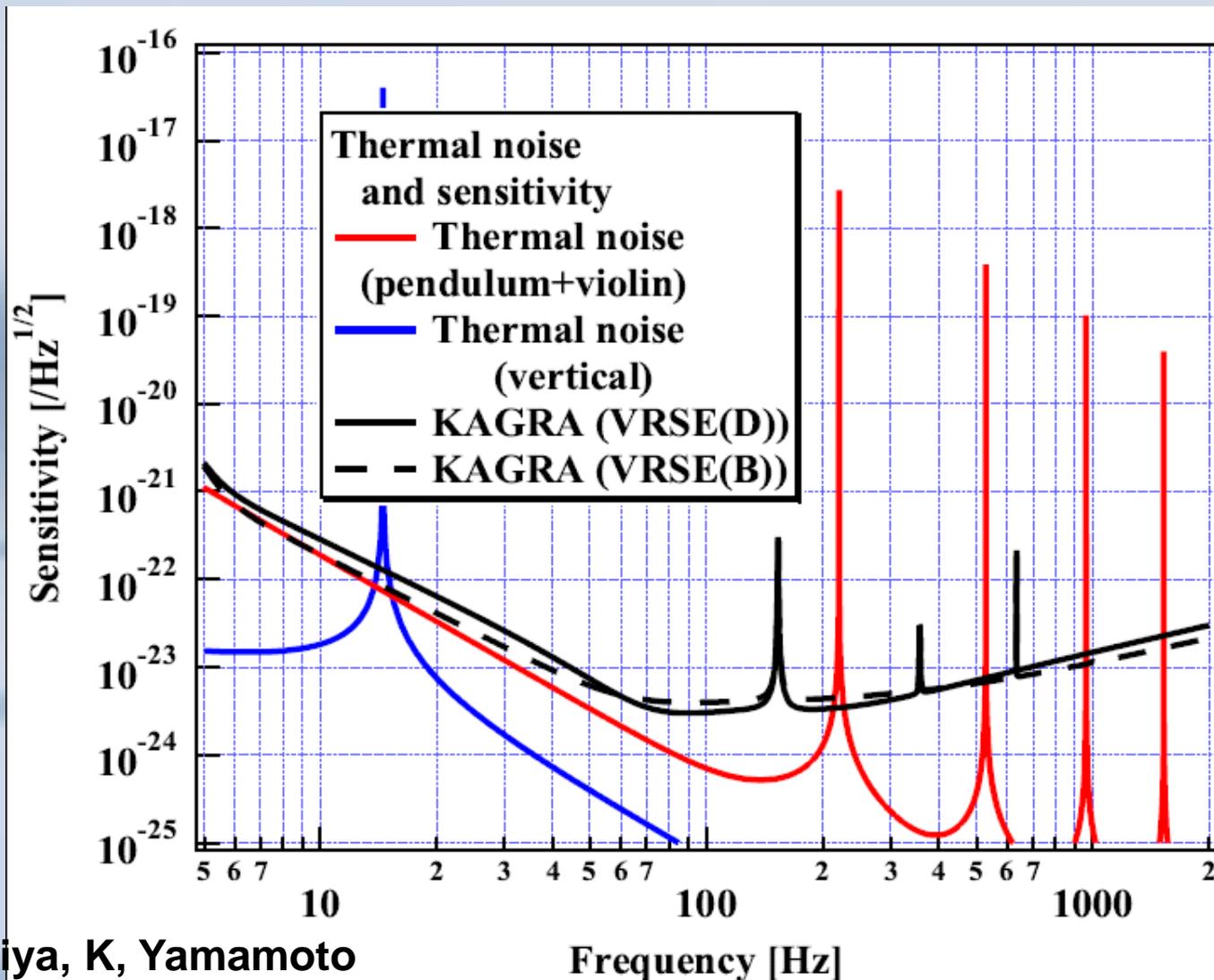
(Analytical calculation with simple assumption)

	Resonant frequencies	Q-values
Pendulum	1.1 Hz	$2 \cdot 10^7$
1 <sup>st</sup> violin	220 Hz	$1.0 \cdot 10^7$
Vertical	14.5 Hz	$5 \cdot 10^6$
Pitch	5.2 Hz	$5 \cdot 10^6$
Yaw	1.8 Hz	$2.2 \cdot 10^7$

In the cases of Pendulum (and violin) and Yaw modes, **loss dilution factors by gravity** were taken into account. Dilution factors are on the order of **unity** because of **thick fiber** (In the case of room temperature interferometer, they are on the order of 100 or 1000 ).

