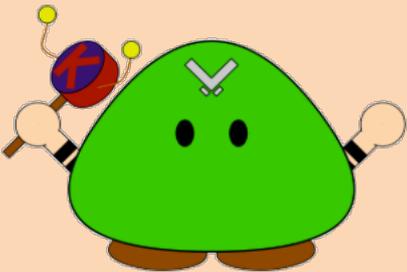




Thermal noise reduction with higher-order Laguerre-Gauss modes

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GWADW 2014

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Outline

✧ Introduction

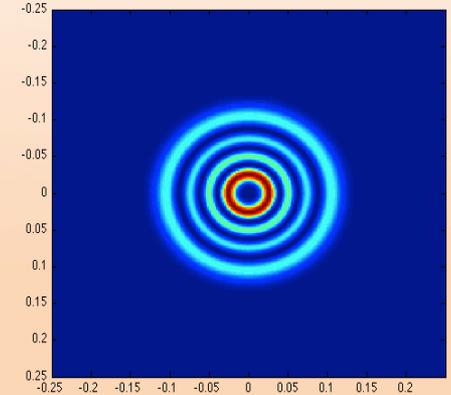
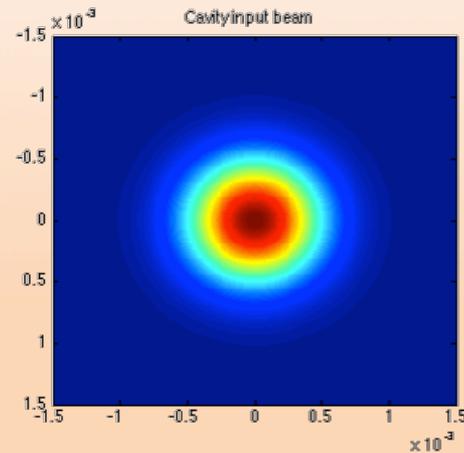
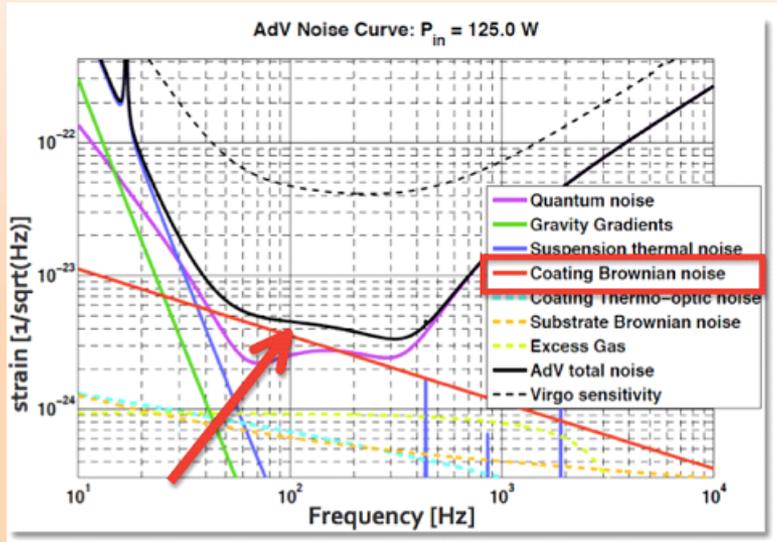
✧ State of the art

✧ Non-Gaussian interferometer at the APC

✧ Reduction of the degeneracy

✧ Conclusions

Introduction



- ✧ Sensitivity of 2nd generation gravitational wave detectors will be limited by coating thermal noise around 100 Hz
- ✧ For same diffraction losses, Laguerre-Gauss (LG_{pl}) modes reduce thermal noise thanks to their larger coverage of the surface
- ✧ LG modes resonate in spherical Fabry-Perot cavities
- ✧ LG_{33} mode reduces thermal noise by ≈ 1.8 in AdVirgo geometry ³

Outline

✧ Introduction

✧ **State of the art**

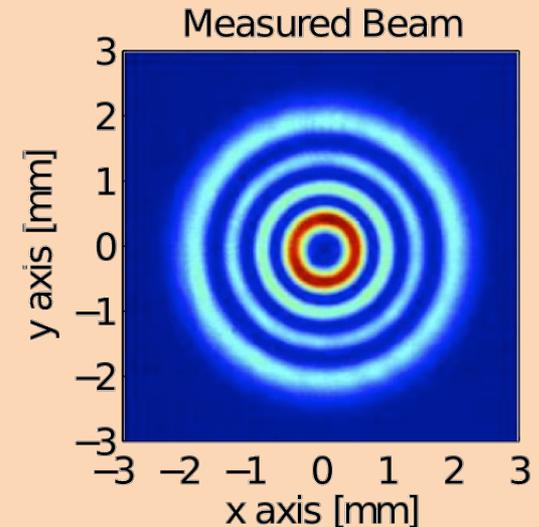
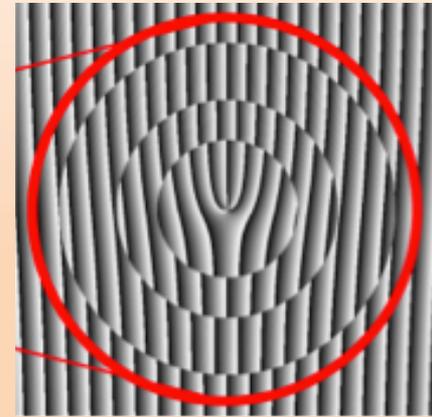
✧ Non-Gaussian interferometer at the APC

✧ Reduction of the degeneracy

✧ Conclusions

Beginning: LG generation

- ✧ A generic LG beam can be generated by spatial light modulators or diffractive phase plate and a mode cleaner cavity
- ✧ High modal purity achieved ($\sim 99\%$) [1,2]
- ✧ High power generation has been obtained using a phase plate [3]
 - 83 W on LG_{33} mode
 - Conversion efficiency 59%
 - Modal purity $> 97\%$ also at high power



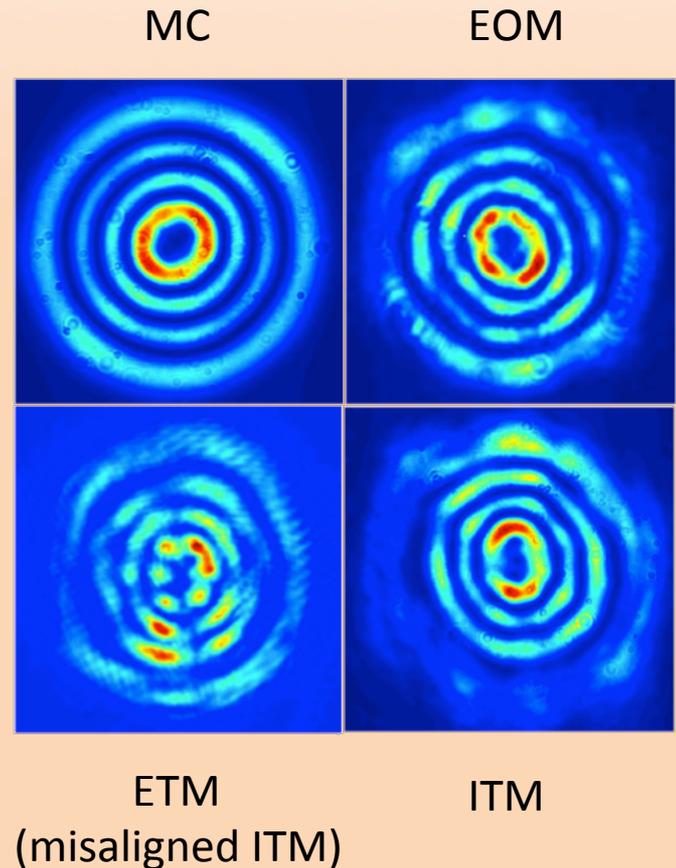
[1] M. Granata et al., PRL 105, 231102 (2010)

[2] P. Fulda et al., Physical Review D 82, 012002 (2010)

[3] L. Carbone et al., PRL 110, 251101 (2013)

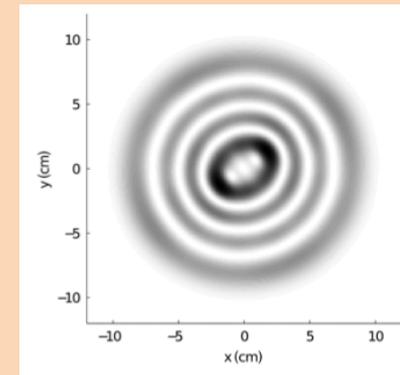
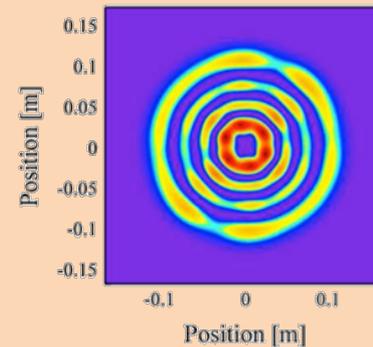
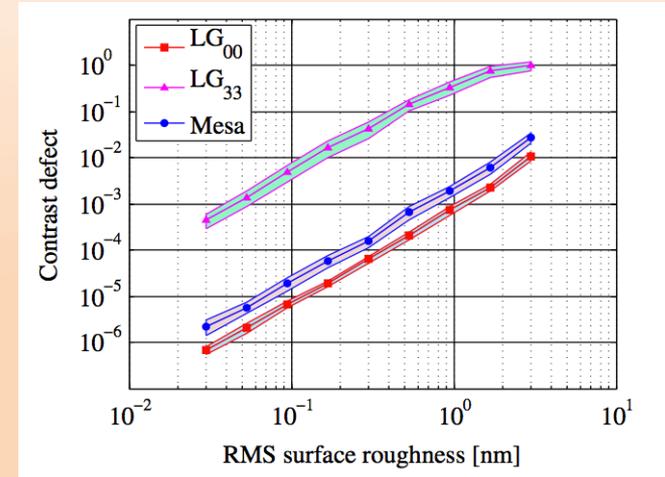
Glasgow 10-m cavity