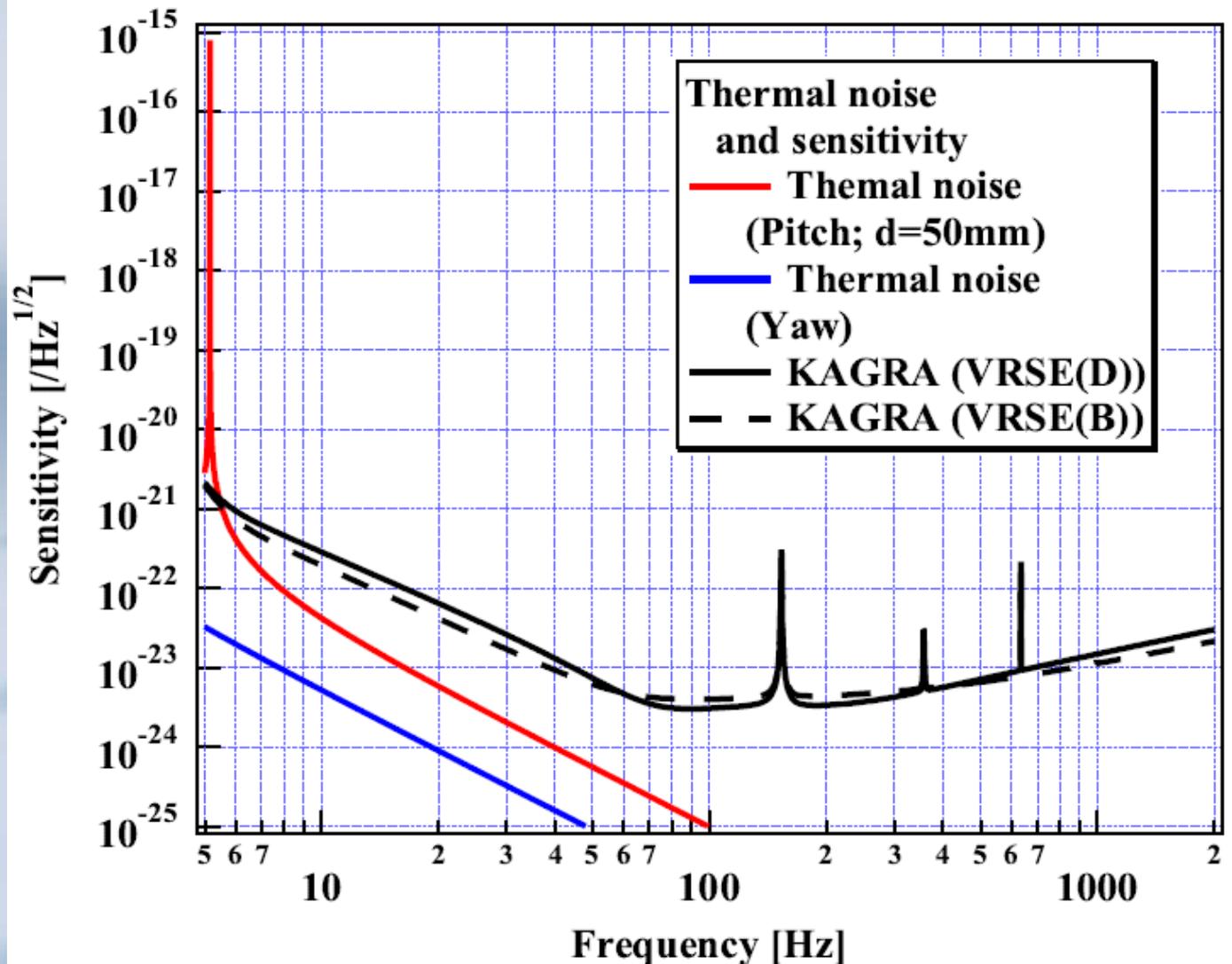
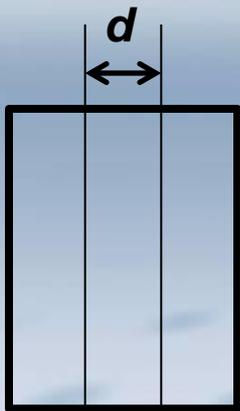
# 3. Suspension

## Horizontal and vertical motion



# 3. Suspension

## Pitch and yaw rotation



# 3. *Suspension*

In principle, KAGRA sensitivity is **not limited by thermal noise**.

However,

(1) There is not so large margin for pendulum around 10 Hz.

(2) The **1<sup>st</sup> violin mode** is around 220 Hz.

Advanced LIGO : 1<sup>st</sup> violin around 500 Hz

**Thick fiber to transfer heat !**

# 3. *Suspension*

**Thick fiber to transfer heat !**

**Elasticity is not perturbation** in KAGRA.

(1) **Thin** wire (only tension) :

Violin mode of **thicker** wire is **lower**.

**KAGRA** : Violin mode of **thicker** fiber is **higher** owing to elasticity (although it is not strong dependence).

# 3. *Suspension*

**Thick fiber to transfer heat !**

**Elasticity is not perturbation** in KAGRA.

(2) Frequency of the first violin mode

When we do not take elasticity into account,

1<sup>st</sup> violin mode is **139 Hz !**

Actually, the **1<sup>st</sup> violin mode** is **220 Hz**.

# 3. *Suspension*

**Thick fiber to transfer heat !**

**Elasticity is not perturbation** in KAGRA.

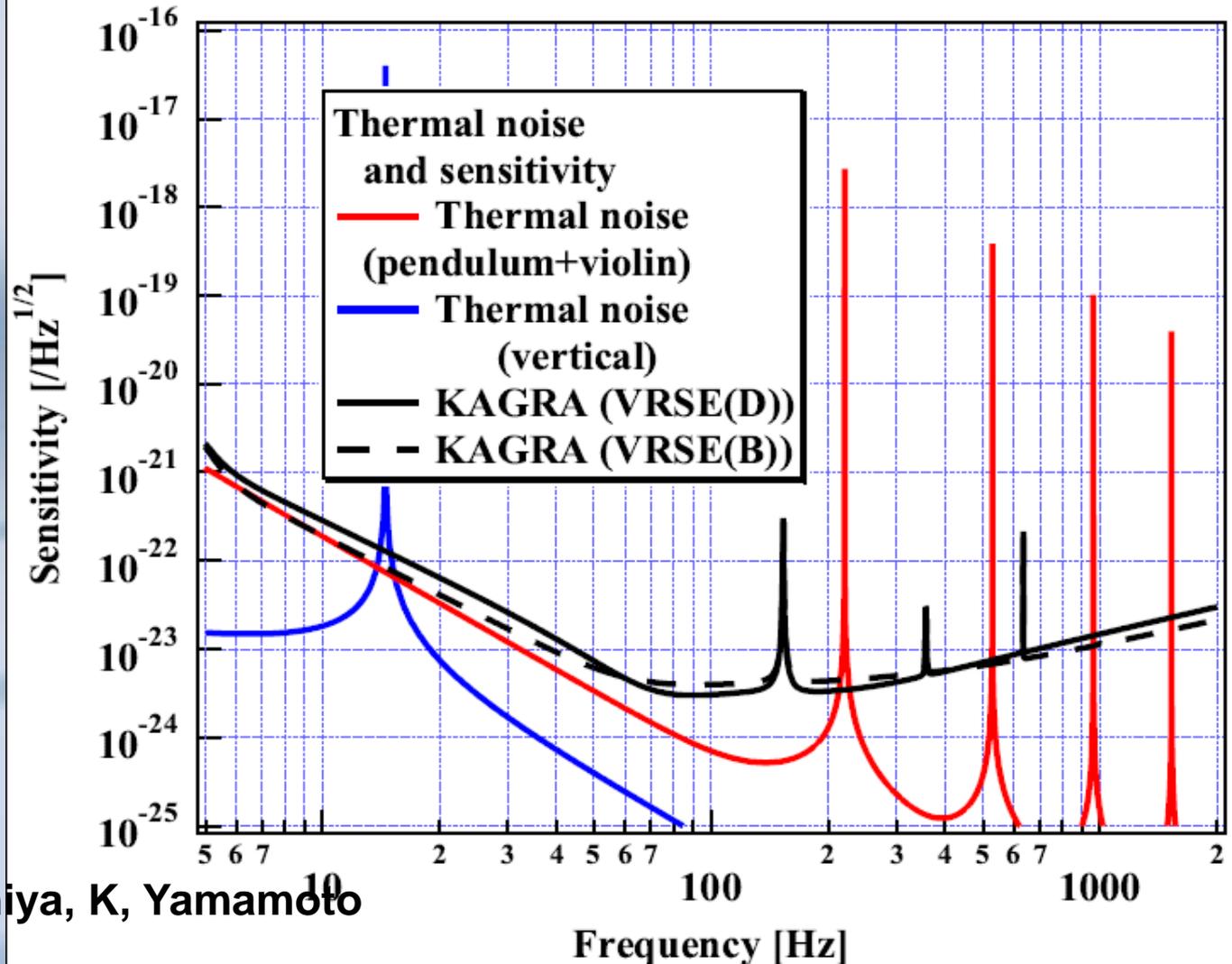
(3) Frequencies of higher violin modes

**Thin** wire (only tension) : n-th violin frequency is **n times** higher than fundamental frequency.

**Thick** wire (only elasticity) :  
n-th violin frequency is  **$n^2$  times** higher.

In KAGRA, both of **tension and elasticity** must be **considered**.

# 3. Suspension



# 3. *Suspension*

**Thick fiber to transfer heat !**

**Elasticity is not perturbation** in KAGRA.

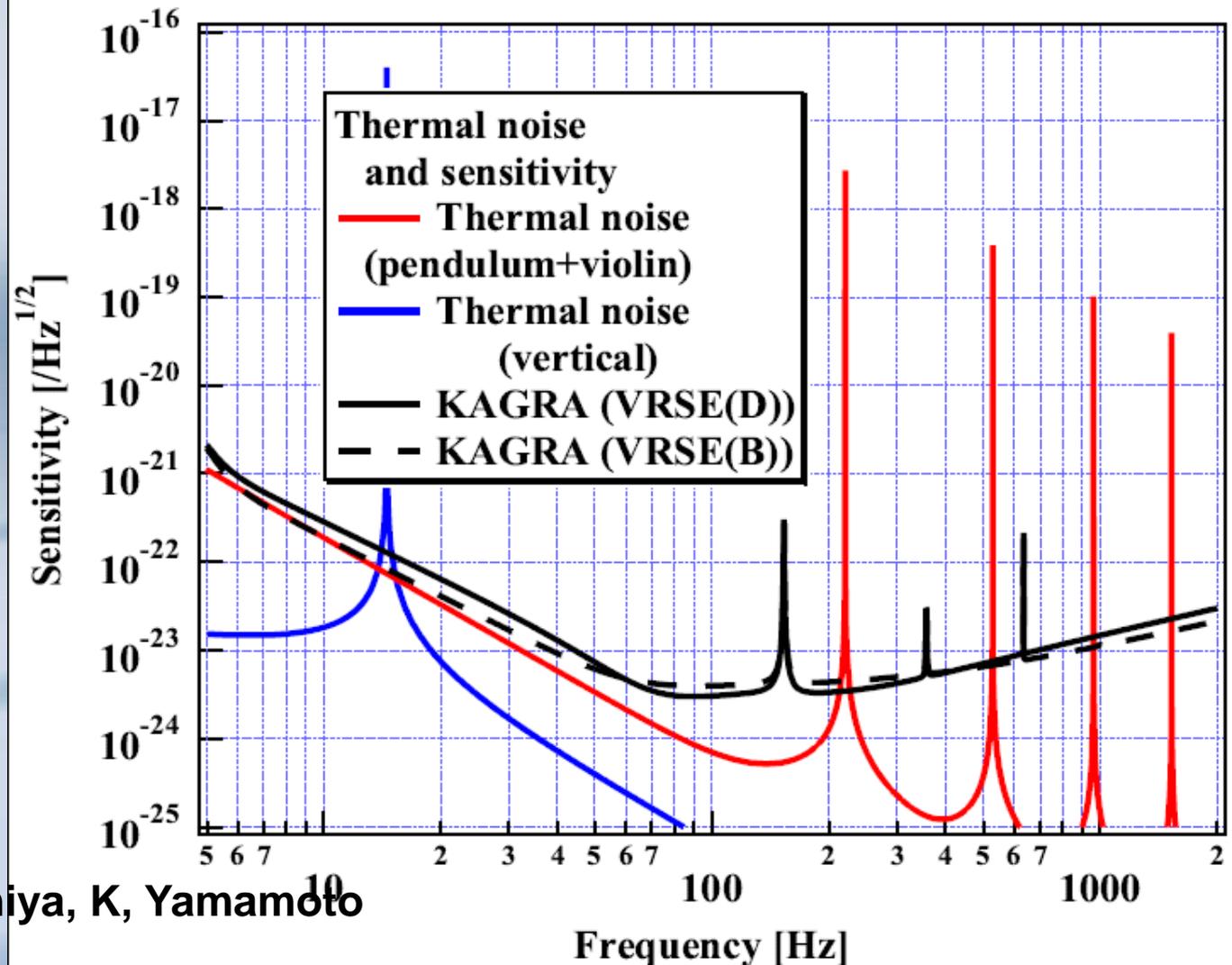
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# 3. *Suspension*