- ✧ First attempt to realize a suspended cavity resonating on LG_{33} mode
- ✧ Locking on the LG_{33} mode not achieved
- ✧ Complexity of the LG system
 - Clipping
 - Mode matching
 - Resonance splitting due to astigmatism



Main problem: LG degeneracy

- ✧ A n-order LG mode is n-times degenerated
- ✧ Expected contrast defect 3 order of magnitude worse than Gaussian beam: target value (10^{-4}) reached for RMS < 0.01 nm [5]
- ✧ Greater coupling on other n-order modes due to lower order defects [6-7]

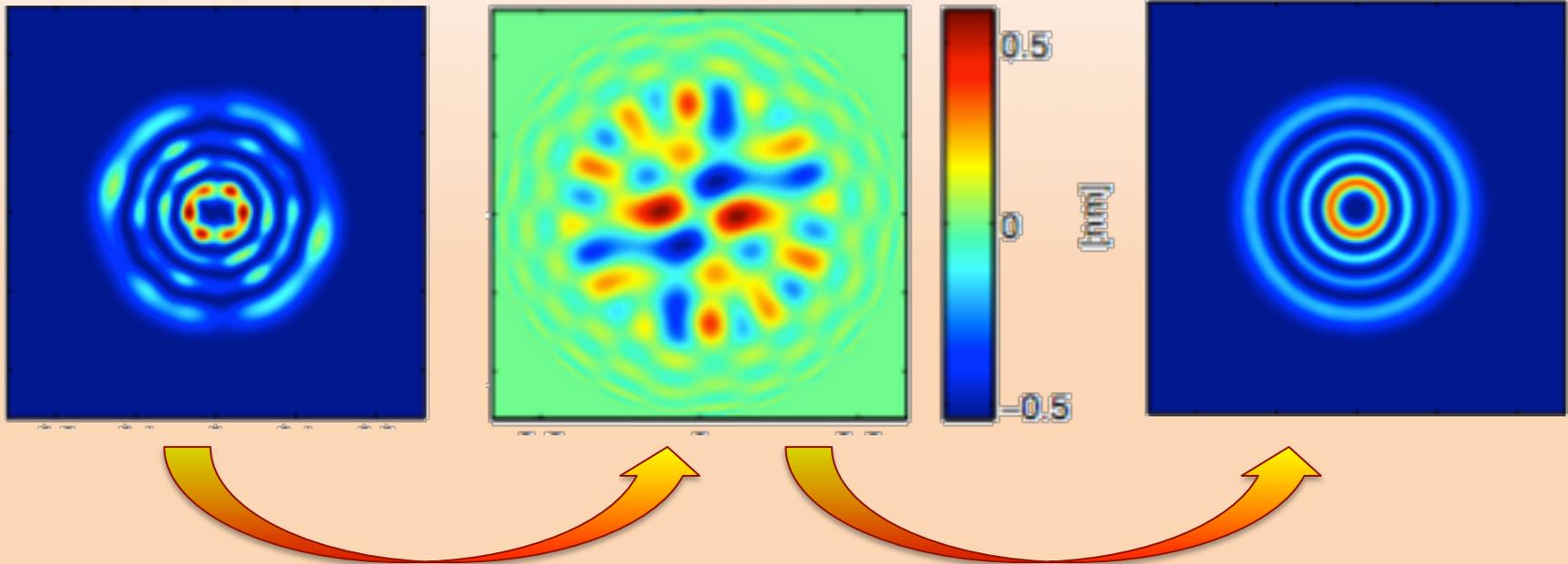


[5] T. Hong et al., Physical Review D 84, 102001 (2011)

[6] M. Galimberti et al, GWADW 2010

[7] C. Bond et al., Physical Review D 84, 102002 (2011)

Thermal compensation



- ✧ CHRAC: possible in-situ thermal correction of mirror defects to recover a high beam quality ($> 99.9\%$) [8]
- ✧ Adaptive algorithm for estimating the map directly from the reflected intensity pattern [9]

[8] R. A. Day et al., Physical Review D 87, 082003 (2013)

[9] G. Vajente, R. A. Day, Physical Review D 87, 122005 (2013)

Questions

- ✧ Is a LG fabry-Perot Michelson interferometer feasible?
- ✧ Is the degeneracy an unsolvable problem?

Outline

✧ Introduction

✧ State of the art

✧ **Non-Gaussian interferometer at the APC**

✧ Reduction of the degeneracy

✧ Conclusions

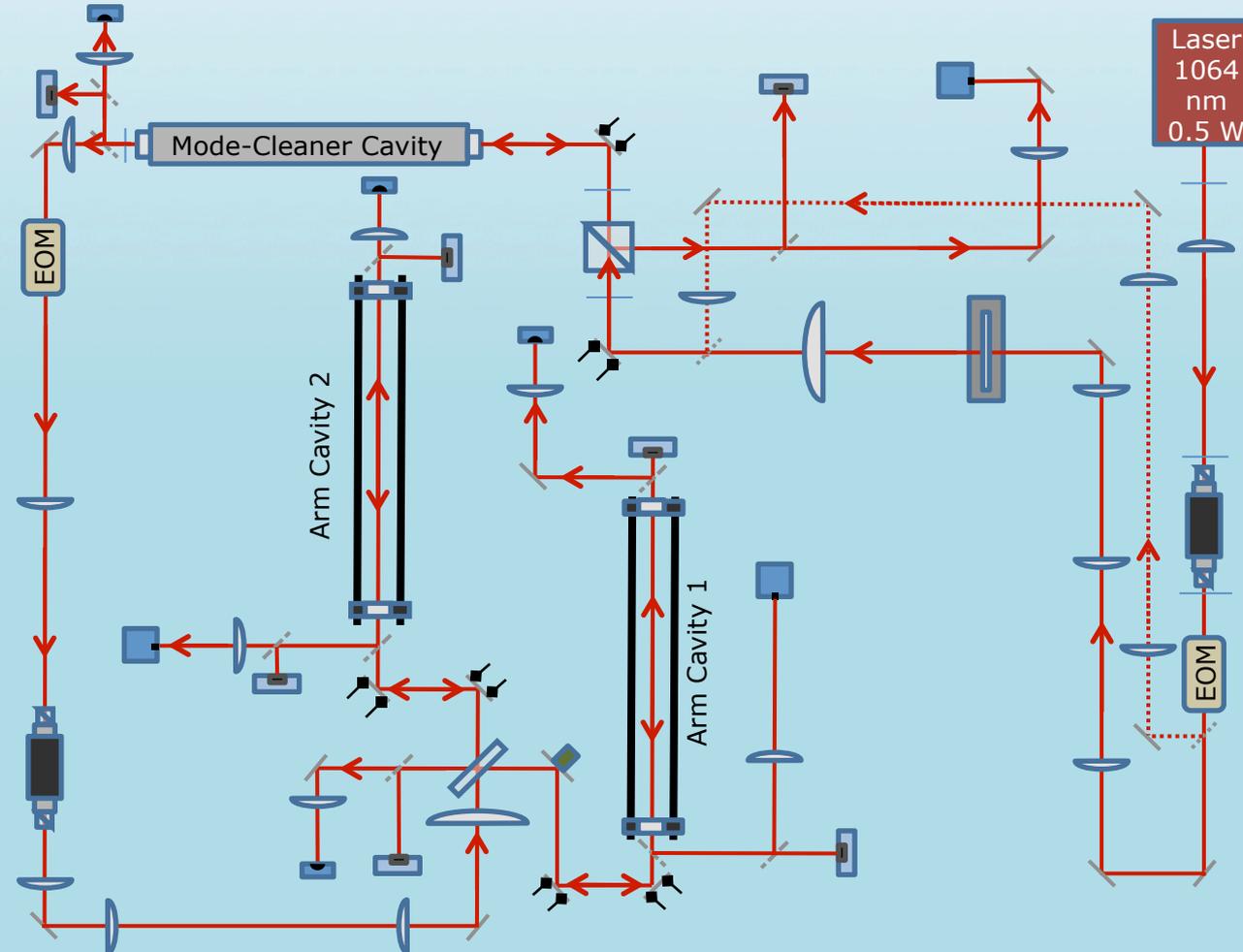
Aim of *Non-Gaussian ITF*

Realize a table-top interferometer using a non-Gaussian (LG₃₃) mode

- ✧ LG system feasibility
 - Matching and pre-alignment procedures using Gaussian beam
 - Control systems (longitudinal and angular)
- ✧ Identification of the main limits and constraints
- ✧ Comparison between measures and simulations

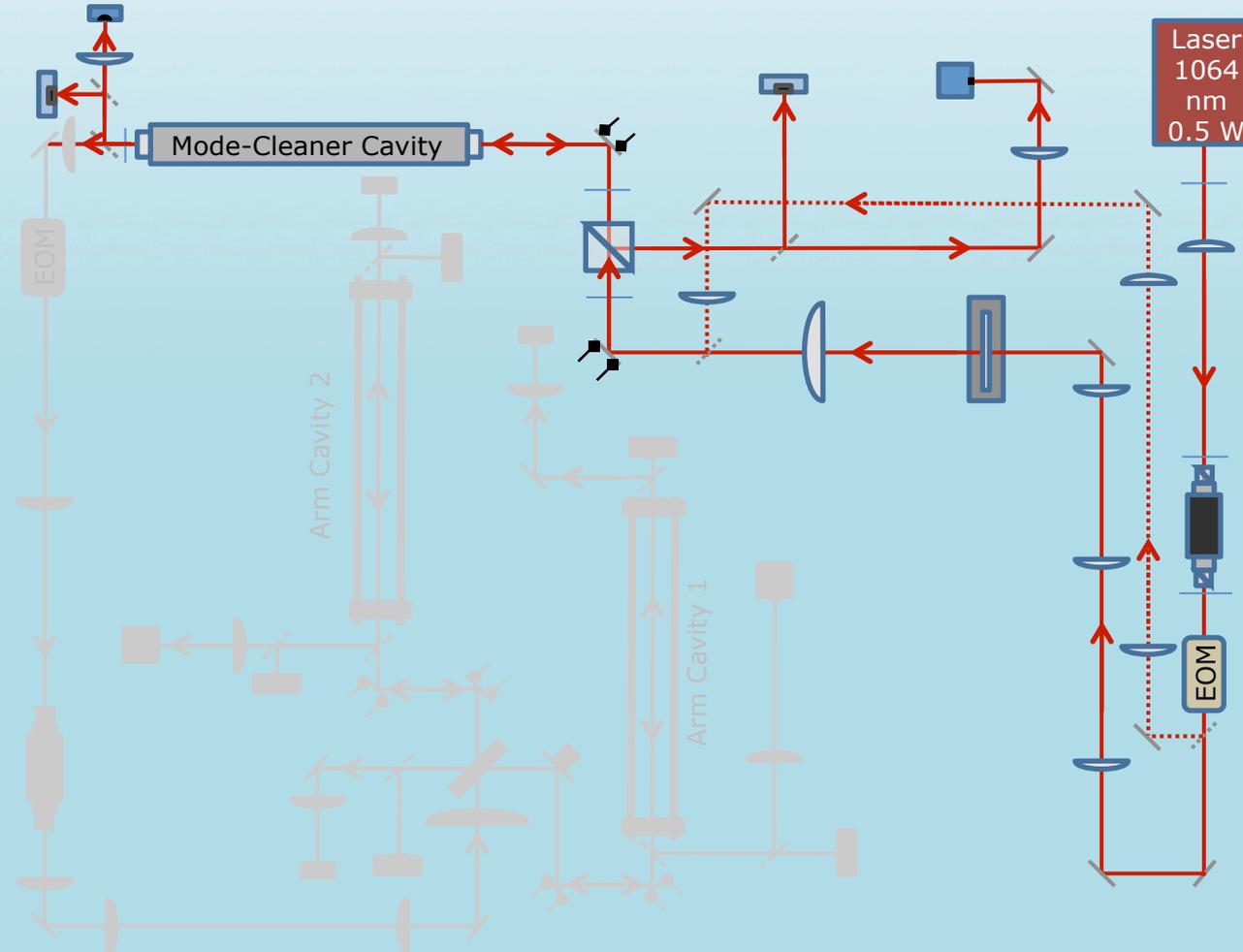
- ✧ Test other modes (LG and non-LG)
- ✧ Mirror thermal compensation

Optical scheme



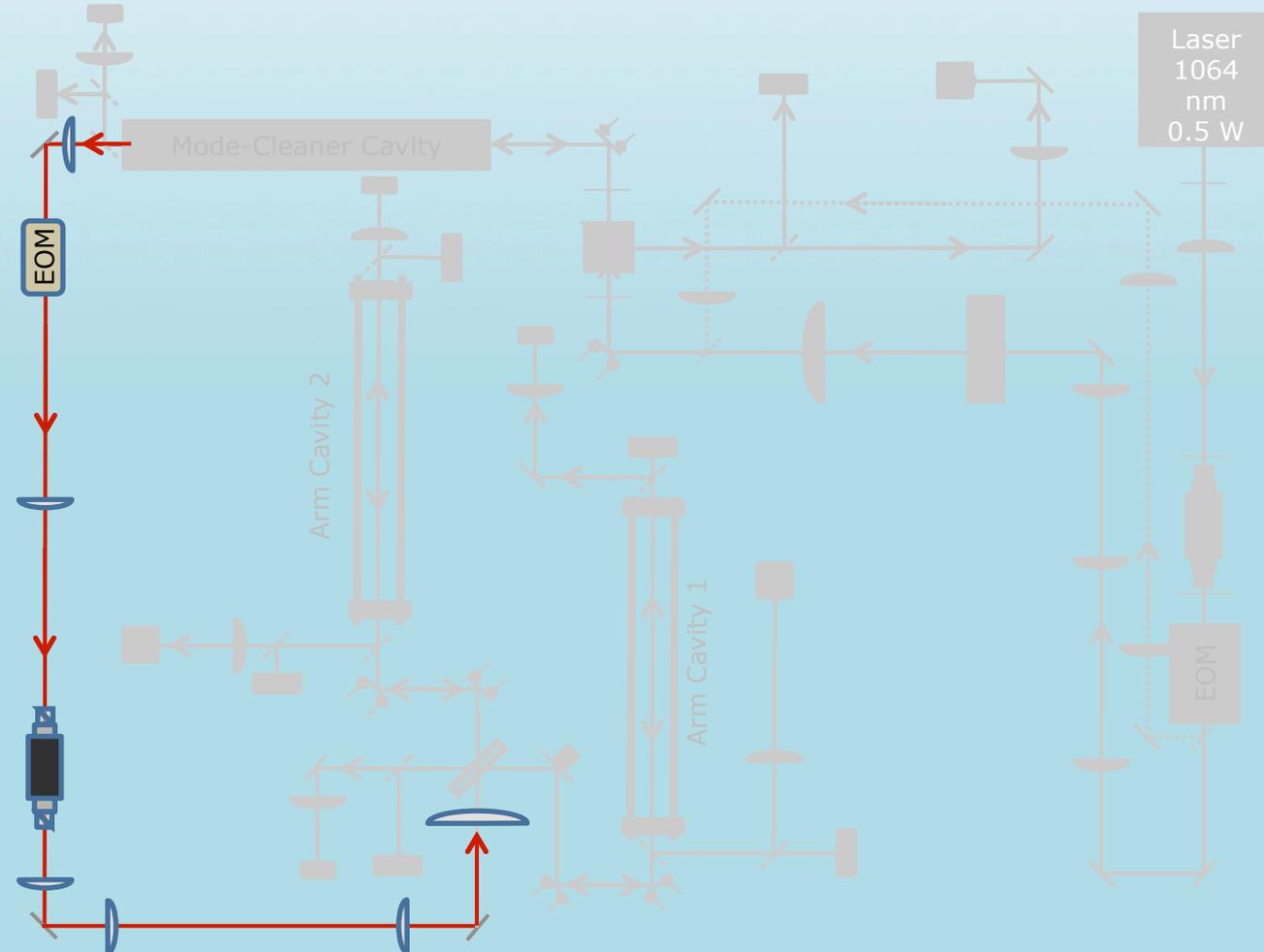
- ◇ Generation:
 - Phase plate
 - Linear mode cleaner
- ◇ Mode matching telescope
- ◇ Fabry-Perot arm cavities ($F=200$)
- ◇ 30-cm long plano-concave cavities
- ◇ Gaussian beam used for alignment and matching

Optical scheme



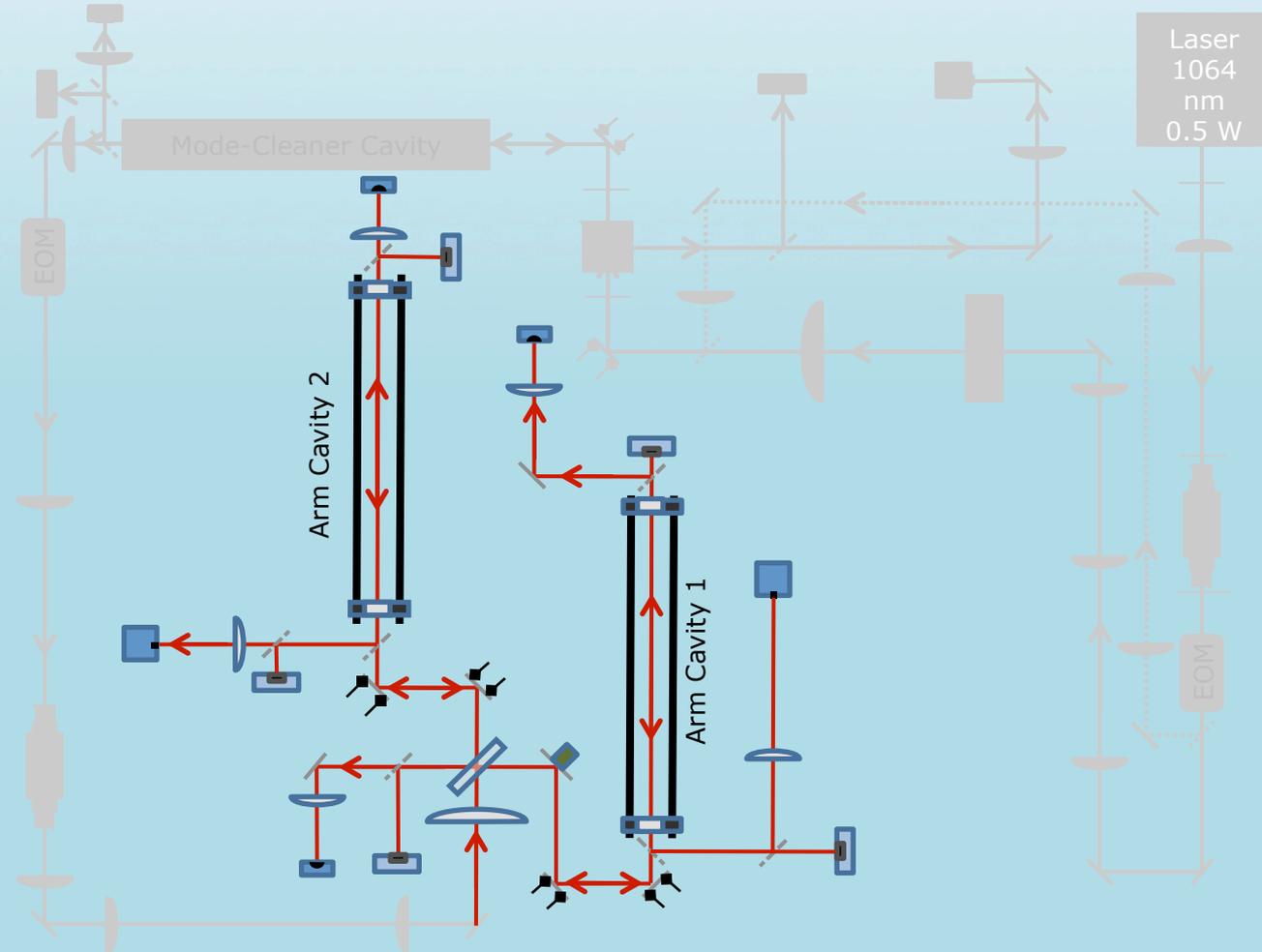
- ✧ **Generation [1]:**
 - **Phase plate**
 - **Linear mode cleaner**
- ✧ **Mode matching telescope**
- ✧ **Fabry-Perot arm cavities ($F=200$)**
- ✧ **30-cm long plano-concave cavities**
- ✧ **Gaussian beam used for alignment and matching**