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In KAGRA, both of **tension and elasticity** must be **considered**.

# 3. *Suspension*

Higher violin modes ?

**Thicker fiber** : It is **not** so **effective**.

(2.2 mm diameter, 245 Hz)

**Shorter fiber** :

**Pendulum** mode thermal noise is **larger**.

**Mirror diameter** is 220 mm.

Current design (300mm) fiber

is **not** so **enough long** ...

# 3. *Suspension*

Open questions

Calculation

**Coupling** to other degree of freedom

Q of pendulum could be spoiled by blade spring ?

Measurement

**Bonding** mechanical dissipation

Sapphire **blade spring**

# ***4. ELITES***

**ELITES: ET-LCGT interferometric Telescope  
Exchange of Scientists  
Grant for **collaboration** about **cryogenic**  
between **KAGRA and ET**  
European 7th Framework Programme  
Marie Curie action (Mar. 2012 - Feb. 2016)**

**European people can visit Japan  
for KAGRA.**

# 4. ELITES

Measurement of **coating mechanical loss**  
at cryogenic temperature (**Glasgow**)  
nm layer coating (**Sannio**)

Sapphire fibers **with nail heads**

**Q-value**

Measurement in **Glasgow, Jena, Rome** and Tokyo

**Thermal conductivity**

Measurement in **Jena, Rome** and Tokyo

**Strength**

Measurement in **Glasgow**

# 4. ELITES

**Blade spring : Strength test (Glasgow)**

S. Barclay and G. Hammond's poster (d-4, Thu)

**Bonding**

Marielle van Veggel's talk (Monday afternoon)

**Hydroxide Catalysis Bonding (Glasgow)**

B. Douglas and Marielle van Veggel' poster (d-3, Thu)

**Indium (Jena, Glasgow)**

# 5. Summary

**Outlines** of KAGRA thermal noise  
(**sapphire suspension**) were discussed.

**Cryogenic technique** reduces **thermal noise**.

Open issues

(1) **Coating** mechanical loss

Collaboration (Tokyo-Glasgow) is in active.

(2) Measurement of **bonding** mechanical loss

We have plans in near future (Jena, Glasgow).