Optical scheme



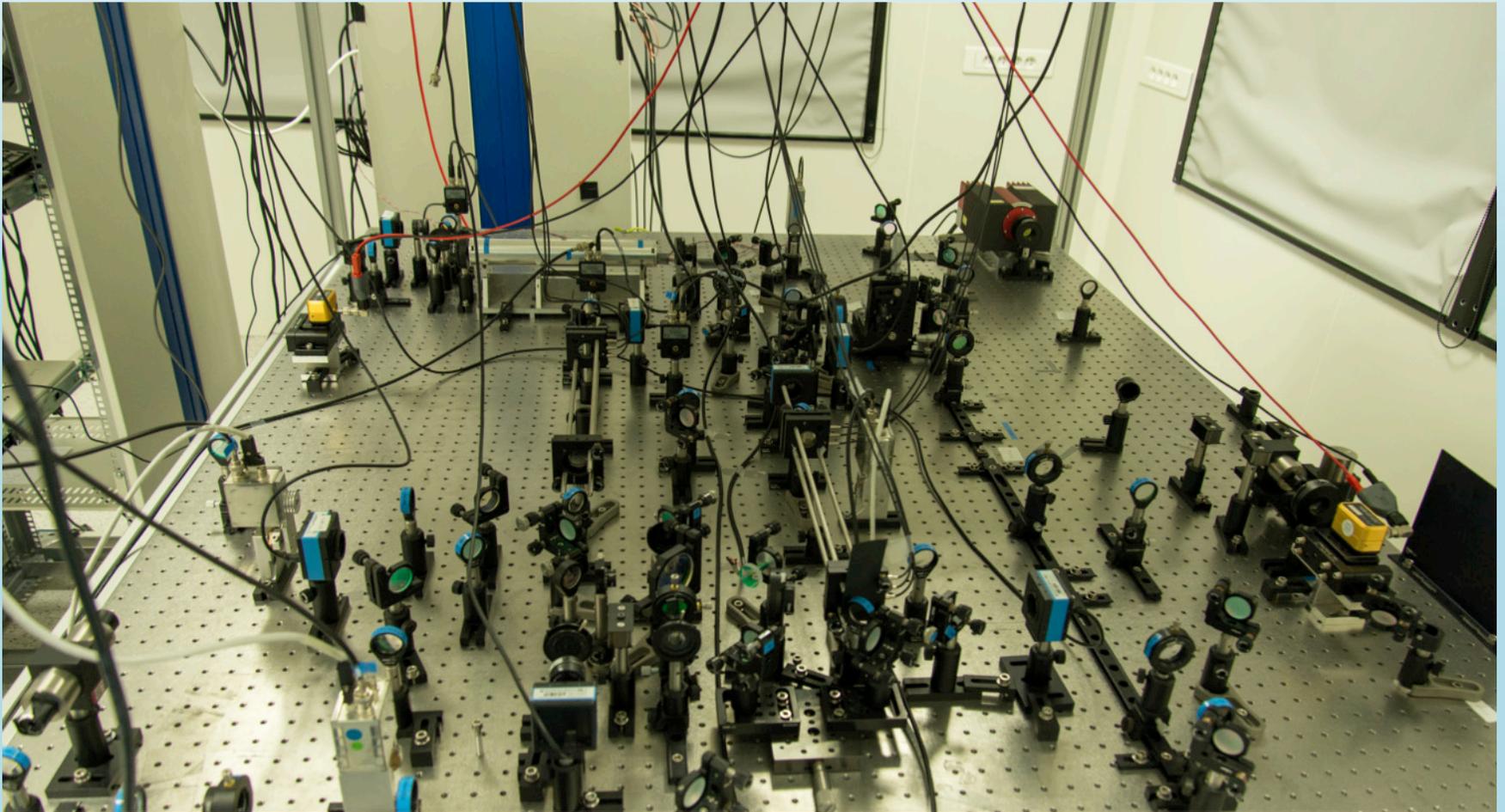
- ◇ Generation:
 - Phase plate
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Optical scheme

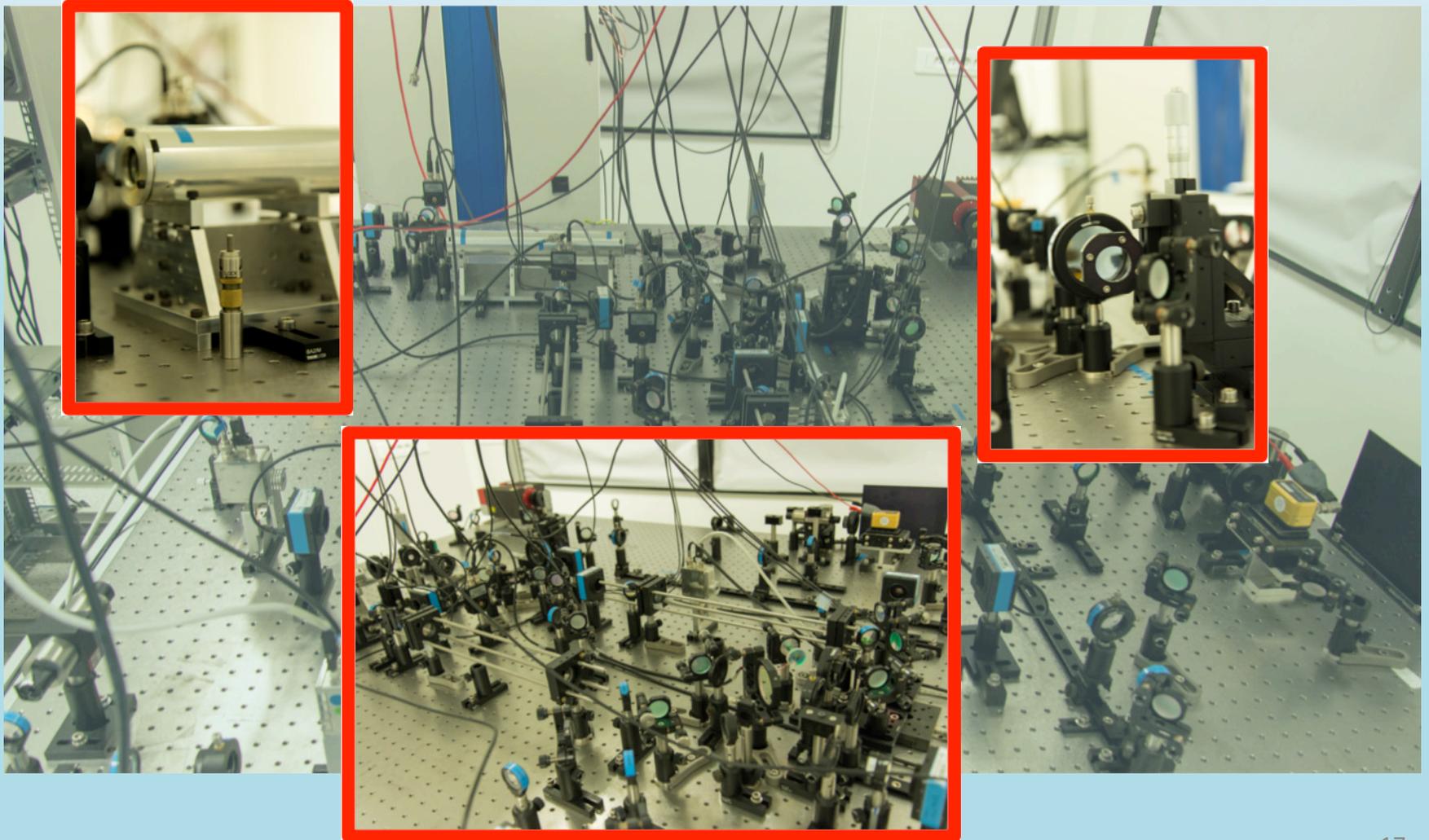


- ◇ Generation:
 - Phase plate
 - Linear mode cleaner
- ◇ Mode matching telescope
- ◇ **Fabry-Perot arm cavities (F=200)**
- ◇ 30-cm long plano-concave cavities
- ◇ Gaussian beam used for alignment and matching

Experimental setup

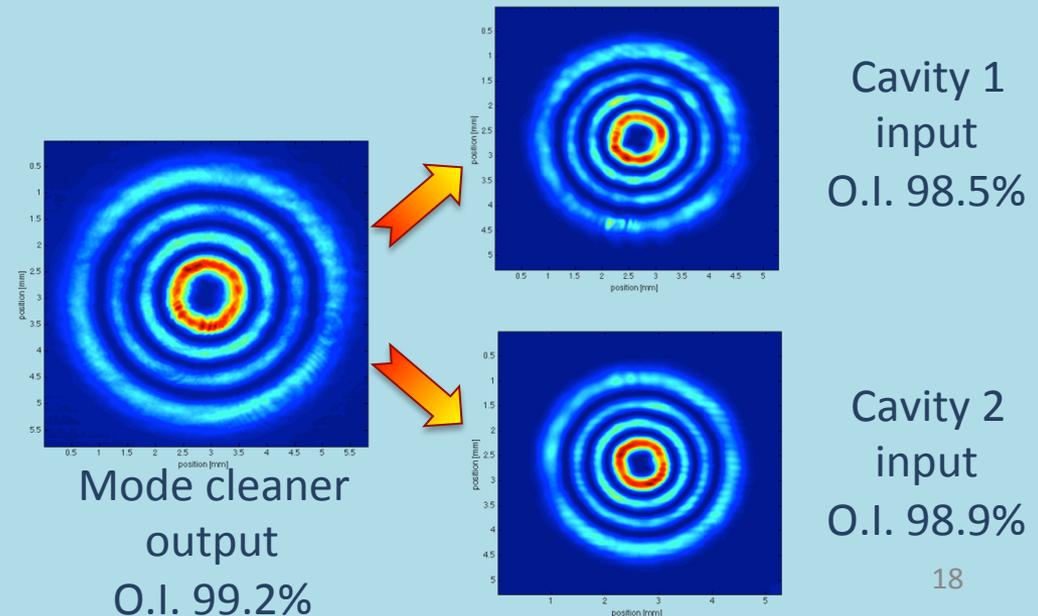
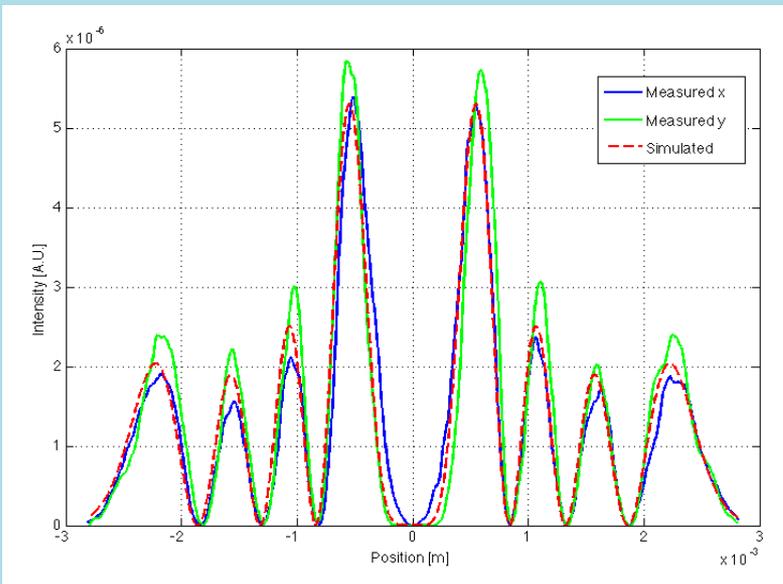


Experimental setup

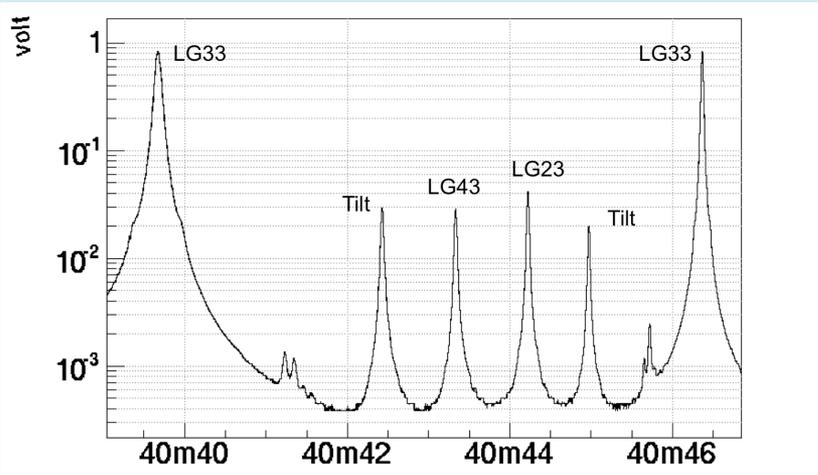


Input beam

- ✧ Gaussian and LG_{33} beams superposed before the mode cleaner input mirror
 - Alignment of the Gaussian beam in the MC cavity
 - Switching on the LG_{33} beam (only optimization required)
- ✧ LG_{33} purity (evaluated in terms of overlap integrals O.I.) maintained from mode cleaner to arm cavities input



Cavities characterization



Gaussian	Tilt	Mismatching	
	0.8% - 3%	0.2%	
LG ₃₃	Tilt	LG ₄₃	LG ₂₃
Cavity 1	3.6% - 2.4%	3.1%	5%
Cavity 2	5.5% - 4.3%	2.4%	4.2%

✧ Cavity characterization

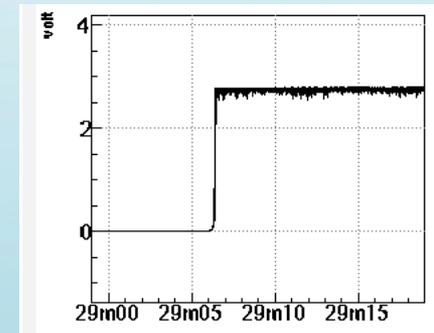
- Mismatching greater by a factor ~ 40 (confirmed by theory and simulations)
- Tilts recovered by a fine tuning of the cavity mirrors (possible only by piezo actuators)

✧ Mismatching analytical estimation

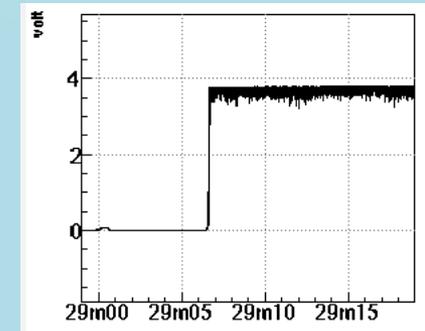
- 4.5% waist size error (only waist size error)
- 2.2 cm waist position error (only position error)

Interferometer control system

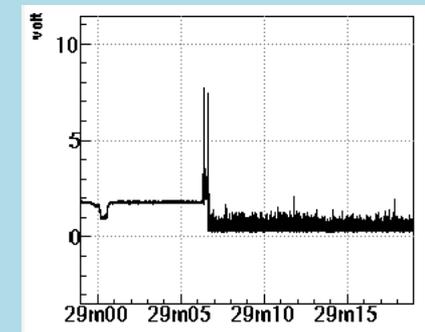
- ✧ Digital control system (AdVirgo-like)
- ✧ Arm cavities: standard control system (PDH)
- ✧ ITF: Schnupp asymmetry between arms not possible (huge impact on matching), Michelson error signal extracted through dithering
- ✧ Very fast lock and relock thanks to an automated system (software script)
- ✧ Stable locking of both arm cavities and Interferometer
- ✧ Power fluctuation given by acoustic noise (acoustic insulation received and installed in the next weeks)