(3) Measurement for sapphire **blade spring**

(4) Precise **calculation**

# ***5. Summary***

**ELITES** supports our investigation.

**Vivid and latest updates** are reported by **younger** people **later**.

R. Kumar's talk on Wednesday afternoon

A. Khalaidovski's and D. Chen's talk

on Tuesday morning, D. Chen's poster e-1(Thu)

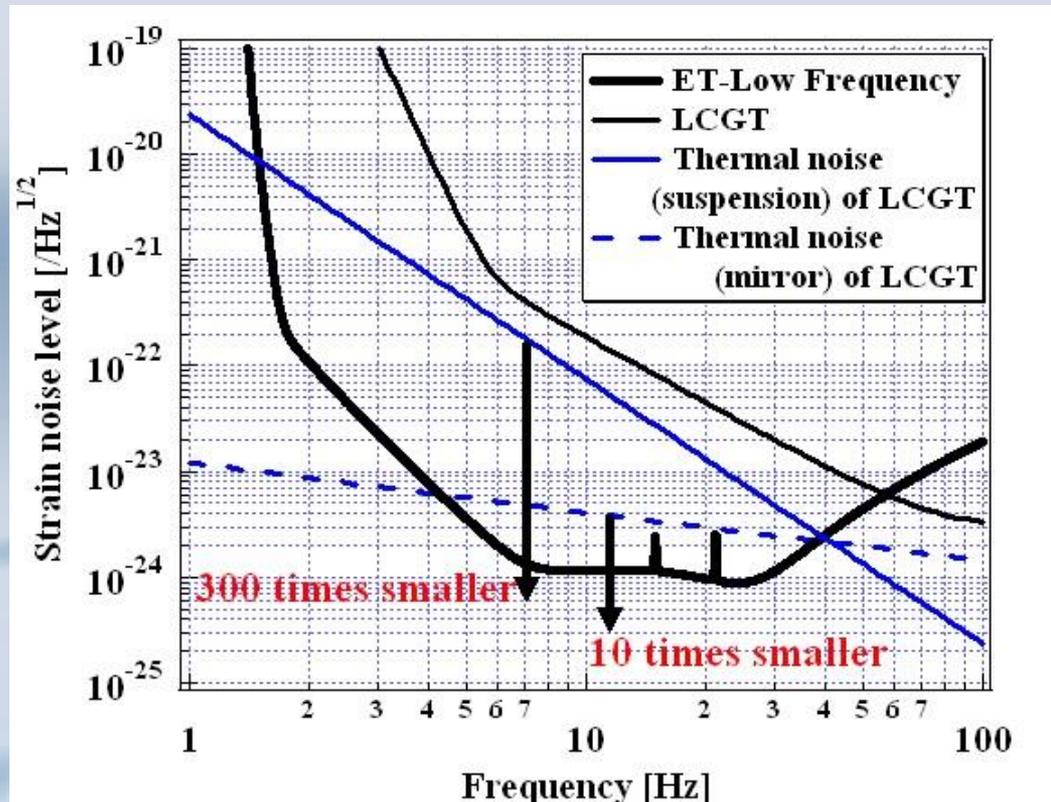
**Thank you for your attention !**

# 5. Einstein Telescope

(a) Thermal noise

**Mirror** thermal noise : **10** times smaller

**Suspension** thermal noise : **300** times smaller



S. Hild *et al.*, Classical and Quantum Gravity 28 (2011) 094013.

R. Nawrodt *et al.*, General Relativity and Gravitation 43 (2011) 363.

# 5. *Einstein Telescope*

(a) Thermal noise

**Mirror** thermal noise : **10** times smaller

**3** times **longer arm** (10 km)

**3** times **larger beam radius** (9cm)

**Suspension** thermal noise : **300** times smaller

**3** times **longer arm** (10 km)

**7** times **heavier mirror** (200 kg)

**5** times **longer suspension wire** (2 m)

**100** times **smaller dissipation in wires** ( $Q=10^9$ )

# ***4. Challenges for cryogenic***

**1. Issues of cooling : Reduction of heat load  
(Absorption in mirror)**

**In order to keep mirror temperature ...  
Absorption in mirror : less than **1 W****

**Coating : 0.4 W (1 ppm)**

**Substrate : 0.6 W (**50 ppm/cm**)**

**Our target of substrate : **20 ppm/cm****

# Sensitivity of KAGRA

## Thermal noise

**Assumption (1) : Upper ends of fibers are fixed rigidly.**  
Resonant frequencies (except for violin modes) are different from the actual system. However, the thermal noise above the resonant frequency is the same.