Cavity 1



Cavity 2

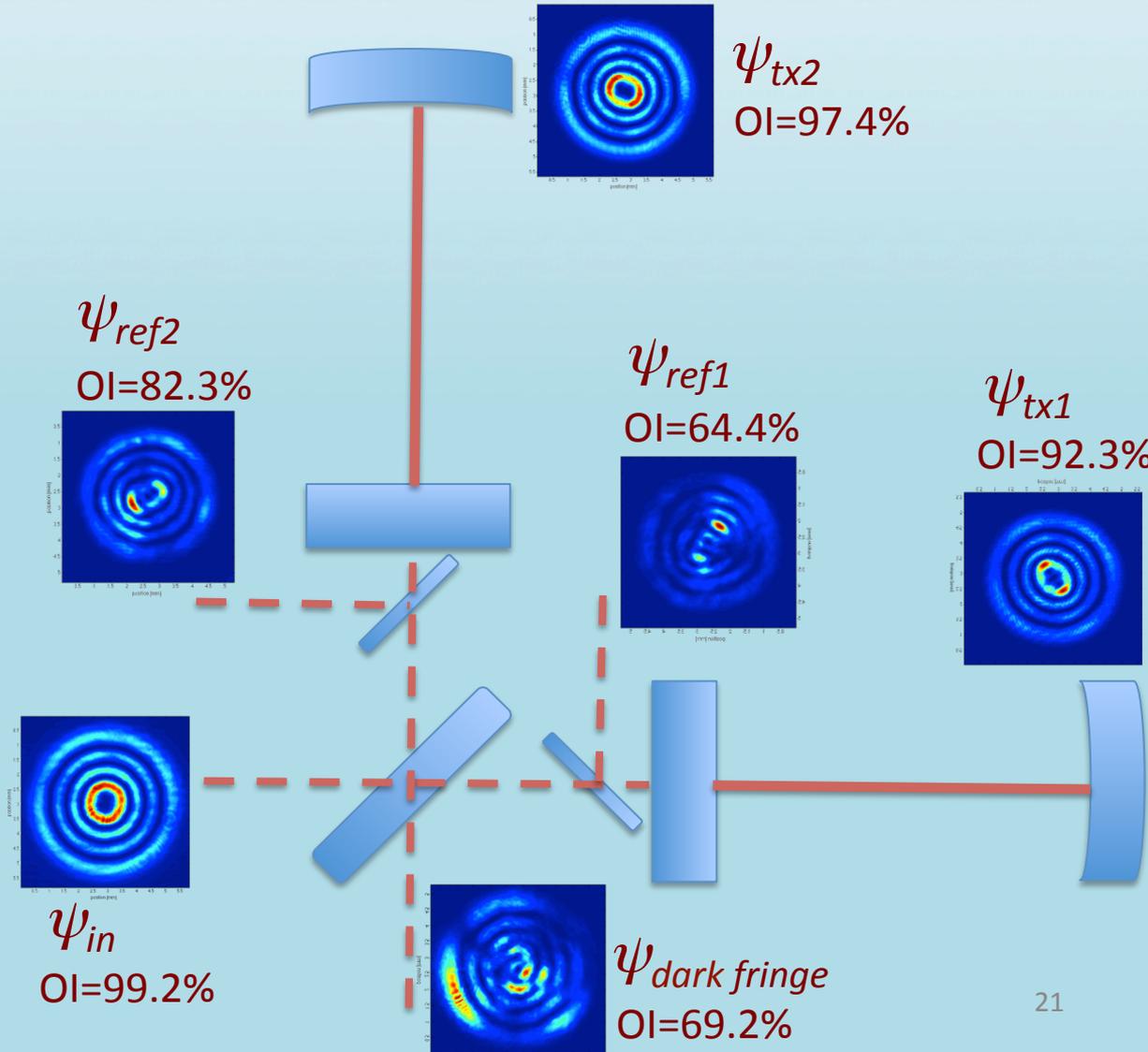


ITF

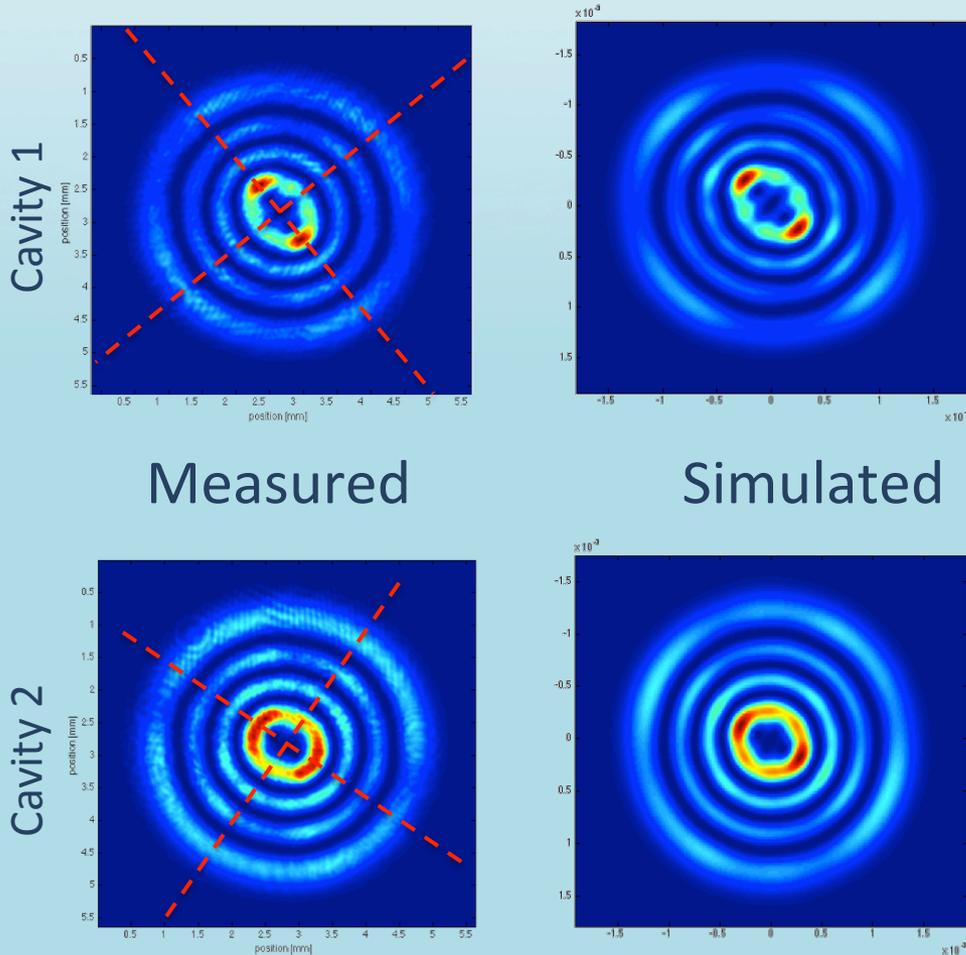
Image analysis

✧ Best visibility 74%

✧ Simulations carried out for explaining the obtained results



Transmitted beams

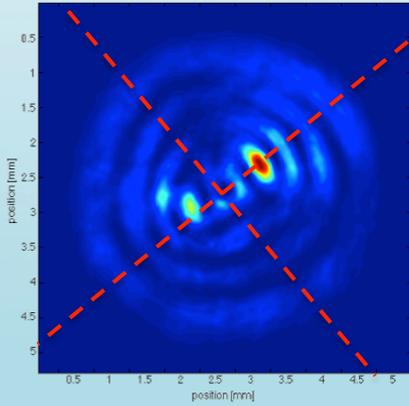


✧ Estimation starting from shapes and the relative overlap integrals

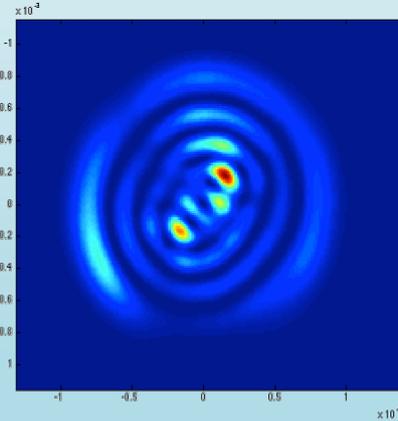
	Astigmatism
Cavity 1	0.27%
Cavity 2	0.16%

Reflected beams

Cavity 1

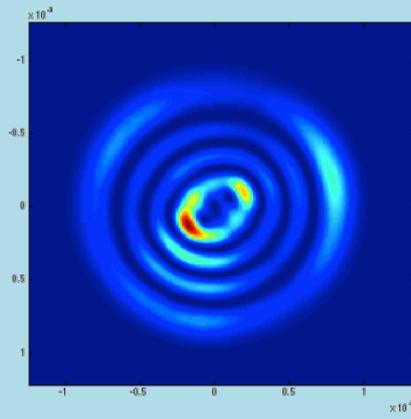
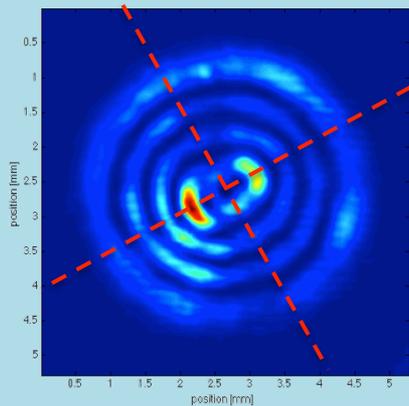


Measured



Simulated

Cavity 2

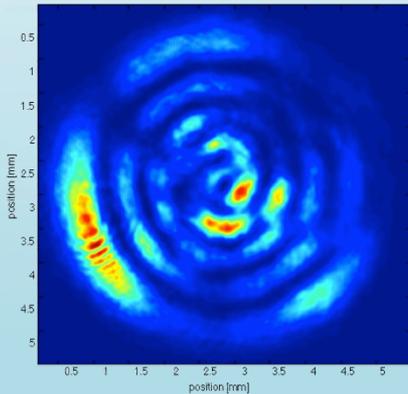


- ✧ Same astigmatism obtained in the previous slide
- ✧ Tilt estimation made from overlap integrals and resonance scans (amplitude of tilts modes)

	Tilt ITM	Tilt ETM
Cavity 1	-5 μrad (x) -50 μrad (y)	4 μrad (x) 5 μrad (y)
Cavity 2	8 μrad (x) 65 μrad (y)	-2 μrad (x) -12 μrad (y)

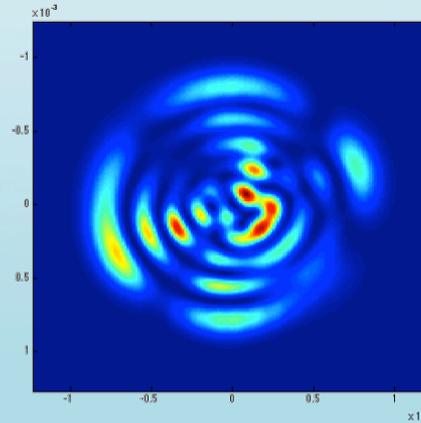
Dark fringe

Measured

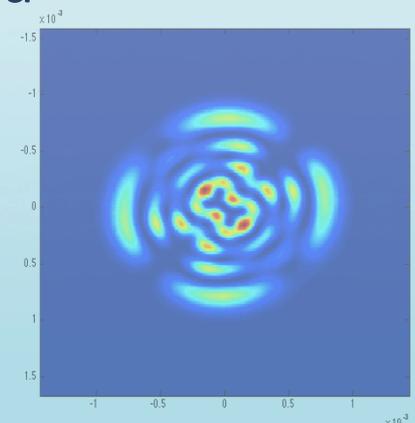


Visibility 74%

Simulated



Visibility 72%
(astigmatism+mismatch
+tilts)