**Assumption (2):**

**Number of fiber : 4**

**Fiber length : 0.3 m**

**Fiber diameter : 0.16 mm**

**Q-values of sapphire fibers :  $5 \cdot 10^6$**

**Horizontal motion along optical axis**

**Pendulum and violin modes**

**Loss dilution by tension (gravity) must**

**be taken into account.**

# Sensitivity of KAGRA

## Thermal noise

### Vertical motion

Gradient of interferometer baseline is  $1/300$ .

Q-values of stretch is assumed to be  $5 \cdot 10^6$ .

### Pitch motion

Distance between the optical axis

and center of gravity of mirror is 1 mm.

Q-values of stretch is assumed to be  $5 \cdot 10^6$ .

### Yaw motion

Distance between the optical axis

and center of gravity of mirror is 1 mm.

Q-values of shear is assumed to be  $5 \cdot 10^6$ .

Loss dilution by tension (gravity) must

be taken into account<sub>53</sub>

# ***3. Expected thermal noise***

## **Horizontal and vertical motion**

**Four sapphire fibers should transfer 1 W heat.**

**Between 100 Hz and 250 Hz, there are 1<sup>st</sup> violin mode and vertical mode.**

**Room temperature interferometer : 1<sup>st</sup> violin > 300 Hz  
vertical mode ~ 10 Hz**

**Thick fiber to transfer heat !**

**Thicker fiber : Lager thermal noise (pendulum mode)**

**Longer fiber : Lower violin mode, lower vertical mode  
-> Smaller heat transfer**

**Shorter fiber : Higher violin mode, higher vertical mode  
-> Fiber should be longer than mirror radius**

# Known methods of bonding

	Precise polish	Interposition material	Temperature treatment	Sapphire-Sapphire	Thermal conductance	Mechanical loss
AFB, Diffusion	Necessary	none	1300~1400 °C	<del>Almost same as bulk</del> ~ 28 MPa	~ 4 W/K/mm <sup>2</sup>	Not yet measured
Direct(1), SAB1 (~ 2000)	Necessary	None (Ar <sup>+</sup> beam)	300 K	-	-	-
Direct(1), SAB2 (2011)	Necessary	Fe, etc (Ar <sup>+</sup> beam)	300 K	Not yet measured	Not yet measured	Not yet measured
Hydroxy-catalysis, silicate	Necessary	KOH, Na <sub>2</sub> SiO <sub>3</sub> , H <sub>2</sub> O	300 K	~ 7 MPa	~ 0.3 W/K/mm <sup>2</sup>	Not yet measured
Metalize, soldering	(Not required)	Active metal	< 1000 °C?	<del>Not yet measured</del> 50MPa	Not yet measured	Not yet measured
Adhesive	Not required	Al <sub>2</sub> O <sub>3</sub> , AlPO <sub>4</sub> , H <sub>2</sub> O	~ 500 °C	~20 MPa	Not yet measured	Not yet measured

AFB: Adhesion Free Bonding  
SAB: Surface activation Bonding

20MPa  
(Ultrasonic soldering)

# 3. *Expected thermal noise*

## Horizontal and vertical motion

In principle, KAGRA sensitivity is **not limited by thermal noise**.

However, between 100 Hz and 250 Hz (**best sensitivity frequency region**), there are peaks of **1<sup>st</sup> violin mode** and **vertical mode**.

Ratio of frequency of 1<sup>st</sup> violin mode to that of pendulum mode is smaller than that of room temperature interferometer.

Room temperature interferometer :

1<sup>st</sup> violin > 300 Hz, vertical mode ~ 10 Hz

**Thick fiber to transfer heat !**

Note : These peaks make Signal to Noise Ratio of matched filter for neutrons star coalescence about 0.95 times smaller (K. Yamamoto).

Can we push **thermal noise peaks** away ? (K. Somiya)

# ***3. Expected thermal noise***

## **Pitch and yaw rotation**

In principle, KAGRA sensitivity is **not limited by thermal noise**.

Around **20 Hz**, there is **peak of pitch mode**.