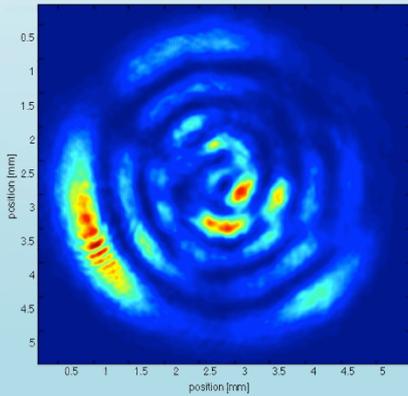
Visibility 92%
(astigmatism only)

✧ General agreement
between the measured
and simulated images

	Tilt ITM	Tilt ETM	Astigmatism
Cavity 1	-5 μrad (x) -50 μrad (y)	4 μrad (x) 5 μrad (y)	0.27%
Cavity 2	8 μrad (x) 65 μrad (y)	-2 μrad (x) -12 μrad (y)	0.16%

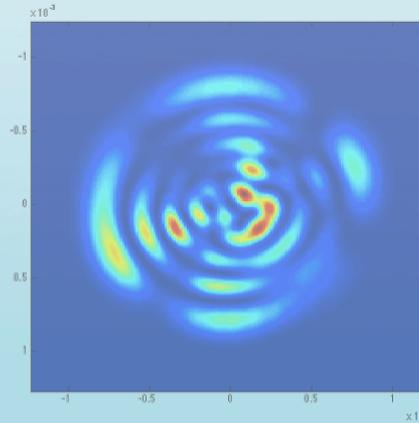
Dark fringe

Measured

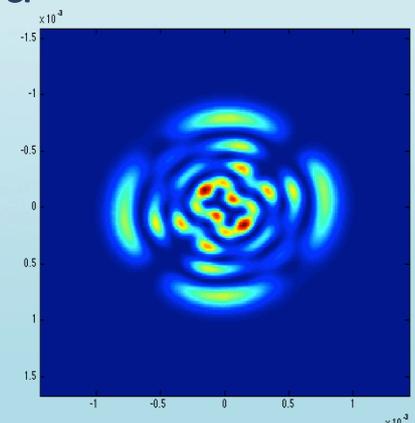


Visibility 74%

Simulated



Visibility 72%
(astigmatism+mismatch
+tilts)



Visibility 92%
(astigmatism only)

✧ General agreement
between the measured
and simulated images

	Tilt ITM	Tilt ETM	Astigmatism
Cavity 1	-5 μrad (x) -50 μrad (y)	4 μrad (x) 5 μrad (y)	0.27%
Cavity 2	8 μrad (x) 65 μrad (y)	-2 μrad (x) -12 μrad (y)	0.16%

Near-future steps

- ✧ Improve the quality of the dark fringe
 - Fine tuning of both input and end cavity mirrors by piezo actuators (planned in the next week)
 - Automatic alignment procedure using a quadrant photodiode at the dark fringe port (planned in the next week, Virgo quadrant)
- ✧ Measure of cavity mirrors maps
- ✧ Installation of acoustic insulation for acoustic noise reduction

Outline

✧ Introduction

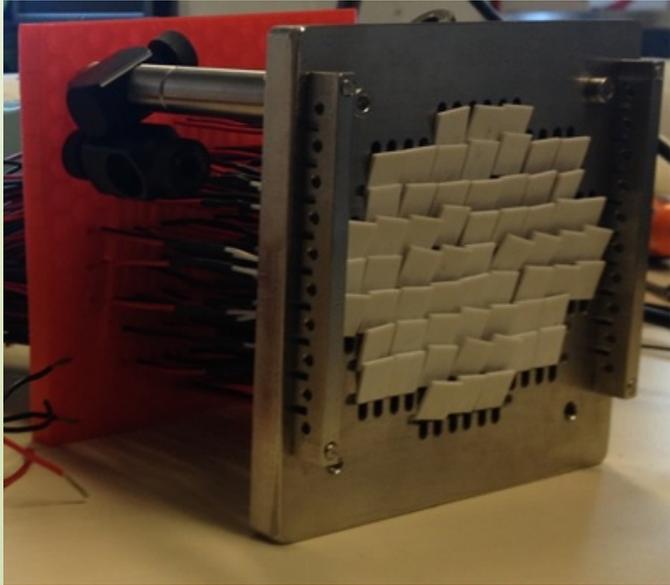
✧ State of the art

✧ Non-Gaussian interferometer at the APC

✧ **Reduction of the degeneracy**

✧ Conclusions

Thermal compensation & LG₃₃

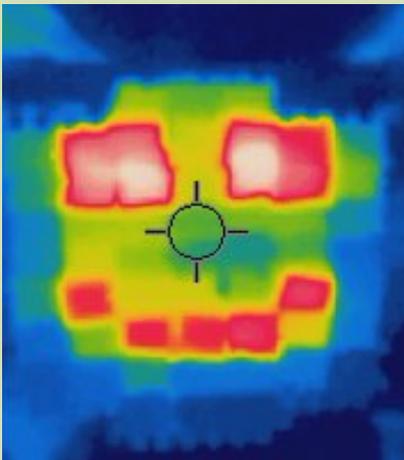


✧ Installation of the CHRAC-like thermal compensation system

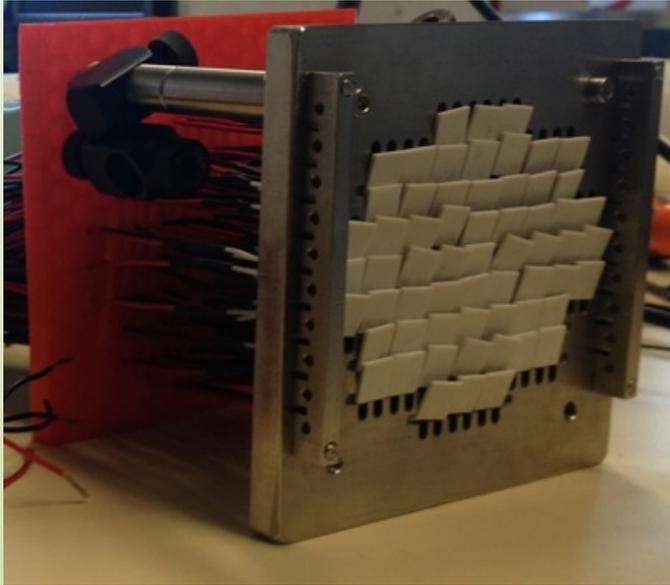
- Setup modified to accommodate the CHRAC
- BK7 cavity mirrors (higher thermal coefficient)

✧ Correction of only one cavity

- ✧ Simple cavity (transmitted and reflected beams)
- ✧ Asymmetric ITF (1 FP cavity and 1 simple mirror)

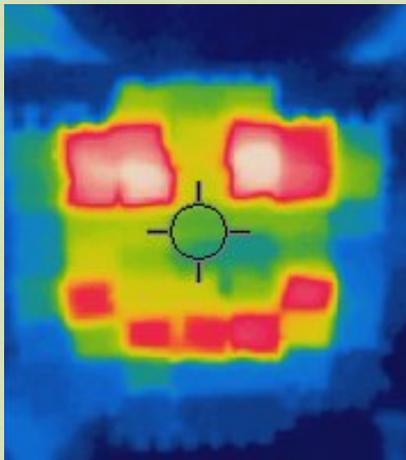


Thermal compensation & LG₃₃



✧ Installation of the CHRAC-like thermal compensation system

- Setup modified to accommodate the CHRAC
- BK7 cavity mirrors (high thermal coefficient)



See Annalisa Allocca
Friday morning

Asymmetric ITF (1 FP cavity and 1 simple mirror)

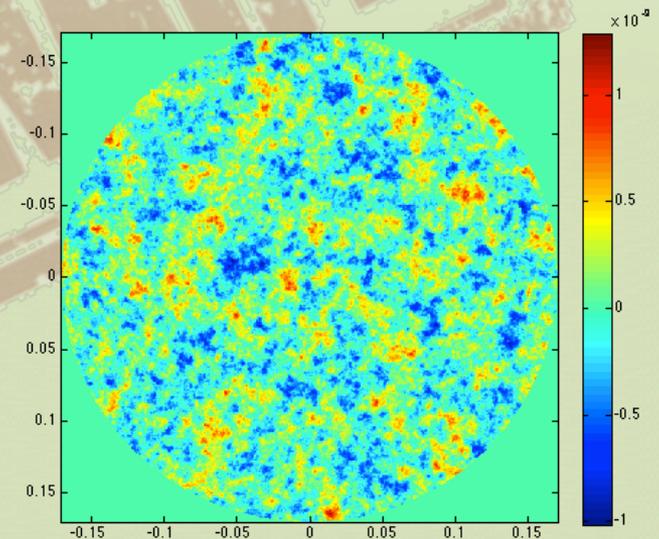
Other paths to reduce the degeneracy

AIM

Improving the contrast defect maintaining the same thermal noise reduction of LG_{33}

RMS roughness = 0.3

- ✧ 10 OSCAR simulations
- ✧ Advanced Virgo configuration
- ✧ Realistic mirror maps (generated by ITM04 PSD [5,10])



[5] T. Hong et al., Physical Review D 84, 102001 (2011)

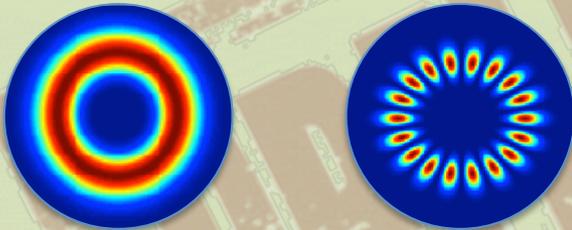
[10] H. Yamamoto, LIGO-T1100353-v1 (2011)