Room temperature interferometer : pitch mode ~ 3 Hz

**Thick fiber to transfer heat !**

Pitch mode frequency depends

on **distance between fibers ( $d$ )**.

This distance must be as small as possible (**15 mm~30 mm**).

Note : If this mode is lower than 30 Hz, the effect on Signal to Noise Ratio of matched filter for neutrons star coalescence is small (H. Yuzurihara). 57

# ***3. Suspension***

**Diameter of fiber :**

**Bending length is proportional to square of fiber diameter.**

**Bending length is about 50 mm  
(1.6mm diameter fiber)**

**Mirror radius : 110 mm**

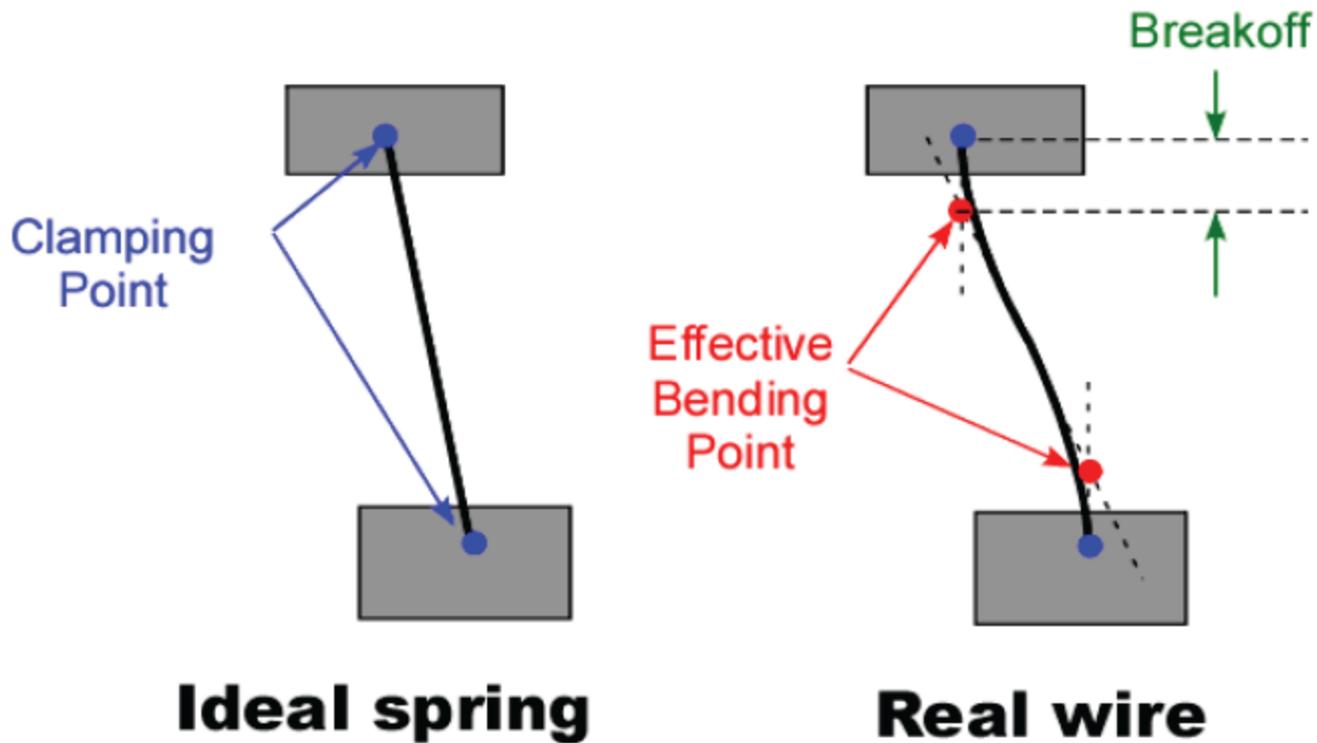
**Fiber diameter is smaller than about 2.2 mm.**

# 3. Suspension

Diameter of fiber :  
Bending length

T. Sekiguchi, Master thesis (2012)

<http://gwdoc.icrr.u-tokyo.ac.jp/cgi-bin/private/DocDB/ShowDocument?docid=770>



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