LG₀₉ + corrective coating

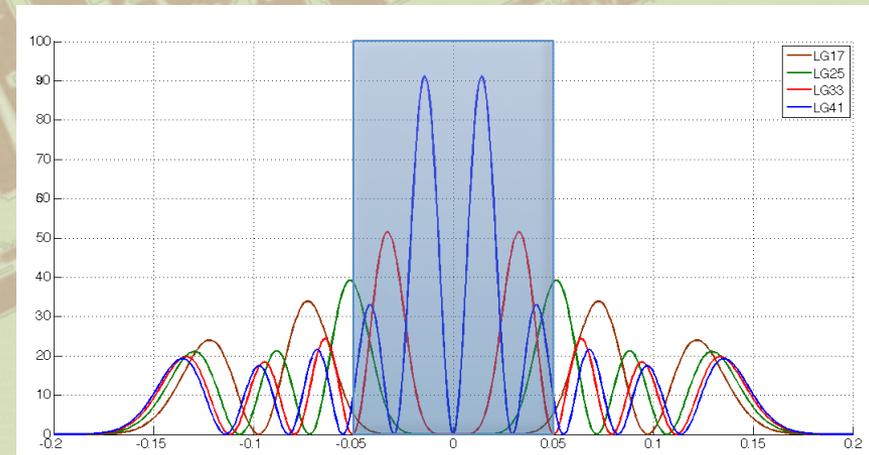
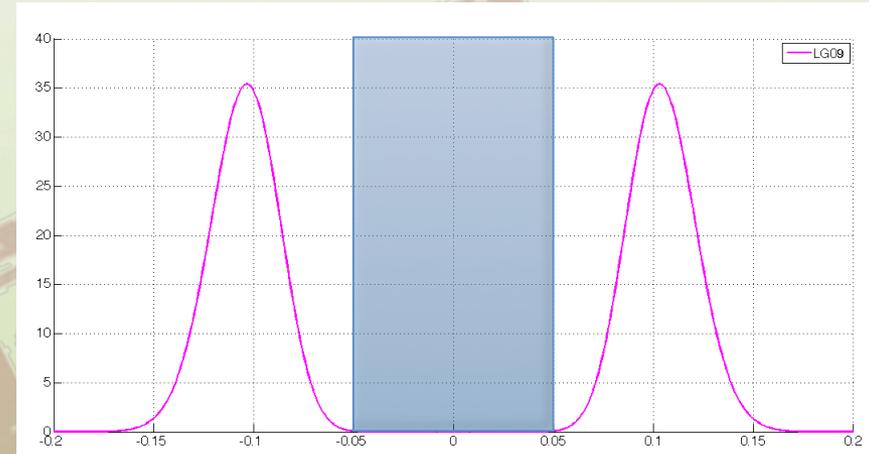
- ✧ Same order of LG₃₃ mode
- ✧ Antireflective coating (as in [5] for reducing the insurgence of other modes



Helical or sinusoidal
LG₀₉ beam



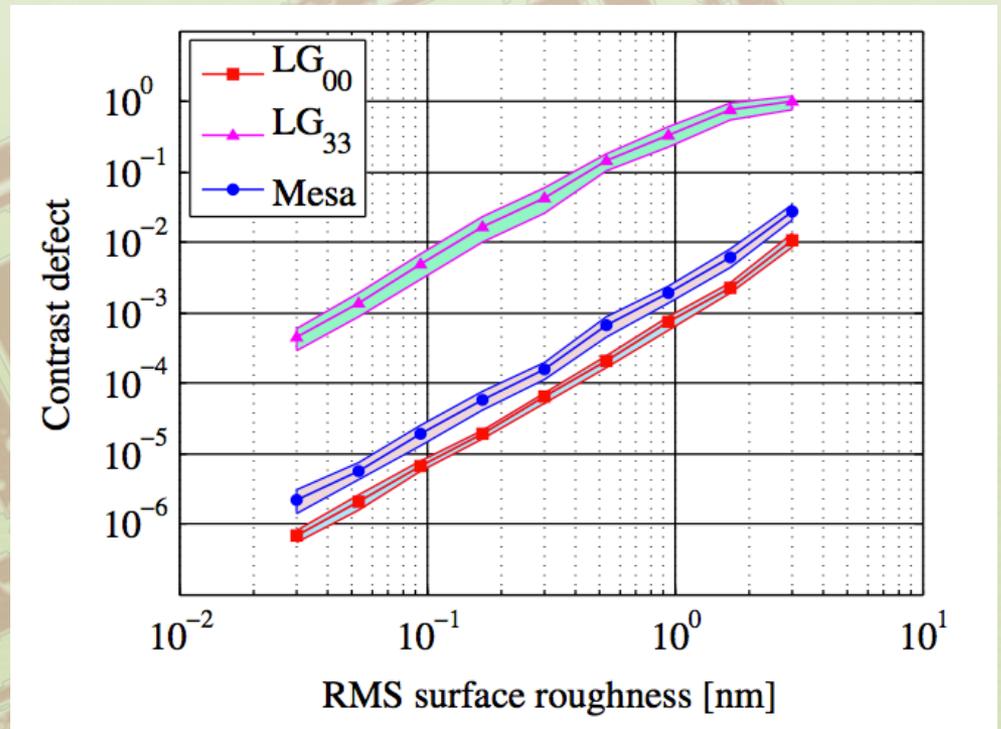
	LG ₀₉	Sin LG ₀₉	LG ₀₉ hole	Sin LG ₀₉ hole
mean	1.6	1.7	4	7.8
std	0.5	0.8	2	6.4



[5] T. Hong et al., Physical Review D 84, 102001 (2011)

But...

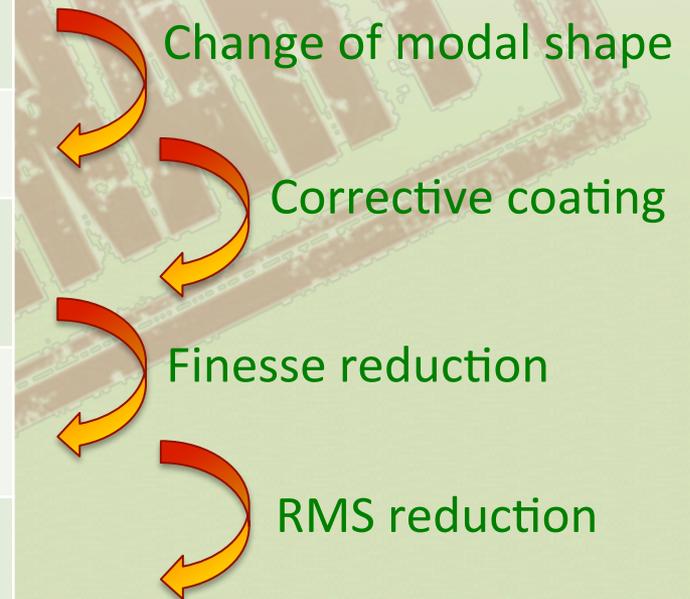
✧ In order to recover a feasible contrast defect a total gain of at least 2 order of magnitude is needed



Other solutions

✧ For obtaining an additional reduction other possible solutions have been considered

Configuration	Contrast defect
LG ₃₃ , F=450	$5.8 \cdot 10^{-2}$
Sin LG ₀₉ , F=450	$3.4 \cdot 10^{-2}$
Sin LG ₀₉ , hole, F=450	$7.7 \cdot 10^{-3}$
Sin LG ₀₉ , hole, F=225	$1.9 \cdot 10^{-3}$
Sin LG ₀₉ , hole, F=225, RMS=0.1 nm	$3 \cdot 10^{-4}$



Conclusions

✧ State of the art

✧ LG₃₃ Table-top experiment at the APC

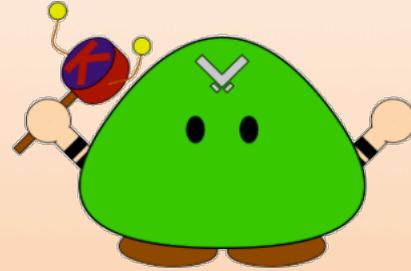
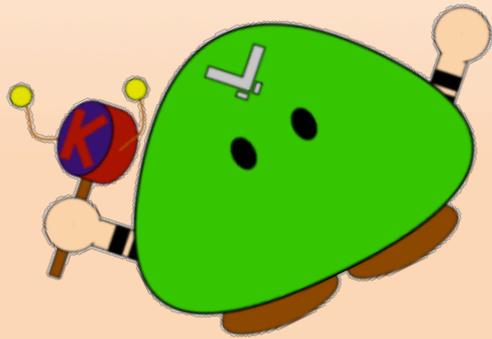
- Careful beam reduction to avoid clipping
- LG₃₃ modal purity ~99% at the input of both cavities
- Good matching of both arm cavities (mismatching ~8%)
- Stable locking of arm cavities and ITF with standard PDH error signals and dithering
- Best visibility 74%, limited by astigmatism and residual tilts
- General agreement between measures and simulations

✧ Reduction of the degeneracy

- CHRAC-like thermal compensation system installation in LG₃₃ experiment at APC
- Other paths for Advanced Virgo configuration under exploration

Next steps

- ✧ Setup improvements:
 - Automatic alignment
 - Acoustic noise reduction
- ✧ Experimental application of the thermal compensation technique on LG₃₃ table-top experiment at APC
- ✧ Under consideration
 - Study (by simulation and experiments) of other modes
 - Power recycling



Thank you!

